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Low cost bridge load test: calculating bridge displacement from acceleration for load assessment calculations

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Abstract

Bridge failure to pass load capacity assessment is unfortunately not an uncommon problem in bridge engineering and it is a potentially expensive problem for the bridge owner. Using load test data to justify increase in assessed load capacity is recognised as a viable approach in professional codes of practice. However, load tests are rarely carried out in practice because traditionally they are expensive to conduct and may not always justify an increase in assessed load capacity. Therefore this paper proposes a simple, quick and reliable approach for bridge load testing. In particular a procedure to calculate the bridge displacement to a moving truck by double integration of bridge acceleration is presented. Integrating acceleration to calculate displacement is not a new approach, with authors reporting difficulties due to errors in acceleration signals and unknown initial conditions. Many of the previous approaches have focused on developing signal processing algorithms to correct for the signal errors and while some good results have been reported, typically the derived displacements are very sensitive to parameters used in the correction algorithm, such as passband filter frequencies. Consequently, without comparison with directly measured displacement data, reliability of the procedure cannot be established and errors quantified. Therefore in this study a stripped down procedure is applied placing emphasis instead on minimising the errors in the recorded acceleration by using appropriate hardware and developing a quality control procedure that allows the user to assess the likely accuracy of the calculated displacement signal. The effectiveness of the proposed approach is trialled in the laboratory and in the field, with an accuracy of $\pm 0.5\text{mm}$ observed.

Keywords

Bridge; Load test; Bridge acceleration; Displacement monitoring;

1.0 Introduction

1.1 Bridge assessment and load testing

Load carrying capacity assessment of a bridge generally is carried out using a Finite Element (FE) model of the bridge to calculate the load effects (e.g. bending moments and shear forces) generated due to the prescribed loads. If the load effects predicted by the model are greater than the calculated load capacity of the deck, the bridge owner/operator is faced with a difficult and potentially expensive problem as even limited strengthening works are expensive. The possibility that a given bridge may have reserves of strength in excess of the calculated value (e.g. as shown by field testing in [1]) means that there has been a growing interest in using load test results to justify

39 increasing the assessed load capacity following a failed load capacity assessment. Broadly speaking a
40 load test involves placing load(s) of known magnitude on the bridge and measuring displacement
41 and/or strain. Bridge assessment codes (e.g. [2], [3]) recognise the potential benefits of conducting a
42 load test and they specifically allow for their use. Despite this, load tests are rarely carried out for a
43 number of reasons:

- 44 (i) traditionally they require specialist equipment and are expensive to implement,
- 45 (ii) they slow the decision process because they take significant time to organise and
- 46 (iii) there is no guarantee that the test will result in an increase in assessed capacity.

47

48 However, in the opinion of the authors, following a failed initial load carrying assessment a
49 quick/reliable method for performing a load test would be very attractive to bridge engineers due to
50 the high potential reward compared to cost. Therefore this paper proposes a simple, reliable,
51 approximate approach for load testing. In particular a procedure to calculate the bridge
52 displacement to a moving load by double integrating bridge acceleration is presented and trialled
53 successfully in the field. The method requires limited equipment (accelerometer, video camera, test
54 truck) and limited planning (no special access equipment or traffic management). Specific details on
55 the proposed method and the results obtained are given in Sections 2-5. However, to give some
56 background on the area, section 1.2 gives a brief overview of conventional sensing systems used for
57 tracking bridge displacement, and Section 1.3 provides an overview of previous work on integrating
58 acceleration signals to calculate displacement. As already mentioned, strain could be measured
59 during a load test but for a quick and easy load testing, strain is not particularly suitable. This is
60 because it is often relatively complicated to access and attach strain gauges to the underside of
61 bridge decks and this motivates the use of easier to deploy accelerometers. (For brevity, the
62 underside of the bridge deck will be hereafter referred to as the 'soffit').

63

64 1.2 Conventional methods for tracking bridge displacement

65 Traditionally the difficulty with measuring bridge displacement in the field is the absence of a fixed
66 reference point means that standard displacement measuring sensors such as Linear Variable
67 Differential Transformers (LVDT) cannot be used. A number of bridge displacement monitoring
68 approaches have been implemented, each with their own advantages and disadvantages and the
69 choice of technology for bridge deformation measurements is discussed elsewhere e.g. [4]. Often
70 the method selected depends on factors such as spatial range/resolution, sample rate/frequency
71 response, number of axes and stability of fixed reference points. For short span bridges over
72 accessible land LVDTs can sometimes be used if the bridge deck is not too high and the user is only
73 interested in vertical deflection. For example LVDT's are used in this study to measure the vertical
74 displacement of a bridge and Moreau et al. [5] use LVDT's for a similar purpose However, in reality
75 LVDT's are rarely practicable in the field and not suitable at all for long spans over water and
76 inaccessible open space. For these kind of bridges, options include total stations [6] and hydraulic
77 level sensing [7] however, GPS is increasingly becoming the most common approach. At the end of
78 the 1990s Roberts et al. [8] used GPS to track the displacement of the Humber suspension bridge to
79 a convey of 5 trucks. In more recent work Mochas & Stiros [9] used GPS to successfully track the
80 displacement of a relatively stiff footbridge. Notwithstanding the work in [9] has limitations,

81 particularly for shorter spans where movement ranges are modest. Therefore more recently a
82 number of authors have placed emphasis on trying to identify bridge deflection using vision based
83 systems and some promising results have been reported. Some of these systems are commercially
84 available (e.g. Imetrum [10]) however they tend to be expensive and require a certain level of
85 expertise to operate. Similar vision based systems have been developed by researchers and
86 presented in the literature [11]–[13] and while these have the advantage of being cheaper (than the
87 commercial systems) they take time and expertise to implement. As well as the cost and/or
88 expertise required to use vision based systems, there are challenges to using them in the field, in
89 particular, (i) camera/lens stability and (ii) varying light conditions. In the field the camera will
90 typically be tens of metres from the bridge deck, requiring highly stable camera mounting to avoid
91 significant errors. For example, a camera 30 m from the bridge deck rotated by just one minute of
92 arc on its support equates to a deck displacement of several millimetres. Typically image tracking
93 algorithms work by tracking a user defined pixel zone of interest (or target) between successive
94 frames, however changing lighting condition might disturb system’s capability for target recognition.
95 Finally a number of authors [14]–[19] have looked at the problem of calculating bridge displacement
96 from acceleration and the work of these authors is described in more detail later in this section,
97 however, first a general overview on the topic of calculating displacement from acceleration signals
98 is provided.

99 1.3 Integrating acceleration to calculate displacement

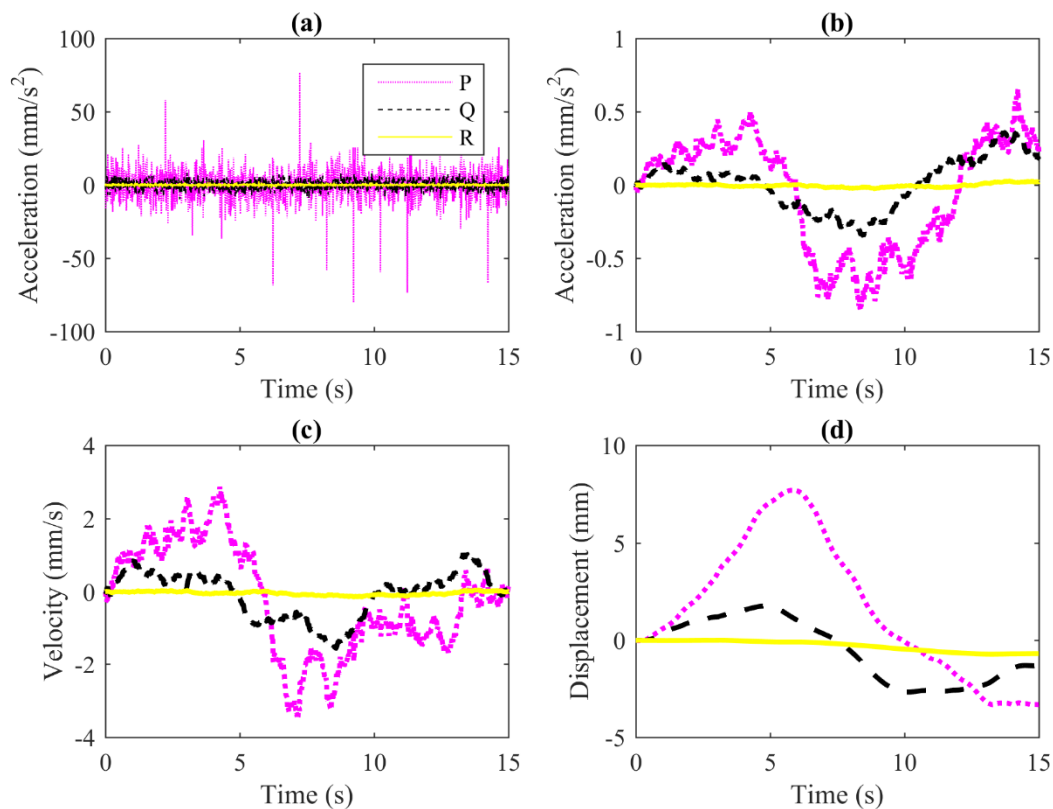
100 Due to the cost/logistical difficulties associated with the methods mentioned in the previous section
101 this paper explores a simple and low cost approach to calculating approximate displacement from
102 acceleration signals. In particular the challenge of calculating the displacement of a bridge due to the
103 passage of a truck is examined, for a load test without the need for traffic management on bridge.

104 Aside from not knowing exactly the initial conditions (velocity and displacement), the fundamental
105 problem with integrating acceleration to calculate displacement is amplification of the low
106 frequency noise that inevitably exists in real acceleration data. Thong et al. [20] give a useful
107 overview on the challenge of doubly integrating acceleration measurements containing noise.
108 Essentially measured acceleration and subsequent computation of velocities and displacements are
109 stochastic variables/processes, characterized by errors (noise) and Stirios [21] provides a rigorous
110 mathematical discussion on this issue. He demonstrates how the errors/noise in the acceleration
111 records are amplified and accumulated during the double-integration procedure. More recent work
112 on the same topic by Moschas et al. [22] demonstrates the same thing using experimental data
113 supported by Finite Element Modelling and detailed statistical analysis. The effect of integrating
114 noise is demonstrated on 15 seconds of acceleration data simultaneously recorded by three
115 different accelerometers, P,Q, R placed on a rigid laboratory floor (Fig. 1(a)). The signals in Fig. 1(a)
116 are expected to be almost entirely broadband accelerometer noise with a small component due to
117 genuine sub-micron ground vibrations at frequencies generally above 5 Hz [23]. The low frequency
118 component of this noise can be exposed by its removal using a moving average filter (a form of low
119 pass filtering).The result after filtering is shown in Fig. 1(b), where the y-axis limits are two orders of
120 magnitude lower than in Fig 1(a). Fig.1(b) shows that signal P has the most low frequency noise,
121 signal R has the least, and signal Q is somewhere in between. The significance of this low frequency
122 noise is evident when acceleration signals P-R shown in Fig. 1(a) are double integrated to
123 displacement, Fig. 1(d).

124 Double integrated signals from accelerometer P suggest that, starting from zero the sensor
 125 experienced a maximum displacement of 8mm at approximately 6 seconds, thereafter it gradually
 126 reduced, reaching -2mm at around 13 seconds where it remained for the rest of the window. Data
 127 from accelerometer Q suggest that the sensor experienced an approximately sinusoidal
 128 displacement over the course of the 15 seconds with an amplitude of approximately 2 mm. Finally
 129 acceleration signals from accelerometer R suggest a displacement of close to zero for the duration of
 130 the 15 second window. If the plot from accelerometer R is examined at a zoomed in scale then
 131 displacement in the range $\pm 0.2\text{mm}$ are evident.

132 The double integration from Fig 1(a) to Fig 1(d) involves the following simple steps:

- 133 (i) apply a linear de-trend function to the raw acceleration signal (Fig. 1a),
- 134 (ii) assume initial velocity is zero, integrate using MATLAB 'cumtrapz' function to calculate
 135 velocity (Fig. 1c) and
- 136 (iii) assume initial displacement is zero and integrate again to obtain displacement (Fig. 1d).



137

138 Fig. 1, Overview of the challenge of obtaining displacement from acceleration signals, (a) raw
 139 acceleration from accelerometers P, Q and R (b) acceleration data after application of moving
 140 average filter to expose low frequency component of measurement noise, (c) velocity following 1st
 141 integration (sensors with largest low frequency noise in part (b) show largest calculated velocity) (d)
 142 displacement following 2nd integration where calculated displacements are approximately
 143 proportional to the low frequency noise observed in (b).

144

145 Recovering dynamic displacements of all but the very long span bridges is more straightforward
146 since the spurious displacement demonstrated in Fig. 1 can be partially avoided by high pass filtering
147 the acceleration signal prior to integration. However, to calculate the displacement response of a
148 bridge due to the passage of a truck the low frequency component of the acceleration signal must
149 be retained as this is the part of the spectra that contains quasi-static response associated with the
150 prescribed moving load. In this case it is challenging to identify a suitable high pass filter cut-off
151 frequency.

152 In the following review of previous research on recovering quasi-static displacements it is observed
153 that the integration procedures involve correction of the signals to conform to an expected shape. A
154 simple example of this is seen in Fig 1. Because the acceleration data were collected from
155 accelerometers placed on rigid ground the true displacement signal in Fig. 1(d) should be a
156 horizontal line of zero displacement. This in turn requires a horizontal line of zero velocity, and to
157 achieve this in the first integration stage a simple 'correction' can be devised. For example, a best fit
158 polynomial fit to signal P in Fig. 1(c) can be subtracted from the signal to leave an approximate
159 flatline velocity which on further integration will yield a more credible displacement. The simple
160 example demonstrates the concept behind all correction methods, i.e. in that the knowledge of the
161 shape of the true displacement signal can be used to establish the approximate shape of the true
162 velocity signal. Then mathematical algorithms can be devised to 'correct' the calculated velocity
163 signal to bring it more in line with the theoretically true velocity signal.

164 Correction approaches of this type are generally known as a base line correction methods (BCM).
165 Heng et al. [24] give a useful summary of how this approach is implemented, with some of the
166 earliest work in this area directed to recovering permanent ground displacements from
167 accelerograms, or earthquake acceleration records [25], [26]. Other methods use a combination of
168 BCM and high-pass filtering, e.g. [27]. One of the difficulties with applying BCM to earthquake
169 acceleration records is the possibility that the acceleration record contains a genuine 'fling step', i.e.
170 a true displacement reflecting permanent deformation due to the earthquake. Therefore not
171 something to be corrected for, or removed. However, in structural engineering typically such issues
172 do not arise which makes the use of baseline correction a reasonable approach.

173

174 A number of authors have applied BCM related methods to recover truck-induced bridge
175 displacements. Faulkner et al [14] use a combination of BCM and high-pass filtering to calculate the
176 response of a bridge to a moving load, showing that provided a suitable pass-band frequency is
177 chosen, even the forced part of the displacement signal (i.e. the portion of the signal when the truck
178 is on the bridge) can be determined reasonably reliably. However, no guidance is provided on
179 choosing the pass-band frequency for a given bridge which is a major limitation given the strong
180 effect this choice has on the recovered displacement. Paultre et al [15] also use a combination of
181 BCM and high-pass filtering to calculate the displacement of a bridge due the passage of a truck.
182 Again they show good agreement between calculated displacement and displacement recorded
183 using an LVDT, but no guidance on pass band frequency is provided. Park et al [16] present an
184 excellent study where they propose a correction method they term 'Velocity Estimation Method'
185 (VEM) which shows good performance, but again the issue of parameter choice for the integration
186 method remains problematic. Gindy et al. [17] propose a similar but slightly simpler correction

187 method with comparison using an LVDT but in addition they measured bridge velocity
188 experimentally using a laser system to show good agreement at the intermediate stage.

189 In an effort to calculate the ‘approximately true’ bridge displacement from an acceleration record,
190 the methods described above attempt to ‘correct’ the calculated velocity signal to mitigate the
191 natural errors (noise) that occur in the recorded acceleration. Another approach is to ‘correct’ the
192 recorded acceleration data prior to integration by attempting to fit a mathematical function that
193 captures the true acceleration in the recorded acceleration but not the unwanted noise. For
194 example Kropp [18] showed that an appropriate polynomial fitted to a bridge acceleration signal
195 could be integrated to provide a reasonable indication of the maximum displacement, even if the
196 calculated displacement signal did not exactly follow the displacement signal recorded on the bridge
197 using a deflection gauge. Gindy et al. [19] used a state space model to try to represent the noise free
198 acceleration. Double integration of this modelled acceleration provided a very good match with the
199 displacement signal recorded on the bridge.

200 The fundamental problem with the approaches described is that the user has to select certain
201 ‘parameters’ to be used in the algorithm (e.g. the pass band filter frequencies or polynomial order)
202 and which are problematic to choose correctly. Further, if a directly measured displacement signal is
203 available the user can adjust the parameters to obtain the best match. These issues are well
204 demonstrated by Graves [28] who applied correction methods suggested in [29], [30] to acceleration
205 data recorded during a number of different earthquakes, finding that the parameters can be (in his
206 words) ‘tuned’ until the calculated displacement matched the residual displacement data provided
207 directly by GPS.

208 It is important to point out that, although Graves [28] was talking about processing earthquake
209 records his observation is equally relevant when dealing with bridge acceleration signals. the ability
210 to find a suitable processing algorithm is significantly increased if the analyst can ‘tune’ the
211 parameters to match the recorded displacement. However, if these ‘tuned’ parameters are then
212 applied to acceleration signals from a similar, but slightly different bridge, or to the same bridge with
213 slightly different loading conditions but without directly measured displacement for comparison
214 there is no way to characterise the errors in the calculated displacements

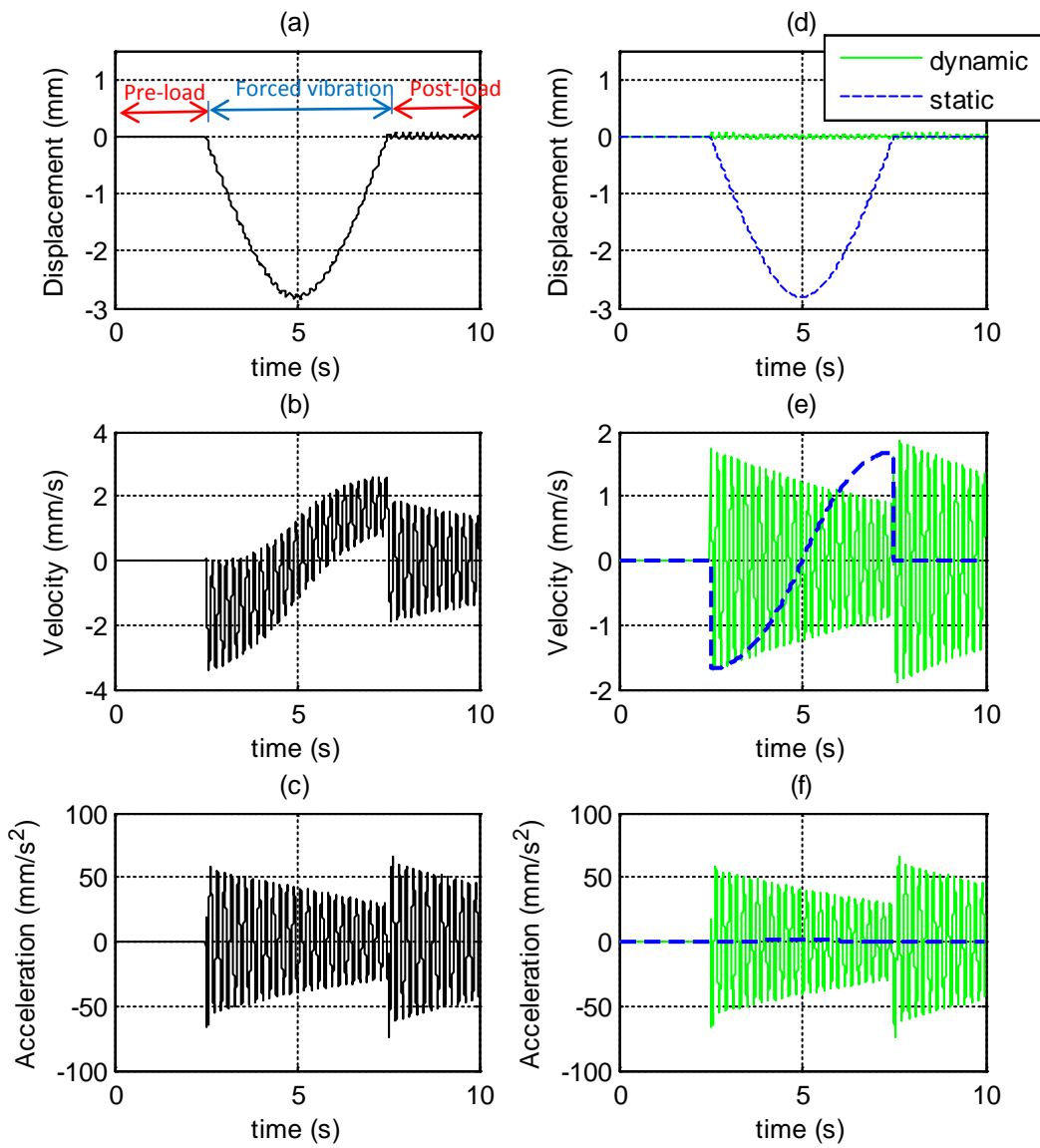
215 Therefore the focus in this paper is not on developing a new algorithm for calculating bridge
216 displacement from acceleration but rather to:

- 217 (i) minimise the errors in the recorded acceleration by using appropriate hardware, and
- 218 (ii) develop a quality control procedure that allows the user to assess the likely accuracy of the
219 calculated displacement signal.

220 To this end, Section 2 explains how the static component of the bridge response to be recovered
221 presents in the acceleration signal, Section 3 demonstrates how the accuracy of the calculated
222 displacement is affected by the quality of accelerometer used, Section 4 demonstrates the
223 effectiveness of the proposed approach using data collected during a laboratory trial, and Section 5
224 validates the proposed approach using data collected in the field.

225 **2.0 Basic Theory**

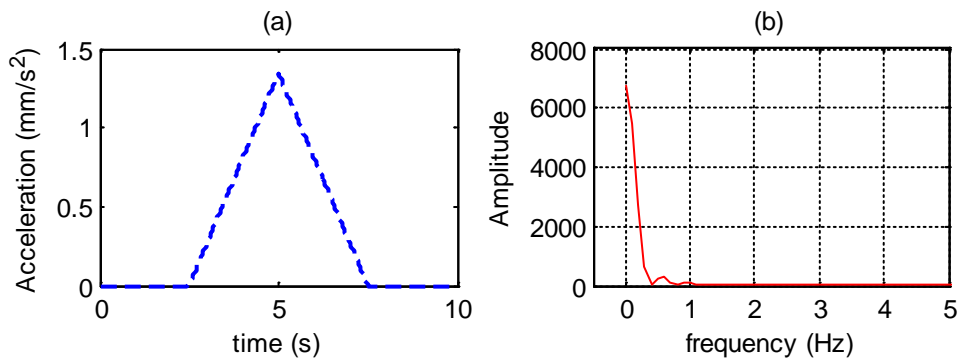
226 This section provides a graphical overview of how the static component of a bridge displacement
227 signal presents in the corresponding acceleration signal. To demonstrate this a simple model,
228 developed in MATLAB and described in detail in [31], simulates a point load crossing a beam. Figs.
229 2(a)-(c) show the mid-span displacement, velocity and acceleration, respectively, as a point load
230 travelling at 4 m/s crosses a beam with a span of 20 m. This is a very crude representation but
231 modelling the truck as a single point force is sufficient to demonstrate in Fig. 2(a) the combination of
232 static and dynamic bridge response to a moving truck. The load does not enter the bridge until 2.5
233 seconds into the simulation and equally 2.5 seconds of post load signal is included at the end of the
234 simulation. The 'pre-load' and 'post-load' indicated in Fig. 2(a) are included to replicate the kind of
235 signals that will be integrated later in the paper, i.e. a short portion before the truck arrives, the
236 forced part where the truck is on the bridge, and a short part of the post-load signal after the truck
237 leaves. Fig. 2(d) shows the static and dynamic components of the displacement signal shown in (a) as
238 dashed and solid plots, respectively. The static component is obtained by incrementally moving the
239 load across the bridge, applying it statically at each location and calculating the mid-span
240 displacement. The dynamic component is calculated by subtracting the static component from the
241 signal shown in Fig 2(a). Fig. 2(e) shows the component parts of the velocity signal, obtained by
242 differentiating the static and dynamic components of displacement shown in (d). Finally Fig. 2(f)
243 shows the static and dynamic components of the acceleration signal calculated by differentiating the
244 velocity components in (e). In Fig. 2(f) it can be seen that the amplitude of the dynamic
245 component of acceleration totally dwarfs the static component which appears as an almost straight
246 line. However, Fig. 3(a) reproduces the dashed curve of Fig. 2(f) at a magnified scale revealing it to
247 have a triangular shape. Fig. 3(b) shows the frequency content of the signal shown in Fig. 3(a) with
248 the expected energy concentration at the low end of the spectrum. In fact it is the static component
249 shown in Fig. 3(a) that when integrated will provide the static component of displacement. The
250 difficulty is acceleration signals recorded on real structures will inevitably contain some level of
251 unwanted low frequency noise, distorting the static component of acceleration, resulting in errors in
252 the calculated displacement. In the next section the error (in mm) that can be expected from five
253 different accelerometers is quantified.



254

255 Fig. 2, Total response of the mid-span section and its components due to a force travelling at 4m/s:
 256 (a) total displacement; (b) total velocity; (c) total acceleration; (d) components of displacement; (e)
 257 components of velocity; (f) components of acceleration.

258



259

260 Fig. 3, Static components of acceleration signal (a) in time domain (b) in frequency domain

261 3.0 Trialling Different Accelerometers

262 As already explained when choosing the accelerometer the most important consideration is that the
 263 low frequency noise is minimised because it will dominate errors in calculated static displacement.
 264 Therefore the performance of a number of different accelerometers is examined by calculating
 265 displacements from acceleration signals recorded on a (rigid) floor in the laboratory. Knowing the
 266 correct results to be 'zero' allows an assessment of the errors to be expected when using each type
 267 of accelerometer. Some types of accelerometer are inherently unsuited for recovering quasi-static
 268 displacements and are not used in this experiment, for example piezoelectric accelerometers
 269 designed for shock and vibration applications usually cannot reliably capture frequencies below 0.5
 270 Hz.

271 In this study five different accelerometers are trialled, four micro-electrical-mechanical-system
 272 (MEMS) accelerometers (GCDC, Opal, K-Beam, JA) and one force balance accelerometer (QA), all
 273 capable of detecting static acceleration due to gravity, i.e. at 0 Hz. Fig. 4 shows these five
 274 accelerometers, and a brief description of each is given below.

275 **GCDC:** Manufactured by Gulf Coast Data Concepts (Fig. 4(a)), it is robust, inexpensive and very easy
 276 to use/deploy. Using a simple .txt file the user specifies parameters such as scanning rate,
 277 acceleration threshold above which data is to be recorded, etc., and the data can be downloaded via
 278 the USB connection. The specification sheet for the sensor does not specify the noise that can be
 279 expected. The accelerometer in the device is a triaxial MEMS Kionix KXRB5-2050 and while the 'noise
 280 density' for this accelerometer is available in the literature ($0.00044 \text{ m/s}^2/\sqrt{\text{Hz}}$), this will be less than
 281 the total sensor noise.

282 **Opal:** Manufactured by APMD Inc, these are designed for use as part of a wireless sensor network in
 283 biomechanical applications (Fig. 4(b)). The device contains a gyroscopes and magnetometers as well
 284 as a triaxial MEMS accelerometer. The specification states accelerometer noise to be 0.0012
 285 $\text{m/s}^2/\sqrt{\text{Hz}}$.

286 **K-Beam:** Manufactured by Kistler, the type 8315A (Fig. 4(c)) is a uniaxial MEMS accelerometer with a
 287 measurement range of $\pm 2g$. The specification states accelerometer noise to be $0.00025 \text{ m/s}^2/\sqrt{\text{Hz}}$.

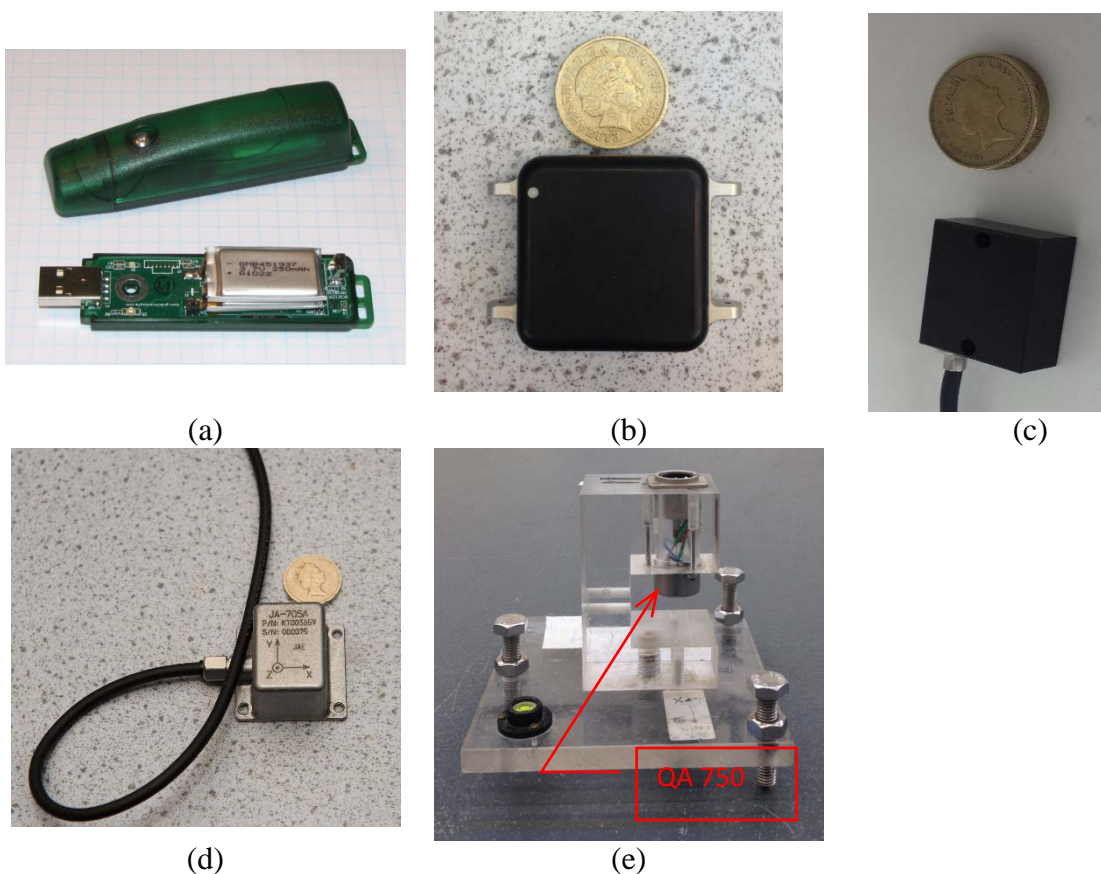
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289 **JA:** The JA-70SA manufactured by Japan Aviation Electronics is an extremely low noise MEMS triaxial
290 accelerometer. The specification gives noise as better than $0.00001 \text{ m/s}^2/\sqrt{\text{Hz}}$

291

292 **QA:** The navigation grade force balance accelerometer (QA-750) manufactured by Honeywell (Fig.
293 4(e)) is uniaxial sensor and the most expensive device in this trial. However, they provide excellent
294 performance with respect to noise, $<0.000069 \text{ m/s}^2/\sqrt{\text{Hz}}$ (0-10 Hz) and $< 0.00069 \text{ m/s}^2/\sqrt{\text{Hz}}$ (10 -500
295 Hz). Fig. 4(e) shows a photo of the QA accelerometer mounted in a perspex housing with cable
296 connectors and a perspex base plate with three steel foot screws for levelling when used on uneven
297 ground.

298

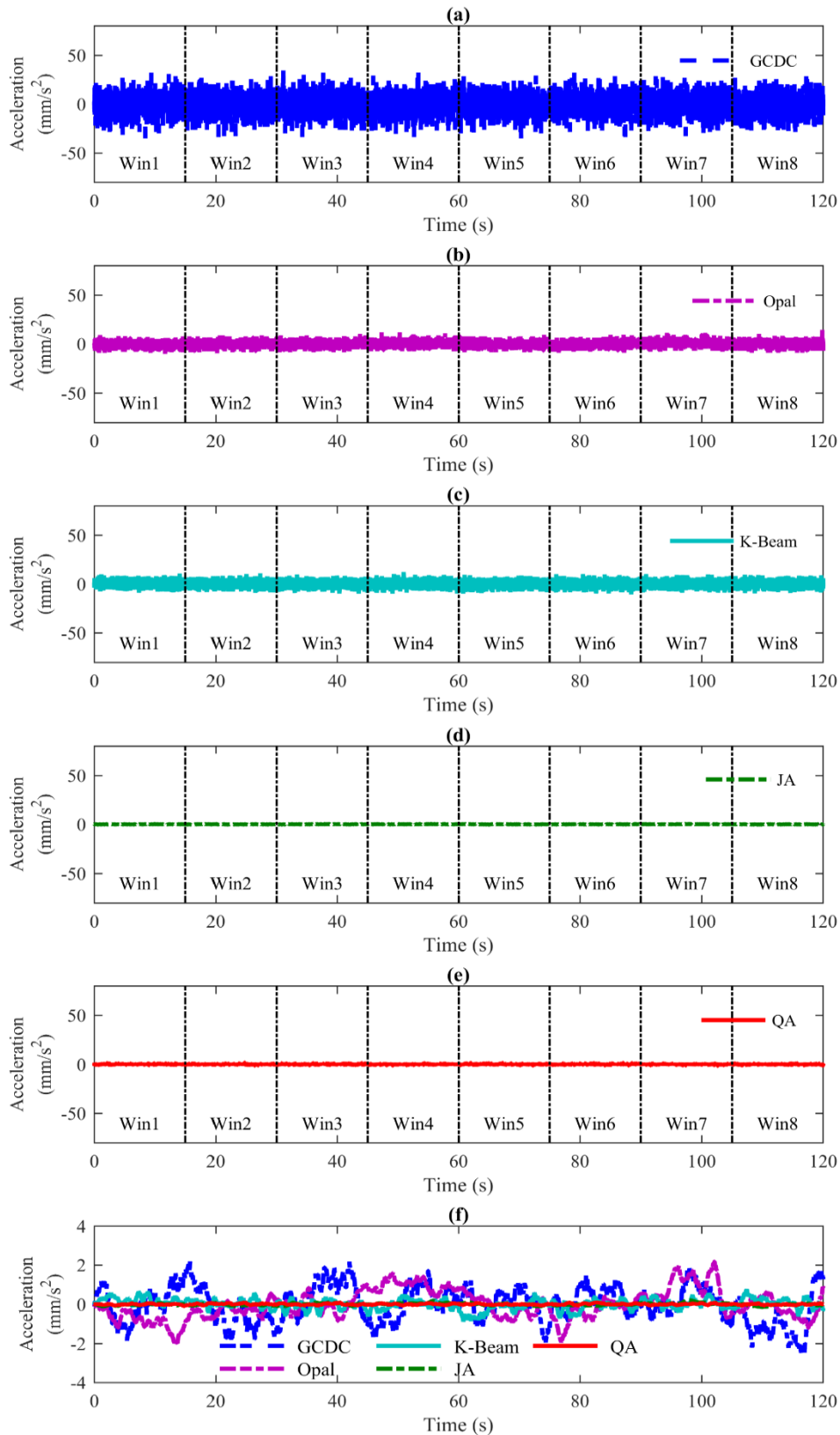


299 Fig.4, Accelerometers trialled in this study (a) GCDC: low cost MEMS accelerometer with on board
300 power and logging capability, (b) Opal: higher quality MEMS accelerometer with on board power and
301 logging capability , (c) K-Beam: conventional MEMS accelerometer which requires external power
302 and data logger , (d) JA high quality MEMS accelerometer which requires external power and data
303 logger, (e) QA: Aviation grade force balance accelerometer which requires external power and data
304 logger .

305

306 120 seconds of acceleration signal from the GCDC, Opal, K-Beam, JA and QA accelerometers placed
307 on the rigid laboratory floor are shown in Figs. 5(a) to (e), respectively. Each signal was recorded
308 with a scanning frequency of 128 Hz. The y-axis limits in each of the five plots (a-e) are the same and

309 it is immediately obvious that the GCDC has the largest noise, the QA and JA accelerometers have
310 the least noise, with the level of noise in the Opal and K-Beam accelerometers somewhere in
311 between. This is consistent with the noise levels in the sensor specifications. The noise evident in
312 plots (a)-(e) is high frequency noise, although as shown in section 2 it is actually the low frequency
313 part of the acceleration that most strongly affects calculating displacement from acceleration. To
314 get a feeling for what this low frequency noise looks like in the time domain a 6-second moving
315 average filter was applied to each of the signals shown in Fig. 5 (a)-(e) to remove the high frequency
316 component with the result shown in Fig 5(f) using y axis limits 20 times smaller than those used in
317 plots (a-e). Again the GCDC exhibits the most noise, the QA and JA contain the least noise, with the
318 Opal and the K-Beam somewhere in between. The moving average filter played no further role in
319 this study.



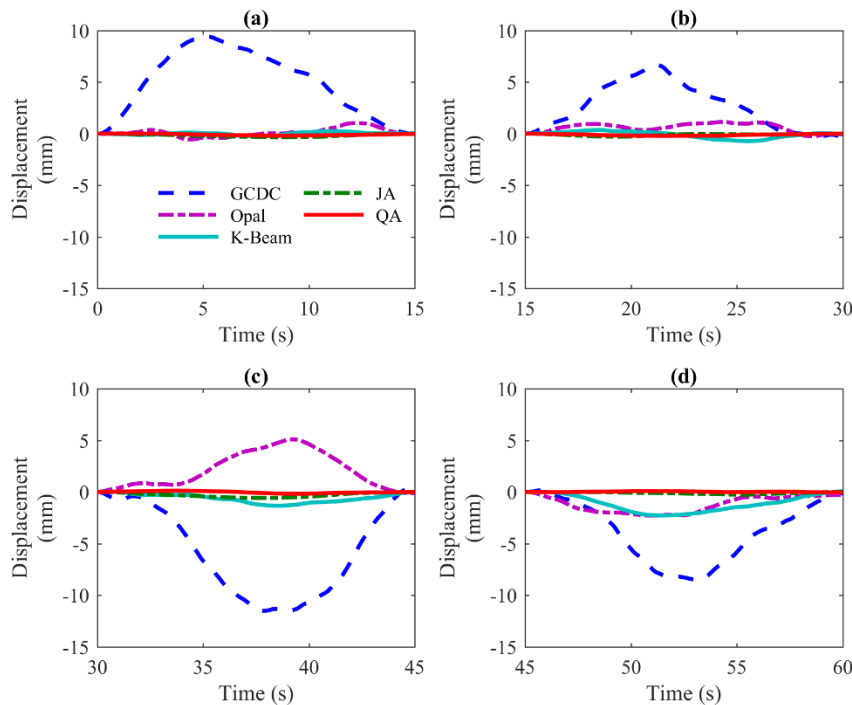
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321 Fig. 5, Acceleration signals recorded from five different accelerometers placed on the rigid
 322 laboratory floor (a) GCDC accelerometer, (b) Opal accelerometer, (c) K-Beam accelerometer, (d) JA
 323 accelerometer, (e) QA accelerometer, (f) signals from parts (a-e) of the figure after smoothing with a
 324 moving average filter.

325 In Fig. 5(a-e), eight separate 15-second partitions/windows (Win 1 –Win 8) are included on the figure
 326 to indicate that the signals are not integrated as whole 120-second signals but as a sequence of
 327 short independent signals, to illustrate the range of errors that can be expected when integrating
 328 field acceleration signals to displacement. 15 seconds in duration is chosen as it is a realistic duration
 329 for a typical highway bridge including ambient signal before the trucks arrival, plus the forced
 330 portion of the signal (when the truck is on the bridge) and the short period of ambient vibration
 331 immediately after the truck leaves (see Fig. 2(a)).

332 Fig. 6 shows the result of double integrating the signals in windows 1-4 of Fig 5. In particular Fig. 6(a)
 333 shows the result of double integrating the first 15 seconds of acceleration recorded by each of the
 334 five sensors, i.e. the ‘Win1’ data from Figs 5(a)-(e). In Fig. 6(a), the dashed (GCDC) plot shows the
 335 result of double integrating window 1 (Win1) of the ‘GCDC’ signal shown in Fig. 5(a). Similarly the
 336 other plots in Fig 6(a) are the result of double integrating the window 1 data from parts (b), (c), (d)
 337 and (e) of Fig. 5. All the plots in Fig. 6(a) are calculated assuming zero initial displacement and
 338 velocity. Signals are de-trended using the MATLAB linear de-trend function then double integrated
 339 using the MATLAB ‘cumtrapz’ function. No other filtering or correction procedures are applied.

340 In Fig. 6(a) GCDC data indicate a maximum displacement of 10 mm at approximately 5 seconds. Also
 341 in Fig. 6(a) the window 1 acceleration data from the other sensors produce a displacements at least
 342 an order of magnitude smaller. A similar pattern is observed for window 2 acceleration data in Fig.
 343 6(b), i.e. all sensors except the GCDC predict displacements close to zero (at the displacement limits
 344 adopted in the plot). However, window 3 acceleration data (Fig. 6(c)) indicate a maximum
 345 displacement of 6mm at approximately 38 seconds for the Opal.

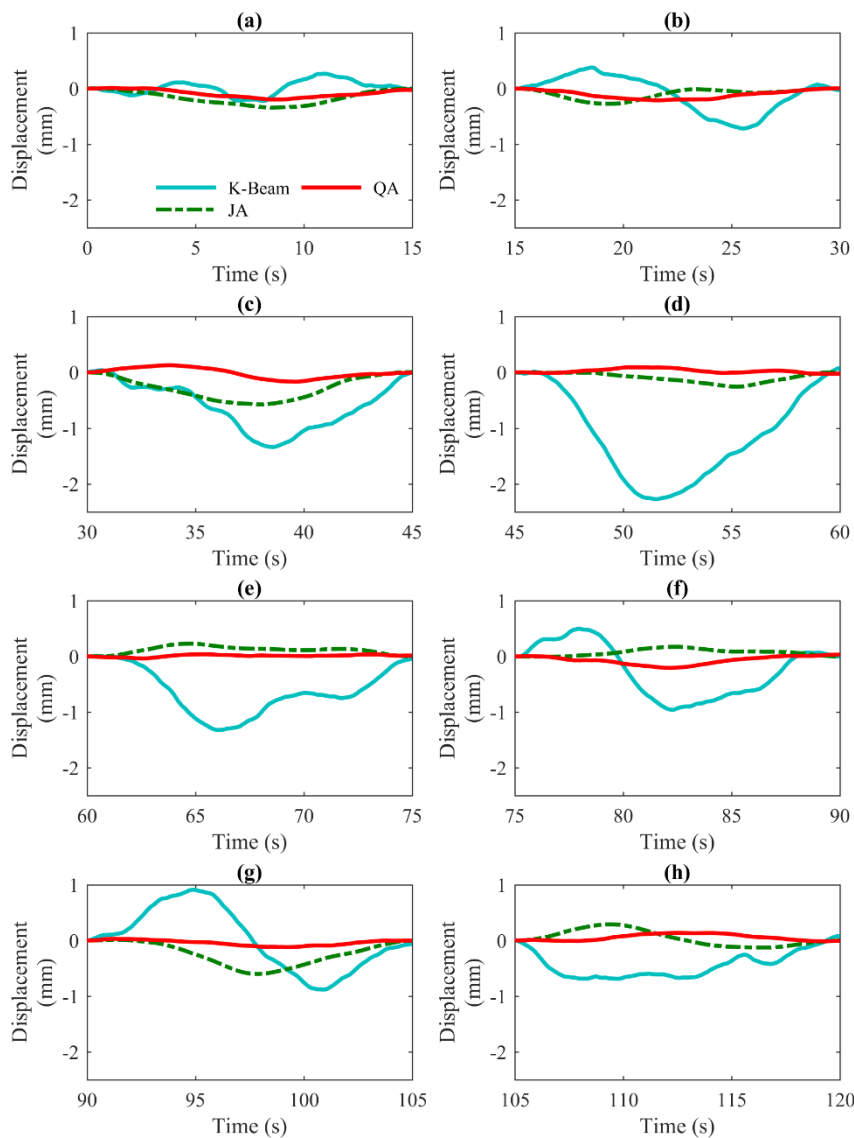


346

347 Fig. 6, Displacements calculated following the double integration of the acceleration signals shown
 348 in Fig. 5; (a) Window 1 data, (b) Window 2 data, (c) Window 3 data, (d) Window 4 data.

349

350 Fig. 6 tells us that GCDC and Opal accelerometers should not be used for this application but is not
351 informative about errors in the displacement calculated using the other three accelerometers, i.e. K-
352 Beam, JA and QA. Therefore a zoomed in view of the displacement calculated from these sensors is
353 shown in Fig. 7 showing the errors in the displacement calculated from the K-Beam accelerometer to
354 be larger than those from either the JA or QA accelerometers. JA and QA performance are
355 comparable, with the QA appearing to perform slightly better, hence the QA was selected for the
356 laboratory and field trials.

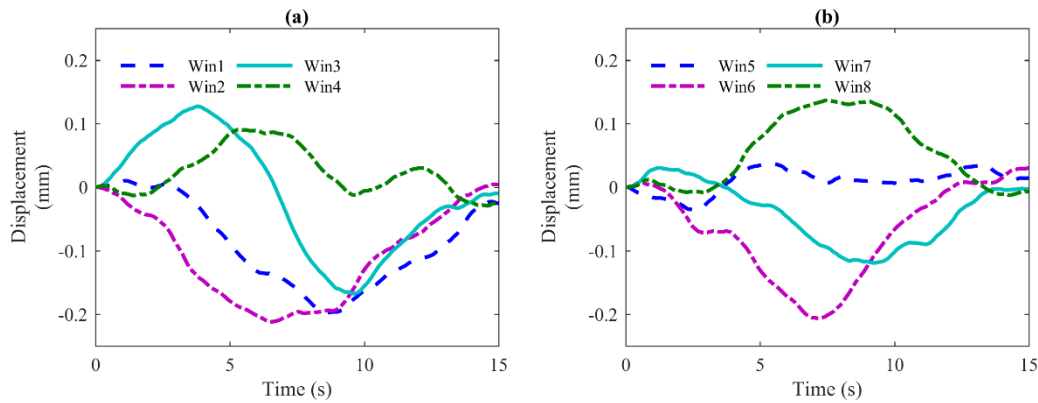


357

358 Fig. 7, Displacements calculated following the double integration of the acceleration signals shown in
359 Fig 5; (a) Window 1 data, (b) Window 2 data, (c) Window 3 data, (d) Window 4 data, (e) Window 5
360 data, (f) Window 6 data, (g) Window 7 data, (h) Window 8 data

361

362 Fig. 8 shows only the QA displacements, with movements in the region of $\pm 0.2\text{mm}$ observed. For the
363 field application the bridge quasi-static deflection due to truck crossing is expected to be around 3
364 mm (based on hand calculations using bridge properties and approximate truck weight) so errors in
365 the region of $\pm 0.2\text{mm}$ are acceptable.



366

367 Fig. 8, Magnified views of QA displacements shown in Fig. 7, (a) QA displacements calculated for
368 windows 1-4, (b) QA displacements calculated for windows 5-8.

369 4.0 Laboratory trial

370 As the goal of this paper is to examine the feasibility and accuracy of calculating bridge displacement
371 by analysing the bridge acceleration response to the passage of a moving load a directly measured
372 displacement record is required, in this case provided by a conventional LVDT and an optics-based
373 motion capture system (MCS). Before deploying in a field test the accuracy of the test procedure was
374 verified in a laboratory trial. Sections 4.1 and 4.2 below respectively describe the test setup used and
375 the results obtained and the field test is described in section 5.

376 4.1 Test setup

377 For maximum realism an analog bridge (i.e. the laboratory test structure) was set up that would
378 have both natural frequency and displacement magnitude similar to what was expected on the real
379 bridge, estimated as 4.9 Hz and 3-4mm, respectively based on simple calculations and information
380 from available design drawings. Once set up the analog bridge had a natural frequency of 4.7 Hz and
381 the displacement to the static load was 3.2 mm.

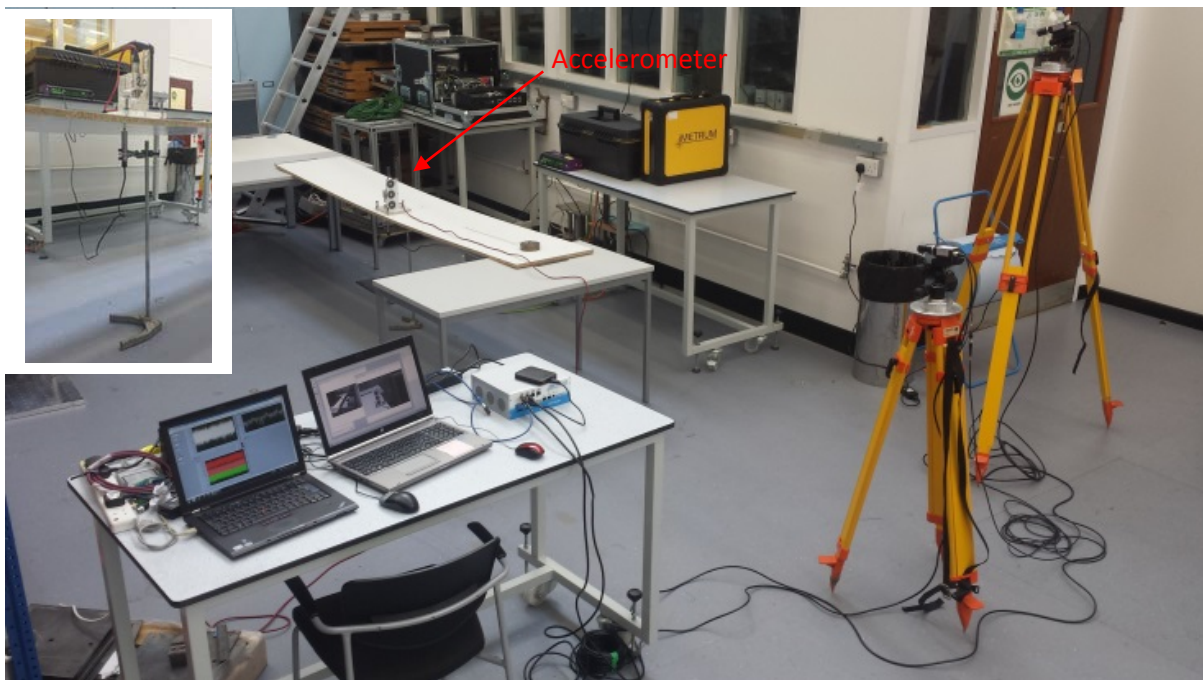
382 The analog bridge (Fig. 9) comprised a sheet of laminated chipboard spanning between two supports
383 representing the bridge 'deck', and the moving load was a small metal cylindrical weight pulled
384 smoothly along the bridge using a string. In Fig. 9 the cylindrical weight is on the right end of the
385 bridge, a QA accelerometer with an optical target of concentric circles is placed at mid-span on the
386 analog bridge, and the insert (top left) shows an LVDT mounted on a retort stand touching the
387 bridge soffit.

388 The camera used in the MCS is mounted on the smaller surveying tripod in Fig. 9 is zoomed in
389 on the optical target. The camera on the taller tripod having a wide angle lens was used not for
390 tracking but to record video of the experiment. However, the cameras are synchronised so that

391 displacement response from the MCS could be interpreted using the video footage. The camera
392 system used is a commercial system manufactured by Imetrum [10].

393 The reason for using two (direct) displacement measurement techniques (i.e. the LVDT and the MCS)
394 was to check the capability of the MCS, which is a logistically superior system for site testing, as in
395 many situations it is impractical to mount an LVDT under a bridge soffit. Once the three
396 measurement systems were set up the test was carried out by pulling the cylindrical weight across
397 the bridge. The results of the test are presented in the next section.

398 As well as experiencing acceleration due to the vertical translation of the deck as the load moves
399 across, the accelerometer will also rotate as the deck deforms. Using the same simulation presented
400 in Fig. 2 with deflection (3 mm), in line with what is expected to be encountered in the field test, the
401 maximum rotation is 0.000339 degrees. The resulting cosine error is negligible ($\cos(0.000339^\circ) \approx 1$),
402 hence can be ignored.



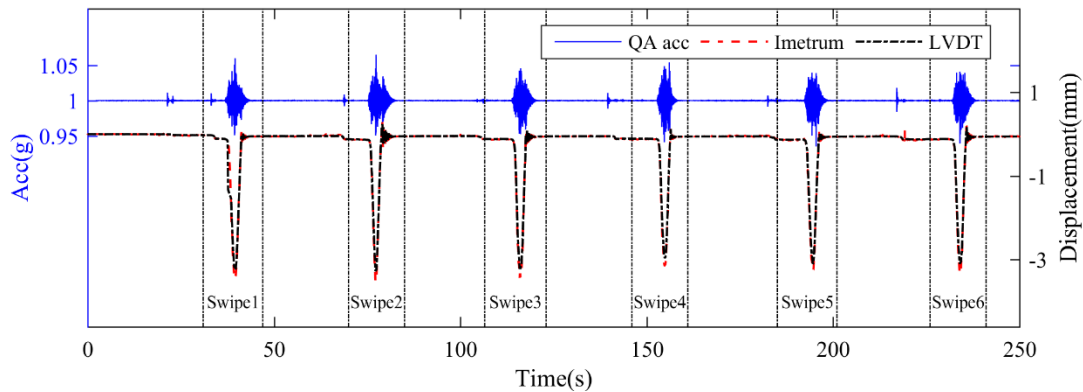
403

404 Fig. 9, Experimental setup used in the laboratory trial including 3 measurement systems: (i) Imetrum
405 camera system, (ii) QA accelerometer and (iii) LVDT.

406 4.2 Results

407 Fig. 10 shows the acceleration measured by the QA accelerometer and the displacement measured
408 by both the Imetrum camera system and the LVDT. In total six separate passes of the moving weight
409 were carried out and this took almost 250 seconds. In the figure acceleration y-axis is on the left
410 hand side and displacement is the y-axis on the right hand side. The raw acceleration (topmost
411 curve) is measured in units of gravity (g) with the 1 g average because the sensor is sitting upright.
412 Six separate pulses of acceleration corresponding to the six separate passes of the moving mass can
413 be seen. The peak displacement is approximately 3 mm and there is very good agreement between

414 the two displacement measuring systems, Imetrum and LVDT.



415

416 Fig. 10, Raw data from the three sensing systems for the 6 passes of the load, acceleration data (QA)
417 is plotted with respect to the y-axis on the left and corresponding data from the two displacement
418 measuring systems (Imetrum & LVDT) are plotted with respect to the y-axis on the right.

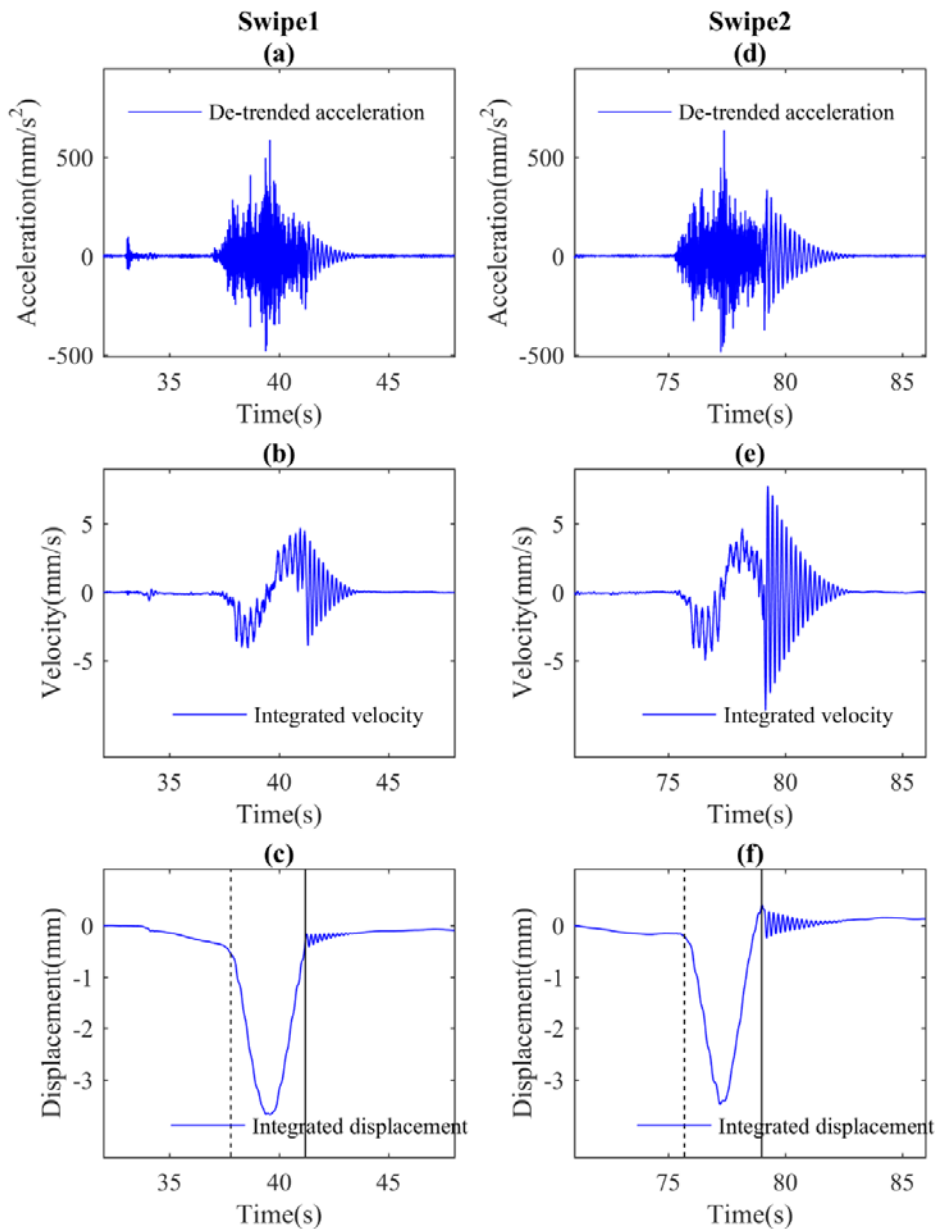
419 To test the reliability of calculating displacement from acceleration the acceleration data are cut into
420 6 separate 'swipes' (1-6) each approximately 15 seconds long, as indicated in Fig. 10 and centred on
421 the approximate centre of the respective acceleration pulse. (In the context of this paper 'swipe'
422 implies a discreet region of interest relating to the passage of the load which is cut from a larger
423 signal).

424 Once the 'swipe' acceleration data is extracted it is de-trended and scaled to units of mm/s^2 , with
425 examples for swipe 1 and swipe 2 shown in Figs. 11(a) and (d) respectively. Similar to the previous
426 examples, integration takes bridge initial displacement and velocity as zero. The mid-span velocity
427 for swipe 1 is obtained by applying the MATLAB 'cumtrapz' function to the acceleration signal in Fig.
428 11(a) and the result is shown in Fig. 11(b). The integration procedure is repeated on the signal
429 shown in Fig. 11(b) with the result shown in Fig. 11(c). Figs 11(d), (e) and (f) show the recorded
430 acceleration, calculated velocity and calculated displacement, respectively, for swipe 2.

431 The method assumes that displacement is zero before the arrival of the truck ('pre load', see Fig. 2)
432 and returns to zero once the truck leaves the bridge ('post-load', see Fig. 2). This may not be true for
433 a real bridge since e.g. locking of the bearings would result in a residual displacement, but it is a
434 reasonable assumption. The video camera recording the experiment allows the reliability of the
435 integration to be checked as follows. From the video camera it is known that the load arrived on the
436 analog bridge at 38 seconds and left at approximately 41 seconds (the entry and exit times are
437 indicated as vertical dashed and solid lines respectively in Fig. 11(c)), hence the calculated
438 displacement before arrival (dashed vertical line) and after departure (solid vertical line) should be
439 approximately zero. However, Fig. 11(c) shows calculated displacement as less than zero from about
440 35 seconds (reaching approximately -0.25 mm just before arrival), not returning to zero as the truck
441 leaves (approx. -0.1 mm) and gradually increasing to become positive (approx. 0.1 mm).

442 The fact that the pre-load and post-load parts of the calculated displacement signal have small
443 errors means that the displacement calculated for the loaded portion of the signal is also likely to
444 have some small errors. The video of swipe 2 shows the load going onto the analog bridge at
445 approximately 76 seconds and exiting at 78 seconds, as indicated on Fig 11(f) using dashed and solid

446 lines, respectively. Similar to part (c) of the figure, in Fig. 11(e) the calculated displacement before 76
 447 seconds, and after 78 seconds is close to zero ($\pm 0.1\text{mm}$), i.e. the calculated displacement for the
 448 unloaded parts of the signal prove relatively accurate so it is likely that the peak displacement in the
 449 loaded portion of the signal is also reasonably accurate. Examination of swipes 3-6 show pre-load
 450 and post-load displacements to be mostly in the range $\pm 0.15\text{mm}$ so over all six swipes the errors are
 451 less than 0.3mm .



452

453 Fig. 11, Calculating displacement from acceleration for swipe 1 (left column) and swipe 2 (right
 454 column) of laboratory test, (a) Swipe 1 acceleration, (b) swipe 1 velocity calculated following
 455 integration, (c) swipe 1 displacement calculated following integration, (d) Swipe 2 acceleration, (e)
 456 swipe 2 velocity calculated following integration, (f) swipe 2 displacement calculated following
 457 integration.

458 Fig. 12 (a) and (b) reproduce the calculated displacement from Figs. 11(c) and (f) respectively but
459 also includes the displacement measured directly using the LVDT and Imetrum in order to check the
460 suggested errors. Fig. 12(c)-(f) shows the same thing for swipes 3-6 respectively. It can be seen in Fig.
461 12 that the calculated displacements for the loaded portion of the signals are very close to the
462 directly measured displacements, which is in line with expectations based on errors observed in the
463 pre-load and post-load portions of the signal. However, some errors are evident, for example in
464 swipe 1 (Fig. 12(c)) the calculated displacement overestimates the peak displacement by about 0.3
465 mm. This level of error is consistent with the magnitude of the error that was pointed out in the pre-
466 loaded portion of swipe 1 (see Fig. 11(c)). Similarly in swipe 4 the calculated peak displacement is
467 approximately 0.2 mm larger than the directly measured value, but this level of error in the peak
468 displacement is consistent with the error at the start of the post-load portion of swipe 4. The pattern
469 for swipes 2, 3, 5 and 6 (Figs. 12(b), (c), (e) and (f), respectively) is similar, i.e. the errors in the
470 calculated displacement (from the correct zero value) in the pre-load and post-load parts of the
471 signal are representative of errors likely to be present in the loaded portion of the signal.

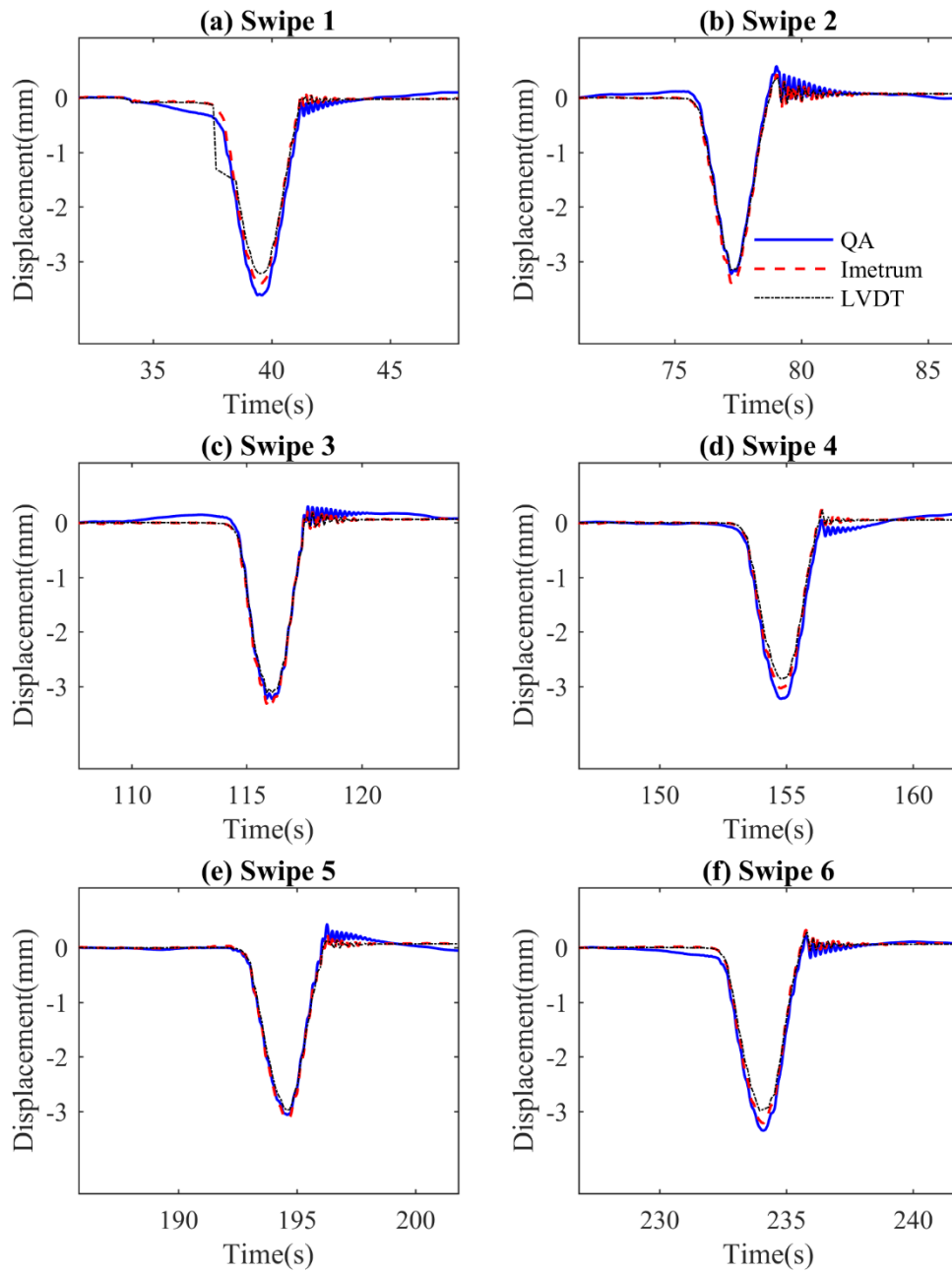
472 In effect it appears that the pre-load and post-load parts of the calculated displacement signal can
473 be used as a quality indicator for the accuracy of the loaded part of the calculated displacement
474 signal. This is an important result as it provides an estimation of accuracy in the absence of directly
475 measured displacements.

476 Comparing displacements calculated through the double integration of acceleration records to
477 displacements measured using some direct means has been reported by other authors. For example
478 Psimoulis et al [32] have compared the displacement calculated following the double-integration of
479 earthquake acceleration records with corresponding ground movements derived from GPS records.
480 In their study they observed that the consistency of the calculated displacement depended on the
481 direction of motion. If the accelerometer used in the study had been a tri-axial accelerometer it
482 would have been interesting to calculate the displacement in the lateral and longitudinal directions
483 as it is possible that calculated movements in these directions could be used as quality indicators. That
484 is to say movements in these directions should be very small relative to the vertical movement.
485

486 In the same way that in the analog bridge test many swipes were used to investigate the error it is
487 sensible to do a number of truck passes in a field test. During these experiments it was found that
488 the magnitude of the errors in the pre-load and post-load parts of the calculated displacement signal
489 can be affected by the start time of the swipe. The amplitude of the static peak tends not to be
490 effected by the swipe start time however, to minimise the errors in the pre load and post load
491 sections of the calculated signal it is prudent to try a few closely spaced start times.

492 Although the errors observed in Fig 12 could probably be corrected by using some of the methods
493 discussed in Section 1 the aim here is to avoid the problems of choosing the correction parameters,
494 and instead develop a robust procedure with inbuilt quality control check. The next section describes
495 field application of the proposed procedure.

496



497

498 Fig. 12, Displacement observed for the three measurement systems for swipes 1-6 (a) swipe 1, (b)
 499 swipe 2, (c) swipe 3, (d) swipe 4, (e) swipe 5, (f) swipe 6.

500

501

502

503 **5.0 Field Trial**

504 Following the laboratory trials, the proposed approach was applied on a real bridge.

505 5.1 Test Bridge

506 The three span concrete road bridge shown Fig. 13(a) used for the field application has beam and
507 slab deck with three separate spans simply supported on piers. The cross section in Fig. 13(b) shows
508 19 m span steel I-sections encased in concrete, at 1.54 m centres.

509 To install the LVDT a bridge with a relatively low soffit and safe access was required. Fortunately, to
510 facilitate river works, the level of the river had been reduced at the time of the measurement,
511 exposing a sandbank below the middle of the span nearest to the footpath that could be used as a
512 working platform. Details of the expected natural frequency and deflection are given in section 4.1.

513 5.2 Test set up

514 Fig. 13(c) shows the bridge in plan indicating footpaths on the east and west side of the bridge and
515 four northbound traffic lanes in between. The road layout in the vicinity of the bridge is such that to
516 get multiple passes of the truck in a relatively short time the truck needed to turn right immediately
517 on exiting the bridge. In order to do this safely it needed to travel in lane 4, so it was decided to
518 monitor the beam that was approximately in the middle of lane 4, which happened to be the third
519 beam from the east side of the bridge. The beam and the monitoring location are indicated in
520 Fig.13(c), while the step ladder visible under the northern span in Fig. 13(a) shows the approximate
521 location where deflection was monitored. The sensing equipment installed was the same as was
522 used in the laboratory test, i.e. an accelerometer, an LVDT and the Imetrum camera system. Further
523 details on installation are given below.

524 Fig. 13(d) shows a view of the deck soffit with the instrumentation attached at the mid-span and Fig.
525 13(e) zooms in on the instrumentation. A steel angle is clamped to the corner of the beam allowing
526 the accelerometer to be attached using a magnet. As in the laboratory test an Imetrum optical target
527 was stuck to the side of the accelerometer. The web of the concrete-encased beam could have made
528 an ideal natural target but the view was blocked by the soffit panels.

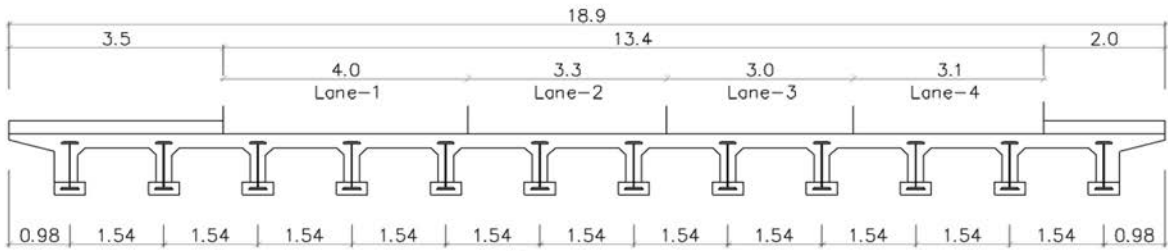
529 The final part of the sensing system to be installed was the LVDT. A small dimple was bored in the
530 steel angle to provide a seating for the tip of the LVDT, which was mounted on the top of a
531 telescopic aluminium pole visible to the left of the ladder in Fig. 13(d). Provided the telescopic pole is
532 installed approximately plumb, the spring loading on the tip of the LVDT should suffice to keep the
533 pole/LVDT stable during a test. However, winds speeds on the day of the test exceeded 30 mph
534 resulting in some movement of the pole and leading to some small inaccuracies in the LVDT data.
535 These are indicated in the next section but they did not prove significant.

536 The wind also impacted location of the camera which was positioned to avoid wind-buffeting and
537 consequent measurement errors. The wind was from the west so camera 1 which was tracking the
538 target at the mid-span of beam 3 was positioned as close to the lee side of the north abutment as
539 line of sight would allow. Camera 2, for recording bridge traffic during the measurements was
540 positioned further south for a wide field of view to be able to see the whole deck and could sustain

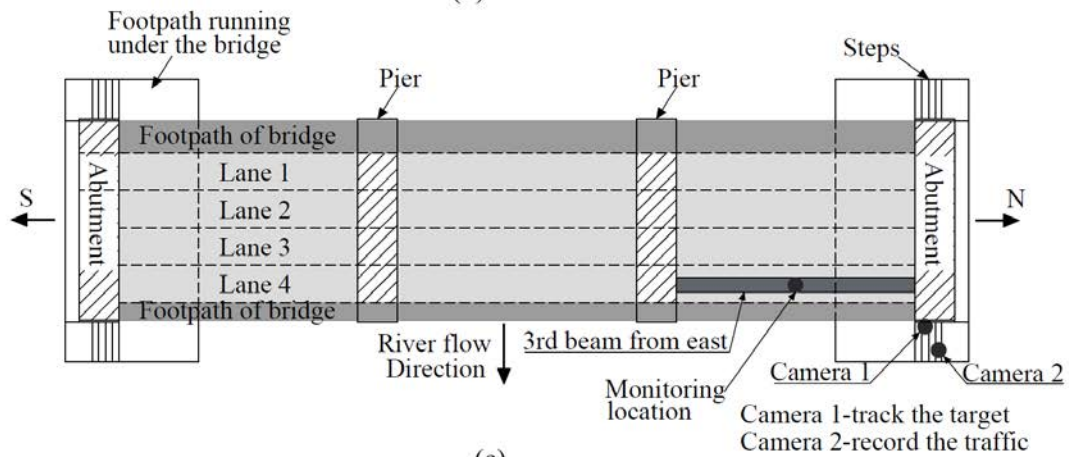
541 buffeting without affecting the results as it was only used for monitoring traffic. The position of
 542 cameras 1 and 2 is indicated in the bottom right of Fig.13(c).



(a)



(b)



(c)



(d)



(e)

543
 544 Fig. 13, Bridge used in field test, (a)side view of the bridge from the East, (b) Typical vertical cross
 545 section through the deck (c) Schematic of test setup, (d) view of deck soffit with instrumentation
 546 installed, (e) Zoomed in view of instrumentation attached to soffit of the beam, accelerometer
 547 installed but LVDT not yet in place

548

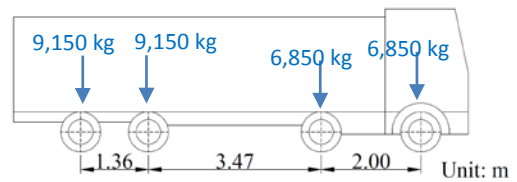
549

550 5.3 Vehicle used

551 The truck used in the test was the four axle Scania P410 shown in Fig. 14(a); part (b) of the figure
552 shows the axle spacing of the truck. On the morning of the test the truck was loaded with stone
553 aggregate and its gross weight was 32 tonnes. The approximate weight on each axle is indicated in
554 Fig. 14(b) and it is assumed that the load on a given axle is equally distributed to between the wheels
555 on the axle.



(a)



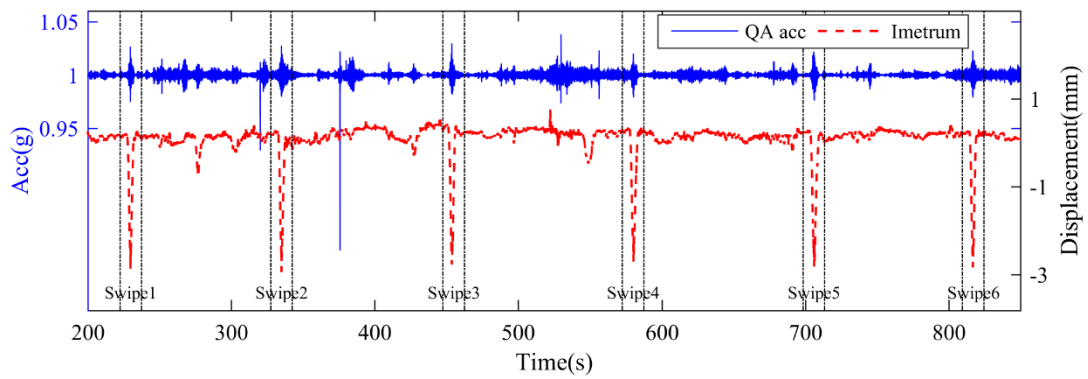
(b)

556 Fig. 14, Truck used in the load test, (a) photo of the truck, (b) axle spacing.

557 5.4 Results

558 Fig. 15 shows the Imetrum displacement data and the corresponding QA acceleration data for the
559 bridge test with acceleration y-axis on the left and the displacement y-axis on the right. Within the
560 16 minutes (960 seconds) test duration the truck crossed the bridge six times as indicated in the six
561 corresponding clear peaks in Fig. 15.

562 The load corresponding to each peak can be checked using camera 2 video, for example for the first
563 deflection peak in Fig. 15 at approximately 230 seconds, Fig. 16 shows camera 2 view at 229 seconds
564 just before the truck reaches mid-span (if the image from 230 seconds is used it is more difficult to
565 identify the truck). The corresponding acceleration pulses do not stand out in Fig. 15, in fact
566 acceleration pulses occur when any kind of vehicle enters the bridge passing over the irregular
567 surface near the support. To identify the acceleration pulses corresponding to truck loading and
568 integrate the correct part of the signal it is necessary to identify the crossing time in the video. With
569 the approximate time of the truck crossing event known, zooming on the acceleration signals allows
570 the corresponding acceleration segment to be identified, as shown for swipe 1 and swipe 2 in Figs.
571 17(a) and (d) respectively.



572

573 Fig. 15, Imetrum displacement data and QA acceleration data for the bridge test.

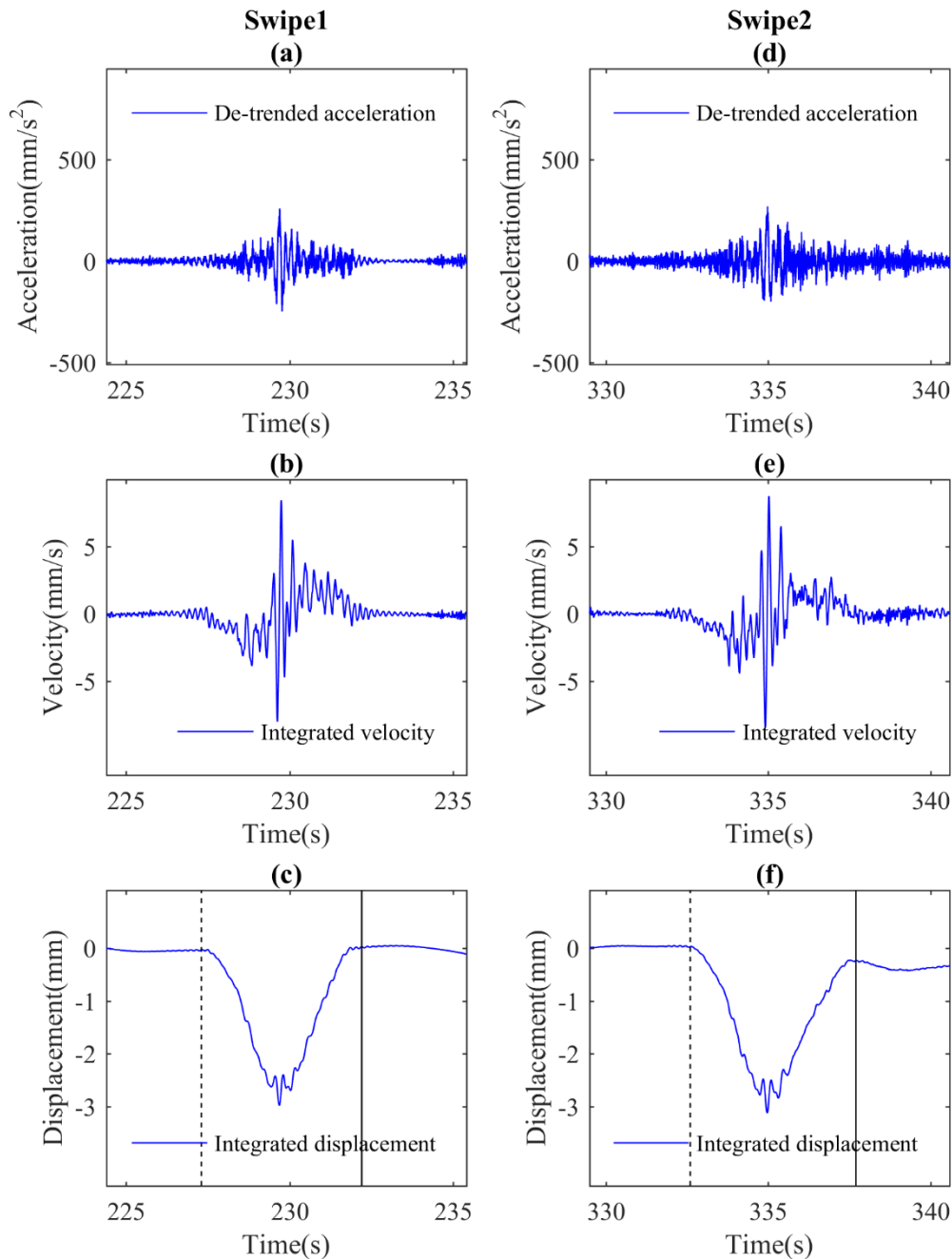
574



575

576 Fig. 16, Loading on bridge at 229 seconds, i.e. truck crossing over bridge during swipe 1.

577 Fig. 17 shows the integration procedure applied to swipe 1 and swipe 2 of the field test and is
 578 analogous to Fig. 11. Fig. 17(a-c) for swipe 1, show the de-trended acceleration signal, the calculated
 579 velocity, and the calculated displacement respectively. Camera 2 shows the truck entering the bridge
 580 at 228 seconds and leaving at 232 seconds, which is indicated by dashed and solid lines, respectively,
 581 in the figure. Fig. 17(c) shows the calculated displacement before the truck arrives and after it leaves
 582 to be very close to zero, i.e. the pre-load and post-load parts of the signal appear to be correct,
 583 which (based on results observed in the laboratory) indicates that the peak displacement of 2.8 mm
 584 for the forced part of the signal is likely to be reliable. For swipe 2 with truck entering the bridge at
 585 333 seconds and leaving at approximately 337 seconds pre-load displacement is correct (i.e. 0 mm),
 586 while post-load part of the signal reads approximately -0.35 mm, which quantifies the likely error in
 587 the forced part of the calculated displacement signal.



588

589 Fig 17, Calculating displacement from acceleration for swipe 1 (left column) and swipe 2 (right
 590 column) of bridge test; (a) swipe 1 acceleration, (b) swipe 1 velocity calculated following integration
 591 of acceleration signal, (c) swipe 1 displacement calculated from integration of velocity signal, (d)
 592 swipe 2 acceleration, (e) swipe 2 velocity calculated following integration of acceleration signal, (f)
 593 swipe 2 displacement calculated following integration of velocity signal.

594

595 Fig. 18 shows the calculated (QA) and measured (Imetrum & LVDT) displacement for all six swipes
 596 and broadly speaking there is good agreement between the three signals. As with the integration

597 process for the analog bridge, initial displacement and velocity at the start of the swipe are assumed
598 to be zero, an assumption validated in Fig. 18. This would not hold true in the case of another heavy
599 vehicle leaving the bridge, but this would be spotted in the video.

600 In Fig. 18(b) the LVDT data shows an anomaly at approximately 339 seconds resulting from the
601 difficulty experienced in keeping the LVDT setup stable during the test. Occasionally the strong wind
602 experienced during the test would move the tip of the LVDT laterally out of the dimple recess before
603 having to be reset manually. This is the likely cause for the displacement anomaly at 339 seconds
604 and most likely for the anomaly at 852 seconds in Fig. 18(d).

605 The observation from the field test, supported by the analog bridge test is that 'close to zero' pre-
606 load and post-load displacement indicate a credible displacement time history. Since the quality
607 assurance requires short periods before and after the truck passes with no other heavy vehicles
608 (trucks) present means that the proposed procedure would not be suitable during periods of busy
609 traffic. It is also limited to relatively short bridges because of more frequent truck passing and the
610 increasing unreliability of double integration. However in the 'small hours' around 4AM it is usual to
611 find periods when even the busiest bridge may be empty long enough for a measurement to be
612 taken.

613

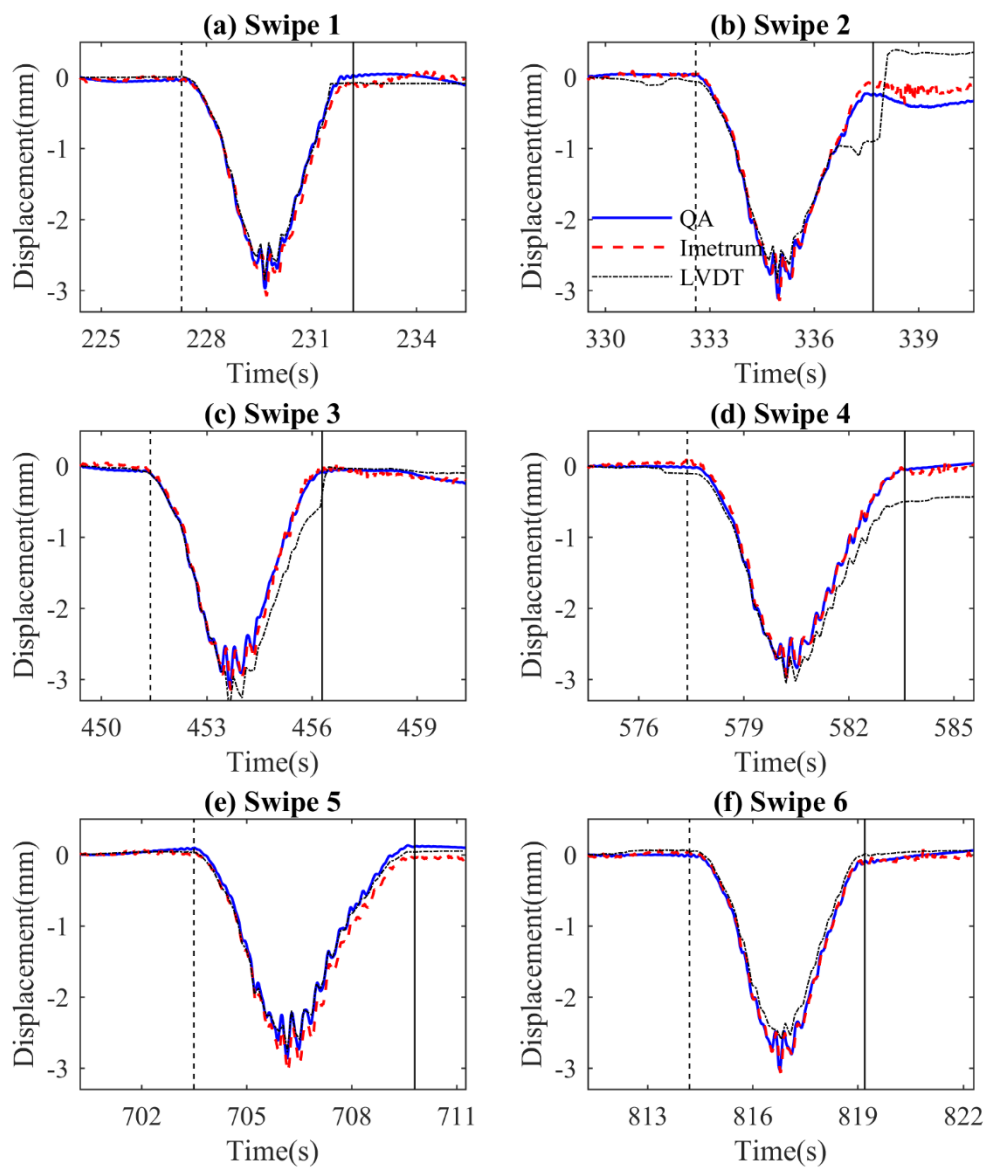
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620 Fig 18, Displacement observed for the three measurement systems for swipes 1-6 (a) swipe 1, (b)
 621 swipe 2 (c) swipe 3, (d) swipe 4, (e) swipe 5, (f) swipe 6.

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627 **6.0 Conclusions**

628 This paper presents a method for carrying out a low cost minimally invasive bridge load test by
629 calculating bridge displacement to a moving load from the bridge acceleration response. The
630 performance of the method is examined in both laboratory and field conditions and accurate results
631 are observed in both tests. The paper presents two novel contributions to existing work in this area.

632 Firstly the paper demonstrates the importance of low frequency accelerometer noise. Selection of
633 accelerometer was done by comparing performance of a range of sensors. A simple numerical model
634 demonstrates how the quasi-static component of bridge displacement response to a moving load
635 appears in the bridge acceleration signal in time and frequency domain.

636 Second, the proposed method provides an in-built quality control check on the calculated signal.
637 Methods presented in the literature to calculate bridge displacement from acceleration have
638 demonstrated their accuracy in one off experiments by comparing the 'calculated' displacement to
639 the displacement measured directly using e.g. LVDT. However without such a reference it has been
640 impossible to estimate accuracy in the calculated displacement. The approach proposed here uses
641 video footage synchronised with acceleration signals to estimate the magnitude of the likely errors
642 in the calculated displacement signal.

643 The paper presents an extensive experimental study in both laboratory and field conditions with
644 displacement measured directly by LVDT and an optical tracking system. The two direct
645 measurement systems validated each other and provided error estimates for the calculated
646 displacements. The laboratory trial aiming to reproduce the field trial in terms of truck-passing
647 duration and deflection with total control of loading was very effective and provided the means to
648 judge the reliability of the field test data.

649 While the errors observed in the calculated displacement in this paper are pleasingly small, it is
650 important to understand that the results relate to a specific set of circumstances. Namely; (i) short
651 duration time intervals, (ii) small amplitude bridge accelerations and (iii) small amplitude
652 displacements. The significance of each of these factors in obtaining an accurate 'calculated
653 displacement' has been well demonstrated/explained by others [21], [22]. Therefore an in depth
654 discussion on this is not repeated here, except to point out that if that approach used in this paper
655 was applied to circumstances where one or more of (i), (ii) or (iii) were not true , (e.g. suspension
656 bridge with a long duration acceleration signal, or an earthquake event with high accelerations) large
657 errors could result.

658 Traditionally a bridge load test is a complicated exercise requiring specialist equipment and
659 operators along with road closure. This study shows that a simple measurement using a high quality
660 accelerometer and a video camera, performed in the middle of the night when prevailing traffic
661 volumes are relatively low could provide a reliable deflection estimate for a known load. However, it
662 is important to note that the authors are not claiming that the approach presented in the paper is
663 necessarily the best or most practical approach for logistically feasible load testing. The improving
664 accuracy of GPS to measure vertical displacement and the emergence of camera based displacement
665 monitoring means that there a number of options to measure bridge displacement during a load
666 test. Ultimately the displacement tracking method used during a load test will likely depend on the
667 equipment available, the logistics of the site and the expertise/experience of the test crew.

668 Therefore the aim of this paper is not to promote one method over another, instead the intention is
669 to describe the author's experiences of integrating bridge acceleration to calculate displacement and
670 to report the potential benefits and limitations of the approach.

671 **Acknowledgements**

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