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# An Experimental Evaluation of Switched Combining Based Macro-Diversity for Wearable Communications Operating in an Outdoor Environment 

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#### Abstract

This paper investigates the potential improvement in signal reliability for outdoor wearable communications channels operating at 868 MHz using switched combining based macrodiversity. In this study, a number of different macro-diversity configurations consisting of two and four base stations were considered to help mitigate the impact of body shadowing upon a wearable node which was located on the central chest region of an adult male. During the field measurements, five different walking movements were performed and then analyzed to investigate the efficacy of using macro-diversity. It was found that all of the considered switched combining schemes including switch-and-stay combining (SSC), switch-and-examine combining (SEC) and SEC with post-examining selection (SECps) provided a worthwhile signal improvement when an appropriate switching threshold was adopted. The maximum diversity gain obtained in this study was found to be 19.5 dB when using four-base station SECps. The diversity gain, the number of path examinations and the number of path switches between base stations for the switched combiner output varied according to the determined switching threshold, highlighting the importance of the selection of an appropriate threshold level. Furthermore, the performance/complexity trade off is demonstrated. Finally, the fading behavior at the output of the switched diversity combiners was then characterized using the diversity specific equations developed under the assumption of independent and non-identically distributed Nakagami- $m$ fading channels. Over all of the measurement scenarios considered in this study, the theoretical models provided an adequate fit to the fading observed at the output of the virtual switched combiner.


Index Terms—diversity gain, macro-diversity, Nakagami-m fading, shadowing, switched combining, wearable communications.

## I. INTRODUCTION

COmbining the signal obtained from spatially separated antennas is one well-known method of mitigating the detrimental effects of fading and improving the signal reliability and the performance of wireless communication systems [1], [2]. Since spatial diversity schemes generally require no additional transmit power or bandwidth, they are more commonly applied compared to other diversity techniques such as time, frequency and polarization diversity [3]. Spatial diversity schemes are often implemented using two main configurations, namely micro- and macro-diversity which are differentiated

[^0]according to the allocation of the antennas. In micro-diversity based systems, the antennas are typically positioned within a single base station and their spacing is in the order of, or shorter than the carrier wavelength. The expectation here is that the antennas will experience different small-scale fading (multipath). On the other hand, in macro-diversity based systems, the antennas are located in a number of different spatially separated base stations and their spacing is much longer than the carrier wavelength. This causes the antennas to experience different large-scale fading (shadowing). Hence, micro- and macro-diversity are generally employed to combat the effects of multipath fading and shadowing, respectively [4].

Switched combining and gain combining are the most prevalent combining schemes utilized in conjunction with microand macro-diversity based systems [5]. In switched combining schemes, the receiver selects one of the available diversity paths according to a corresponding criterion. This category of combiners contains both the pure selection combining (PSC) and threshold selection combining (TSC) techniques. On the other hand, in gain combining schemes, the output of combiner is formed as a linear combination of the signals received by all of the diversity paths. This class of combiner includes the equal gain combining (EGC) and maximum ratio combining (MRC) techniques. In general, a better performance can be achieved by gain combining schemes compared to switched combining schemes. Furthermore, it is widely recognized that MRC is generally considered as the optimal combining scheme in terms of the performance. Nevertheless, switched combining has remained popular due to its relatively low complexity and ease of implementation. In a PSC system, the combiner requires continuous and simultaneous knowledge of all of the possible signal branches, which can be both time- and powerconsuming. Contrastingly, in a TSC system, the receiver stays with the current branch as long as its signal-to-noise ratio (SNR) is above the predetermined switching threshold. In other words, the receiver switches from the current branch to another only when its SNR falls below the predetermined switching threshold [6]. Therefore, this approach prevents the unnecessary monitoring of the SNR of all branches but more importantly avoids needless switching between branches especially when the SNR of the currently selected branch is at level which is sufficient to provide the desired information recovering capacity. The TSC grouping of combiners consists
mainly of the switch-and-stay combining (SSC), switch-andexamine combining (SEC) and SEC with post-examining selection (SECps) schemes.

Over the last few decades, a number of studies investigating spatial diversity techniques have been performed in the context of wearable or equivalently body-centric communications [714]. However, the majority of these have considered only PSC, EGC and MRC schemes [7-12]. As mentioned above, these combining schemes can be resource consuming compared to simpler TSC schemes and therefore may be impractical for implementation in wearable systems which favor low complexity, low cost and ultra-low power architectures [15], [16]. To this end, the authors of [13], [14] have studied cooperative diversity using the SEC scheme for on-body communications channels. In [13], it was shown that a cooperative switched combining scheme provided an improvement in outage probability (OP), a reduction in power consumption and a low switching rate. In [14], the author demonstrated that the outage performance of the cooperative switched combining scheme was not considerably degraded, but it had a much lower switching rate between branches when compared to the traditional cooperative PSC scheme.

Moreover, the majority of the studies on spatial diversity techniques for wearable communications which have been presented in the literature have focused on micro-diversity systems positioned either on the human body or at a base station with the aim of mitigating the impact of multipath fading [7-9]. However, the use of micro-diversity alone may not be sufficient to overcome the arguably more critical signal degradations caused by random shadowing events induced by the human body and obstacles in the local surroundings. To overcome human body shadowing in wearable communications channels, spatial diversity using antennas distributed across the human body has been proposed [17], [18]. For example, in [17], front and back positioned antennas used together with a PSC scheme provided mitigation of human body shadowing and an overall improvement in signal reliability in outdoor body-to-body communications channels at 2.45 GHz . In [18], six receiver antennas were distributed across the front and back torso of the human body to help overcome the detrimental effects of human body shadowing in off-body communications within an indoor environment at 868 MHz . The benefit of having more than two signal branches was demonstrated by comparing the diversity gains between dualbranch and six-branch receiver configurations. Nonetheless, there are many drawbacks to constructing diversity systems designed to be worn on the human body, especially when compared to integrating the technology into a local base station or using combining opportunities offered by multiple base stations. These include potential obtrusion to the user, the additional weight added to the wearable system, associated circuity and enclosures and also the extra drain on battery life.

To the best of our knowledge, a systematic investigation of the utilization of TSC based macro-diversity to overcome shadowing for outdoor wearable communications has yet to appear in the open literature. Therefore, in this paper, we examine the potential improvement in signal reliability
for outdoor wearable communications channels operating at 868 MHz using the switched combined signal forwarded from multiple spatially distributed base stations. It is widely known that an SSC scheme gains no further benefit from having more than two signal branches [19]. Accordingly, we consider dual-base station SSC, $L$-base station SEC and $L$-base station SECps schemes in this study. Most importantly though, for the first time, we statistically characterize the fading behavior observed at the output of the switched diversity combiners, i.e., from the perspective of combiner output, using the diversity specific equations which were developed under the assumption of independent and non-identically distributed (i.n.i.d.) Nakagami- $m$ fading channels.

The remainder of the paper is organized as follows. In Section II, we briefly review the statistical characteristics of the Nakagami- $m$ fading model before introducing theoretical equations for the cumulative distribution functions (CDFs) and probability density functions (PDFs) of $L$-base station SSC, SEC and SECps schemes operating in i.n.i.d. Nakagami$m$ fading channels. In Section III, we describe the measurement set-up, experiments and environments. In Section IV, the achievable diversity gain, correlation, number of path examinations and number of path switches for the SSC, SEC and SECps schemes are presented and compared with those for the PSC scheme. Model fitting for the SSC, SEC and SECps schemes is presented in Section V while a further performance analysis is conducted while considering the OP for the three schemes in Section VI. Finally, Section VII concludes the paper with some closing remarks.

## II. First-Order Statistics of Switched Combiners Operating Nakagami-m Fading Environments

## A. The Nakagami-m Fading Model

The Nakagami- $m$ fading model has been proven to characterize the fading behavior of a diverse range of wireless channels such as those found in body-centric [20], [21] and land-mobile [22], [23] communications systems. It is a general statistical model which includes as special cases a number of well-known distributions such as the one-sided Gaussian ( $m=0.5$ ) and Rayleigh ( $m=1$ ) distributions [24]. It can also be used to approximate the Rician distribution when $m>1$. As well as modeling small scale fading, the Nakagami$m$ model can be used to describe shadowing of the signal amplitude owing to its relationship with the gamma distribution. It is already well established that the gamma distribution can be used to model shadowing of the signal power [25], [26] and since gamma and Nakagami- $m$ random variables are related by a simple quadratic transformation, accordingly the signal power or equivalently SNR over a Nakagami- $m$ fading channel is distributed according to the gamma distribution [6], [27]. The PDF, $f_{\gamma}(\gamma)$, and CDF, $F_{\gamma}(\gamma)$ of the SNR over the Nakagami- $m$ fading channels can be expressed as [6]

$$
\begin{gather*}
f_{\gamma}(\gamma)=\frac{m^{m} \gamma^{m-1}}{\Gamma(m) \bar{\gamma}^{m}} \exp \left(-\frac{m \gamma}{\bar{\gamma}}\right)  \tag{1}\\
F_{\gamma}(\gamma)=1-\frac{\Gamma\left(m, \frac{m \gamma}{\bar{\gamma}}\right)}{\Gamma(m)} \tag{2}
\end{gather*}
$$

where $m$ is the fading severity parameter, $\bar{\gamma}=E[\gamma]$ is the average SNR where $E[\cdot]$ is the expectation operator, $\Gamma(\cdot)$ is the gamma function and $\Gamma(\cdot, \cdot)$ is the upper incomplete gamma function [28].

## B. L-base Station SSC operating over Nakagami-m Fading Channels

For the SSC scheme, when the received SNR at the currently selected branch, or equivalently in this case base station, falls below the predetermined switching threshold the receiver simply switches from one base station to another base station and then stays with that base station irrespective of its channel condition. When the fading observed at each of the base stations is assumed to be i.n.i.d. the CDF and PDF of the output SNR at an $L$-base station SSC combiner can be written as follows [19]

$$
\left.\begin{array}{rl}
F_{\mathrm{SSC}}(\gamma)= & \begin{cases} & \sum_{i=0}^{L-1}\left(\sum_{j=0}^{L-1} \frac{1}{F_{j}\left(\gamma_{T}\right)}\right)^{-1} F_{i}(\gamma), \\
\sum_{i=0}^{L-1} \lambda_{i}\left[F_{i}(\gamma)-F_{j}\left(\gamma_{T}\right)\right] \\
& +\left(\sum_{j=0}^{L-1} \frac{1}{F_{j}\left(\gamma_{T}\right)}\right)^{-1} F_{i}(\gamma), \\
f_{\mathrm{SSC}}(\gamma)= & \gamma \geq \gamma_{T}\end{cases} \\
\sum_{i=0}^{L-1}\left(\sum_{j=0}^{L-1} \frac{1}{F_{j}\left(\gamma_{T}\right)}\right)^{-1} f_{i}(\gamma), & \gamma<\gamma_{T} \tag{4}
\end{array}\right\}
$$

where $L$ is the number of base stations, $\gamma_{T}$ is the fixed switching threshold, $f_{i}(\cdot)$ and $F_{i}(\cdot)$ denote PDF and CDF for $i^{\text {th }}$ base station, respectively, and $\lambda_{i}$ is the probability that the $i^{\text {th }}$ base station is used in the SSC scheme, which can be obtained using an $L$-state Markov chain such that

$$
\begin{equation*}
\lambda_{i}=\left(\sum_{j=0}^{L-1} \frac{1}{F_{j}\left(\gamma_{T}\right)}\right)^{-1} \frac{1}{F_{i}\left(\gamma_{T}\right)}, i=0,1, \ldots, L-1 \tag{5}
\end{equation*}
$$

Now substituting (1) and (2) into (4), we can obtain the PDF of the output SNR of an $L$-base station SSC combiner operating over i.n.i.d. Nakagami- $m$ channels as given in (6).

## C. L-base station SEC operating over Nakagami-m Fading Channels

For the SEC scheme, when the received SNR at the currently selected base station falls below the predetermined switching threshold the receiver switches from the current base station to another base station and examines its SNR.

If it is not above the predetermined switching threshold, the receiver switches to another base station and examines its SNR again. The receiver repeats this process until either it finds an acceptable base station which is above the switching threshold or determines that all base stations are not acceptable. In the latter case, it usually uses the last examined base station. Again, for i.n.i.d. fading at each of the base stations, the CDF and PDF of the output SNR at an $L$-base station SEC combiner can be expressed as [19]
$F_{\mathrm{SEC}}(\gamma)= \begin{cases}\sum_{i=0}^{L-1} \lambda_{i} F_{i}(\gamma)\left[\prod_{k=0, k \neq i}^{L-1} F_{k}\left(\gamma_{T}\right)\right], & \gamma<\gamma_{T} \\ \sum_{i=0}^{L-1} \lambda_{i} \prod_{k=0}^{L-1} F_{k}\left(\gamma_{T}\right)+\sum_{i=0}^{L-1} \sum_{j=0}^{L-1} \lambda_{(i-j)_{L}} \\ \times\left[F_{i}(\gamma)-F_{i}\left(\gamma_{T}\right)\right] \prod_{k=0}^{j-1} F_{(i-j+k)_{L}}\left(\gamma_{T}\right), & \gamma \geq \gamma_{T}\end{cases}$
$f_{\mathrm{SEC}}(\gamma)= \begin{cases}\sum_{i=0}^{L-1} \lambda_{i}\left[\prod_{k=0, k \neq i}^{L-1} F_{k}\left(\gamma_{T}\right)\right] f_{i}(\gamma), & \gamma<\gamma_{T} \\ \sum_{i=0}^{L-1}\left[\sum_{j=0}^{L-1} \lambda_{(i-j)_{L}} \prod_{k=0}^{j-1} F_{(i-j+k)_{L}}\left(\gamma_{T}\right)\right] f_{i}(\gamma), \gamma \geq \gamma_{T}\end{cases}$
where $(a)_{b}$ denotes $a$ modulo $b$ and $\lambda_{i}$ is the stationary distribution of an $L$-state Markov chain and is defined as follows
$\lambda_{i}=\left[\sum_{j=0}^{L-1} \frac{F_{L-1}\left(\gamma_{T}\right)\left(1-F_{j}\left(\gamma_{T}\right)\right)}{F_{j}\left(\gamma_{T}\right)\left(1-F_{L-1}\left(\gamma_{T}\right)\right)}\right]^{-1} \frac{F_{L-1}\left(\gamma_{T}\right)\left(1-F_{i}\left(\gamma_{T}\right)\right)}{F_{i}\left(\gamma_{T}\right)\left(1-F_{L-1}\left(\gamma_{T}\right)\right)}$.
Similarly, by substituting (1) and (2) into (8), the PDF of the output SNR of an $L$-base station SEC combiner operating over i.n.i.d. Nakagami- $m$ channels can be obtained as given in (10).

## D. L-base Station SECps operating over Nakagami-m Fading Channels

When the received SNR at the currently selected base station falls below the predetermined switching threshold a receiver utilizing an SECps scheme switches from the current base station to another base station and examines its SNR in exactly the same manner as an SEC scheme. However, when there is no acceptable base station available after examining all base stations, the SECps scheme selects the best performing base station, i.e., the base station with the highest SNR, instead of the last examined one. For an $L$-base station SECps system in which the SNR is i.n.i.d. at each of the $L$ base stations, the PDF of the output SNR can be expressed as [29]

$$
f_{\mathrm{SSC}}(\gamma)=\left\{\begin{array}{c}
\sum_{i=0}^{L-1}\left(\sum_{j=0}^{L-1} \frac{\Gamma\left(m_{j}\right)}{\Gamma\left(m_{j}\right)-\Gamma\left(m_{j}, m_{j} \gamma_{T} / \bar{\gamma}_{j}\right)}\right)^{-1} \frac{m_{i}^{m_{i}} \gamma^{m_{i}-1}}{\Gamma\left(m_{i}\right) \bar{\gamma}_{i}^{m_{i}}} \exp \left(-\frac{m_{i} \gamma}{\bar{\gamma}_{i}}\right), \\
\sum_{i=0}^{L-1}\left[\lambda_{i}+\left(\sum_{j=0}^{L-1} \frac{\Gamma<\gamma_{T}}{\Gamma\left(m_{j}\right)-\Gamma\left(m_{j}, m_{j} \gamma_{T} / \bar{\gamma}_{j}\right)}\right)^{-1}\right] \frac{m_{i}^{m_{i}} \gamma^{m_{i}-1}}{\Gamma\left(m_{i}\right) \bar{\gamma}_{i}^{m_{i}}} \exp \left(-\frac{m_{i} \gamma}{\bar{\gamma}_{i}}\right), \gamma \geq \gamma_{T}
\end{array}\right.
$$

$$
\text { where } \lambda_{i}=\left(\sum_{j=0}^{L-1} \frac{\Gamma\left(m_{j}\right)}{\Gamma\left(m_{j}\right)-\Gamma\left(m_{j}, m_{j} \gamma_{T} / \bar{\gamma}_{j}\right)}\right)^{-1} \frac{\Gamma\left(m_{i}\right)}{\Gamma\left(m_{i}\right)-\Gamma\left(m_{i}, m_{i} \gamma_{T} / \bar{\gamma}_{i}\right)}, i=0,1, \ldots, L-1
$$

$$
f_{\mathrm{SEC}}(\gamma)= \begin{cases}\sum_{i=0}^{L-1} \lambda_{i}\left[\prod_{k=0, k \neq i}^{L-1}\left(1-\frac{\Gamma\left(m_{k}, m_{k} \gamma_{T} / \bar{\gamma}_{k}\right)}{\Gamma\left(m_{k}\right)}\right)\right] \frac{m_{i}^{m_{i}} \gamma^{m_{i}-1}}{\Gamma\left(m_{i}\right) \bar{\gamma}_{i}^{m_{i}}} \exp \left(-\frac{m_{i} \gamma}{\bar{\gamma}_{i}}\right), & \gamma<\gamma_{T}  \tag{10}\\ \sum_{i=0}^{L-1}\left[\sum_{j=0}^{L-1} \lambda_{(i-j)_{L}} \prod_{k=0}^{j-1}\left(1-\frac{\Gamma\left(m_{n}, m_{n} \gamma_{T} / \bar{\gamma}_{n}\right)}{\Gamma\left(m_{n}\right)}\right)\right] \frac{m_{i}^{m_{i}} \gamma^{m_{i}-1}}{\Gamma\left(m_{i}\right) \bar{\gamma}_{i}^{m_{i}}} \exp \left(-\frac{m_{i} \gamma}{\bar{\gamma}_{i}}\right), & \gamma \geq \gamma_{T}\end{cases}
$$

where $n=(i-j+k)_{L}$ and

$$
F_{\mathrm{SECps}}(\gamma)=\left\{\begin{array}{cc}
\prod_{i=1}^{L} F_{i}(\gamma), & \gamma<\gamma_{T}  \tag{12}\\
\prod_{k=1}^{L} F_{k}\left(\gamma_{T}\right) \\
+\sum_{i=1}^{L}\left[\prod_{j=1}^{i-1} F_{j}\left(\gamma_{T}\right)\right]\left[F_{i}(\gamma)-F_{i}\left(\gamma_{T}\right)\right], & \gamma \geq \gamma_{T}
\end{array}\right.
$$

The PDF of the output SNR can then be obtained by differentiating (12) with respect to $\gamma$

$$
f_{\mathrm{SECps}}(\gamma)= \begin{cases}\sum_{i=1}^{L}\left[\prod_{j=1}^{i-1} F_{j}\left(\gamma_{T}\right)\right] f_{i}(\gamma), & \gamma \geq \gamma_{T}  \tag{13}\\ \sum_{i=1}^{L}\left[\prod_{j=1, j \neq i}^{L} F_{j}(\gamma)\right] f_{i}(\gamma), & \gamma<\gamma_{T}\end{cases}
$$

Again, the PDF of the output SNR at an $L$-base station SECps combiner operating over i.n.i.d. Nakagami- $m$ channels can be obtained by substituting (1) and (2) into (13) as given in (14).

## III. Experimental Setup and Measurement Procedure

The wearable device used in this study was a purposely developed wireless sensor node with dimensions of 45 mm x $60 \mathrm{~mm} \times 1.6 \mathrm{~mm}$ as shown in Fig. 1(a). The unit consisted of a CC1110F32 radio frequency (RF) transceiver, manufactured by Texas Instruments (TI) which was configured to operate at 868 MHz using a printed meander-line PCB monopole antenna. During the experiments, the unit was configured to transmit a 9 byte data packet at a data rate of 500 Kbps using minimum-shift keying. All data transmissions occurred at a regular interval of 20 ms with an output power level of 0 dBm .

The test subject (an adult male of height 1.70 m and mass 75 kg ) wore a sports T -shirt ( $86 \%$ polyester / $14 \%$ elastane) with a special holding pocket purposely sown on to the garment at the central chest region as shown in Fig. 1(a). The sensor node was carefully positioned in the pocket such that the printed antenna was in a plane parallel to the surface of the test subject's body. It is worth highlighting that the battery which was used to power the sensor node ensured that there was at least a 6 mm separation between the body and the RF circuitry. The virtual base station array consisted of 10 identical, equidistant base stations which were positioned in a rectangular configuration with a length of approximately 20 m and a width of 6.6 m as shown in Fig. 2. The purposely

$$
f_{\mathrm{SECps}}(\gamma)=\left\{\begin{array}{cc}
\sum_{i=1}^{L}\left[\prod_{j=1}^{i-1}\left(\frac{\Gamma\left(m_{j}, m_{j} \gamma_{T} / \bar{\gamma}_{j}\right)}{\Gamma\left(m_{j}\right)}\right)\right] \frac{m_{i}^{m_{i}} \gamma^{m_{i}-1}}{\Gamma\left(m_{i}\right) \bar{\gamma}_{i}^{m_{i}}} \exp \left(-\frac{m_{i} \gamma}{\bar{\gamma}_{i}}\right), & \gamma \geq \gamma_{T}  \tag{14}\\
\sum_{i=1}^{L}\left[\prod_{j=1, j \neq i}^{L}\left(\frac{\Gamma\left(m_{j}, m_{j} \gamma / \bar{\gamma}_{j}\right)}{\Gamma\left(m_{j}\right)}\right)\right] \frac{m_{i}^{m_{i} \gamma^{m_{i}-1}}}{\Gamma\left(m_{i}\right) \bar{\gamma}_{i}^{m_{i}}} \exp \left(-\frac{m_{i} \gamma}{\bar{\gamma}_{i}}\right), & \gamma<\gamma_{T}
\end{array}\right.
$$


(a)

(b)

Fig. 1. (a) Purposely developed garment with mounting pocket at front central chest and the bodyworn wireless node used in the measurements; (b) satellite view of the measurement environment showing the positions of base stations.


Fig. 2. Five individual user movement scenarios: a rectangular shape walk path (scenarios 1 and 2); a diagonal-line walk (scenario 3 ); a meandering walk path (scenarios 4 and 5). It should be noted that dotted lines and base station 5 represent the test subject's walk path and the target base station, respectively.
developed base station units also consisted of a CC1110F32 RF transceiver configured to record the received signal strength of each received packet. The antenna used by the base station units was a +3.0 dBi omnidirectional monopole antenna with a 10 dB bandwidth of $61 \mathrm{MHz}(833-894 \mathrm{MHz})$, positioned at a height of 1 m from ground level using a non-conductive support.

As shown in Fig. 1(b), all of the experiments conducted in this study were carried out in an outdoor playing field at the Ormeau Park within the city of Belfast in the United Kingdom. They were designed to emulate the channel characteristics which may be present in outdoor wearable applications such as sports and health monitoring, people tracking and positioning etc. Five individual measurement scenarios, all based around
a walking test subject, were considered as shown in Fig. 2. These scenarios can be broadly categorized into the walk path which the movement followed. They included a rectangular shaped walk path (scenarios 1 and 2), a diagonal-line walk path (scenario 3) and a meandering walk path (scenarios 4 and 5). In practice, it is the SNR which is of most interest in the analysis of the performance of wireless systems. For the purpose of transforming the received signal power into the received SNR, prior to the acquisition of the channel data, a number of noise floor measurements were performed. To improve the robustness of the noise parameter estimates, these measurements were repeated 10 times. The corresponding mean recorded noise threshold was -100.9 dBm while the corresponding lowest received signal power observed in the environment was -94.0 dBm .

## IV. Base Station Correlation, Diversity Gain, Number of Path Examinations and Number of Path SWITCHES

Prior to the data analysis, it was required to transform the received signal power into the received SNR. To this end, the noise parameters $\mu$ (mean) and $\sigma$ (standard deviation) were first estimated from noise floor measurements using maximum likelihood estimation (MLE) [30] under the assumption that noise envelope was characterized by a Gaussian distribution [31]. The estimated noise parameters obtained over the 10 repeated trials were then averaged and found to be 0.0021 mV (standard deviation 0.017 uV ) and 0.0006 mV (standard deviation 0.009 uV ) for the $\mu$ and $\sigma$ parameters, respectively. The total duration of the 10 repeated noise floor measurements was approximately 10 minutes. From the noise parameter estimates, random variables representing the noise process were then generated. Following from this, the received signal power was then transformed into the received SNR using the definition of $\mathrm{SNR}, \mathrm{SNR}=\mathrm{P}_{\text {Signal }} / \mathrm{P}_{\text {Noise }}$ where $\mathrm{P}_{\text {Signal }}$ and $\mathrm{P}_{\text {Noise }}$ denote the signal power and noise power, respectively. As an example, Fig. 3 shows the received signal power at base station 1 for scenario 5 along with its transformed SNR. The average received SNR at each base station for all considered scenarios ranged between 22.6 dB and 34.0 dB . Based on these averaged SNR values, three different switching thresholds were determined, which were low ( 10 dB ), medium ( 30 dB ) and high ( 50 dB ) thresholds.

## A. Base Station Correlation

Since any significant correlation between the signal received at each of the base stations has the potential to degrade the diversity gain, it is important to determine the level of correlation which may exist. For a macro-diversity scheme to be effective, the received signal at each base station should be statistically independent. In the context of diversity reception, two signals are said to be suitably de-correlated if their crosscorrelation coefficient is less than 0.7 [1]. Fig. 4 shows the CDFs of the cross-correlation coefficients calculated for all of the considered scenarios. It is worth noting that the crosscorrelation coefficient computations were performed using the approach proposed in [32]. It is clear from the Fig. 4 that the


Fig. 3. Received signal power (continuous lines) at base station 1 for scenario 5 alongside the transformed SNR (dashed lines).


Fig. 4. CDFs of the calculated cross-correlation coefficients for all of the considered scenarios.
majority of the estimated cross-correlation coefficients were between -0.7 and 0.7 . This result suggests that a switched combining based macro-diversity system equipped with multiple base stations can provide a worthwhile improvement in the received signal reliability.

## B. Diversity Gain

To evaluate the potential improvement in the received signal reliability that could be obtained using a switched combining based macro-diversity system with the SSC, SEC and SECps schemes, we utilize the concept of macro-diversity gain. This is defined as the signal reliability improvement between the SNR of the diversity combiner and that of the target base station for a given probability or signal reliability. It should be noted that for this study, base station 5 was considered as the target base station and all macro-diversity gain calculations were made at a signal reliability of $90 \%$. For brevity, herein we refer to macro-diversity gain as simply diversity gain. In this study, we have considered dual- and four-base station configurations with two different potential groupings of base stations. These were: group 1 a dual-base station configuration consisting of base stations 1 and 6; group 2 another dualbase station configuration consisting of base stations 5 and 10; group 3 a four-base station configuration consisting of base stations 1, 4, 6 and 9; group 4 another four-base station configuration consisting of base stations $3,5,8$ and 10 .

TABLE I
Diversity Gains for the SSC, SEC, SECps and PSC Schemes with Three Different Switching Thresholds for All Measurement Scenarios and Groupings.

|  | Switching <br> Threshold <br> (dB) | Macro-Diversity Gain (dB) |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Group 1 (1, 6) |  |  |  | Group $2(5,10)$ |  |  |  | Group 3 (1, 4, 6, 9) |  |  | Group 4 (3, 5, 8, 10) |  |  |
|  |  | SSC | SEC | SECps | PSC | SSC | SEC | SECps | PSC | SEC | SECps | PSC | SEC | SECps | PSC |
| S1 | 10 | 7.7 | 7.7 | 7.7 |  | 1.5 | 1.5 | 1.5 |  | -0.5 | $-0.5$ |  | 1.0 | 1.0 |  |
|  | 30 | 2.8 | 2.8 | 10.6 | 10.6 | -0.9 | -0.9 | 6.2 | 6.2 | 13.7 | 13.7 | 13.7 | 12.3 | 13.2 | 13.2 |
|  | 50 | -0.4 | -0.4 | 10.6 |  | -2.2 | -2.2 | 6.2 |  | 0.2 | 13.7 |  | $-1.0$ | 13.2 |  |
| S2 | 10 | -2.5 | -2.5 | -2.5 |  | 0.0 | 0.0 | 0.0 |  | -2.5 | -2.5 |  | -3.6 | -3.6 |  |
|  | 30 | 6.4 | 6.4 | 6.4 | 6.4 | 3.8 | 3.8 | 5.1 | 5.1 | 6.8 | 6.9 | 6.9 | 7.6 | 7.6 | 7.8 |
|  | 50 | -8.4 | -8.4 | 6.4 |  | -8.5 | -8.5 | 5.1 |  | -8.2 | 6.9 |  | -6.5 | 7.8 |  |
| S3 | 10 | 6.2 | 6.2 | 6.2 |  | 1.9 | 1.9 | 1.9 |  | 1.1 | 1.1 |  | 1.8 | 1.8 |  |
|  | 30 | 9.8 | 9.8 | 12.8 | 12.8 | 3.2 | 3.2 | 11.4 | 11.4 | 14.6 | 14.7 | 14.9 | 14.9 | 14.9 | 15.0 |
|  | 50 | 3.5 | 3.5 | 12.8 |  | 0.4 | 0.4 | 11.4 |  | -2.0 | 14.9 |  | 0.2 | 15.0 |  |
| S4 | 10 | 8.0 | 8.0 | 8.0 |  | 9.6 | 9.6 | 9.6 |  | 12.2 | 12.2 |  | 9.3 | 9.3 |  |
|  | 30 | 11.1 | 11.1 | 16.5 | 16.5 | 12.2 | 12.2 | 15.3 | 15.3 | 18.8 | 18.9 | 18.9 | 19.2 | 19.2 | 19.5 |
|  | 50 | 5.7 | 5.7 | 16.5 |  | 4.1 | 4.1 | 15.3 |  | 4.2 | 18.9 |  | 5.0 | 19.5 |  |
| S5 | 10 | 7.8 | 7.8 | 7.8 |  | 6.8 | 6.8 | 6.8 |  | 8.0 | 8.0 |  | 5.2 | 5.2 |  |
|  | 30 | 13.9 | 13.9 | 16.6 | 16.6 | 9.0 | 9.0 | 15.0 | 15.0 | 18.2 | 18.3 | 18.4 | 18.2 | 18.2 | 18.3 |
|  | 50 | 5.5 | 5.5 | 16.6 |  | 3.7 | 3.7 | 15.0 |  | 4.0 | 18.4 |  | 5.1 | 18.3 |  |

Table I shows the diversity gain statistics for dual-base station SSC, SEC and SECps schemes with groups 1 and 2, four-base station SEC and SECps schemes with groups 3 and 4. For comparison, the diversity gains for dual- and fourbase station PSC are also shown in Table I. For a medium switching threshold, the benefit of having more than two available base stations was demonstrated by comparing the diversity gains between dual- and four-base station configurations. For example, four-base station SEC with group 3 for scenario 1 provided a diversity gain of 13.7 dB whereas dualbase station SEC with group 1 achieved a diversity gain of 2.8 dB . Moreover, for all of the groupings and scenarios, dualbase station SEC provided the same performance as dual-base station SSC. Table I shows that the estimated diversity gain not only varied according to the different scenarios but also with different groupings. This observation can be attributed to each base station having experienced different shadowing intensities depending on the position and orientation of the test subject's body during each movement scenario. When comparing the diversity gains obtained across all scenarios, the values obtained for scenario 4 were the highest. One possible explanation for this is that the average SNR at the target base station (base station 5) for scenario 4 was smaller than those for the other scenarios. This occurred due to the direct signal path between the bodyworn node and the target base station existing only for a relatively short length of time compared to those for other scenarios due to the test subject's movement.

To visually investigate the improvement in the received signal reliability using the switched diversity schemes, Fig. 5 shows the received SNR time series at base stations 1, 4, 6 and 9 (group 3) along with the output SNR of four-base station SEC and SECps with a medium switching threshold ( 30 dB ) for scenario 2 . When the currently selected base station suffered from deep fading due to the shadowing caused


Fig. 5. Received SNR at base stations 1 (blue), 4 (red), 6 (green) and 9 (yellow) along with the output SNR (black) of four-base station switched diversity schemes for scenario 2: (a) SEC and (b) SECps.
by the test subject's body, the switched combining based macro-diversity schemes selected and switched to another base station. Consequently, for both the SEC and SECps schemes, the majority of SNR values below the 30 dB level (the predetermined switching threshold) were eliminated. This suggests that a macro-diversity system using either an SEC or SECps scheme made up of base stations $1,4,6$ and 9 can mitigate shadowing effect of the person's body and achieve a significant improvement in signal reliability.

For a dual-base station configuration operating with a medium switching threshold, group 1 always provided a greater diversity gain than group 2 with the exception of scenario 4. This suggests that the location of the base stations in group 1 was more appropriate compared to group 2


Fig. 6. Effect of different switching thresholds on achievable diversity gain of four-base station (a) SEC and (b) SECps with group 3 (continuous lines) and group 4 (dashed lines) for all of movement scenarios.
in general. However, for a four-base station configuration, groups 3 and 4 provided similar diversity gains for all of the movement scenarios. As well as this, for the majority of the movements considered in this study, adding the two additional base stations also offered no significant difference in the diversity gains provided by the SEC and SECps schemes when a medium switching threshold was selected. For example, as shown in Table I, the diversity gains for dual-base station SEC and SECps with group 1 for scenario 1 were 2.8 dB and 10.6 dB , respectively. On the other hand, for four-base station SEC and SECps with group 3, both had the same diversity gain which was 13.7 dB . These suggest that a switched diversity system with more than two base stations is less affected by the location of the base stations and thus provides a more stable performance in terms of signal reliability.

Furthermore, it was found that the estimated diversity gains for both the dual-base station and four-base station configurations strongly depended on the switching threshold. For example, the diversity gains for four-base station SEC with group 3 for scenario 2 were $-2.5,6.8$ and -8.2 dB at the low, medium and high switching thresholds, respectively. Interestingly, negative diversity gains were also observed at the low and high switching thresholds, indicating that there was no benefit to using a switched diversity scheme with these switching thresholds. To examine the effect of different switching thresholds on the achievable diversity gain, Fig. 6 shows the diversity gains for four-base station SEC and SECps with different switching threshold values ranging between 0 dB and 60 dB for all of scenarios. It is obvious that the estimated diversity gains varied according to the switching threshold, but there always existed an optimum switching threshold which maximizes the diversity gain. With the optimum switching threshold, both four-base station SEC and SECps systems provided almost the same diversity gain as an equivalent PSC system. While the diversity gain for four-base station

SEC decreases beyond the optimum switching threshold, the diversity gain for four-base station SECps became saturated at the maximum achievable diversity gain level. This was most likely due to the different combining methods implemented by the SEC and SECps schemes. The SEC scheme selects the last examined base station when no acceptable base station is found after examining all available options. On the other hand, the SECps scheme selects the best path which has the highest SNR among all paths instead of the last examined base station. The SECps scheme therefore acts as a PSC scheme when the switching threshold is high and no acceptable path is found after examining all diversity paths.

## C. Number of Path Examinations and Switches

To evaluate the trade off between performance and complexity (which is related to energy consumption), we evaluated the number of path examinations and the number of path switches between base stations for the SEC and SECps schemes. As shown in Fig. 7, the number of path examinations and switches for the SEC an SECps schemes were almost the same when the switching threshold was low while the SECps scheme had a greater number of path examinations and switches compared to the SEC scheme at the middle and high switching threshold levels. This was most likely due to that when there is no acceptable base station available the SEC scheme usually selects the last examined base station while the SECps scheme selects the best performing base station. Consequently, for an $L$-base station arrangement, the SEC scheme has at most $L-1$ path switches whereas the SECps scheme has at most $L$ path switches, i.e., the number of path switches for the SECps scheme usually is greater than that for the SEC scheme. They are the same only if the last examined base station has the highest SNR.

Likewise, the number of path examinations for the SEC and SECps schemes were almost the same at the low switching


Fig. 7. Diversity gain, the number of path examinations and the number of path switches for scenario 5 using the group 3 configuration with four-base station SEC and SECps schemes for different switching thresholds. For comparison, (a)-(b) four-base station PSC using the group 3 configuration and (d)-(f) dual-base station SEC and SECps using the group 1 configuration are also presented.
threshold levels whereas the number of path examinations for the SECps was greater than that for the SEC at the medium and high switching threshold levels. More specifically, for an $L$-base station arrangement, when the receiver switches from the $(L-1)^{\text {th }}$ base station to the $L^{\text {th }}$ base station (i.e., last base station), the SECps scheme needs to monitor the $L^{\text {th }}$ base station whereas the SEC scheme does not need to do this because it switches to the $L^{\text {th }}$ base station anyway irrespective of whether the received SNR at $L^{\text {th }}$ base station is above the switching threshold or not. Based on the diversity gain, the number of path examinations and the number of path switches, it was observed that the SECps scheme provided a greater diversity gain, but the additional number of path examinations and switches will lead to more energy consumption compared to the SEC scheme.

When compared with a PSC scheme, as shown in Figs. 7(a) and (b), the SECps scheme had a smaller number of path examinations at medium switching threshold levels, but it had a similar diversity gain. This can be explained by the fact that the PSC scheme monitors the SNR of all of the base stations and then selects the base station with the highest SNR. Therefore, at medium switching threshold levels, the SECps scheme prevents the unnecessary monitoring while providing a similar performance compared to the PSC scheme, suggesting that the SECps scheme is less complex and thus more energy efficient compared to the PSC scheme. However, as expected, it was observed that the number of path examinations for the SECps and PSC became similar at high switching threshold levels. Figs. 7(d)-(f) show a comparison of the diversity gain, the number of path examinations and the number of path switches between base stations for dual- and four-base station SEC and SECps schemes. While it is obvious that four-base station SEC and SECps provided a greater diversity gain (higher performance) than dual-base station SEC and SECps, they also
had a significantly greater number of path examinations and switches (higher complexity and higher energy consumption). Therefore the choice as to which configuration and scheme to implement for wearable systems will come down to a choice between performance and complexity. For some, but not all cases (see Fig. 7 and Table I), a dual-base station configuration with the appropriate switching threshold/technology may offer a good compromise between complexity (energy consumption) and information recovering capability.

## V. Fading Statistics at the Output of the Switched Combiners

To characterize the fading behavior at the output of the virtual switched combiners, the diversity specific analytical equations presented in (6), (10) and (14) for $L$-base station SSC, SEC and SECps schemes operating in i.n.i.d. Nakagami$m$ fading channels were fitted to the empirical data. The Nakagami $m$ and $\bar{\gamma}$ parameters were estimated using a nonlinear least squares routine written in MATLAB to fit (6), (10) and (14) to the measurement data. Again, we have considered dual- and four-base station configurations with the same groupings presented in Section IV. It should be noted that the minimum data set size used for the parameter estimation was 761 samples.
As an example of the results of the model fitting process, Fig. 8 shows the PDFs of four-base station SEC and SECps (group 3) with three different switching thresholds for scenario 5. The resistor-average distance (RAD) was evaluated to provide a quantitative measure of the goodness-of-fit of the theoretical PDFs with the measured data. Unlike the KullbackLeibler divergence (KLD), the RAD satisfies the triangle inequality and thus is a true distance metric. This can be defined as follows [33]


Fig. 8. Empirical (black circle symbols) and theoretical (continuous lines) PDFs for scenario 5 with group 3 for four-base station SEC with (a) low, (b) medium and (c) high switching thresholds and four-base station SECps with (d) low, (e) medium and (f) high switching thresholds.

$$
\begin{equation*}
\operatorname{RAD}=\left(\frac{1}{\operatorname{KLD}(p, q)}+\frac{1}{\operatorname{KLD}(q, p)}\right)^{-1} \tag{15}
\end{equation*}
$$

where $\operatorname{KLD}(\cdot, \cdot)$ denotes the $\operatorname{KLD}$ given by $\operatorname{KLD}(p, q)=$ $\int_{-\infty}^{\infty} p(x) \log _{2}\left(\frac{p(x)}{q(x)}\right) d x$ with $p(x)$ and $q(x)$ denoting the true PDF of the data and the test PDF, i.e., the approximated PDF of $p(x)$, respectively [34]. As the RAD tends towards zero, the test PDF (theoretical PDF) is in very good agreement with the true PDF (empirical PDF). The RAD analysis results are presented in Table II. The minimum and maximum RAD values were 0.0039 and 0.0887 respectively, suggesting that the theoretical models for SEC and SECps generally provided an adequate fit to the measured data. To assist with the interpretation of the goodness-of-fit, the equivalent RAD was used to calculate the standard deviation $\sigma$ of a zero-mean, $\sigma^{2}$ variance Gaussian PDF that is used to approximate a zeromean, unit variance Gaussian PDF ${ }^{1}$. The minimum and maximum calculated $\sigma$ values corresponding to the RAD above were 1.09 and 1.53 respectively. As the Gaussian distribution is widely known and used, this provides a reference level upon which our fits may be interpreted.

Furthermore, to allow the reader to reproduce the theoretical plots reported, Table III provides the parameter estimates for four-base station SEC and SECps (group 3) with three different switching thresholds for all considered movement scenarios. As we can see from Table III, the parameter estimates ob-

[^1]tained for the fading experienced at each of the considered base stations were different, suggesting that each base station experienced non-identical Nakagami- $m$ fading. Additionally, as expected, the parameter estimates also varied according to the user's movement. For example, when comparing scenarios 4 and 5 for four-base station SECps with a medium switching threshold ( 30 dB ), the estimated $m$ parameters for scenario 4 were higher than those for scenario 5 . This suggests that the fading observed at the four base stations during scenario 4 were subject to less shadowing compared to scenario 5 . This is supported by the fact that the average SNR for the output of four-base station SECps (group 3) for scenario 4 ( 36.4 dB ) was greater than that for scenario $5(35.8 \mathrm{~dB})$.

As shown in Fig. 8, the shapes of the PDFs were different according to the switching threshold that was adopted. When a low switching threshold was chosen (i.e., 10 dB ) the PDFs of both the SEC and SECps were the same as shown in Fig. 8(a) and (d). This was most likely due to the fact that path switching between base stations rarely occurred at the low switching threshold level. More specifically, as shown in Fig. 9(a), there was only one instance of path switching between base stations (base station $6 \rightarrow 9$ ) with the virtual switched combiner selecting base station 9 for the remainder of the time. It should be noted that the received SNR at base stations 1 and 4 in group 3 is not shown in Fig. 9(a) for clarity. As evidence for this, Fig. 9(b) shows that the PDF of the output SNR of four-base station SEC and the PDF of the received SNR at base station 9. It is clear that these two PDFs were similar. Note that the PDF of the received SNR at base station 9 in Fig. 9(b) was generated using the received SNR beyond the vertical line in Fig. 9(a) which represents path switching from base station 6 to 9 .

On the contrary, path switching between base stations occurs

TABLE II
Estimated Resistor-Average Distance for all of the Considered Cases.

| Switching Threshold | Scenarios | Group 1 |  | Group 2 |  | Group 3 |  | Group 4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 2-SEC | 2-SECps | 2-SEC | 2-SECps | 4-SEC | 4-SECps | 4-SEC | 4-SECps |
| Low ( 10 dB ) | S1 | 0.0267 | 0.0224 | 0.0213 | 0.0213 | 0.0070 | 0.0206 | 0.0139 | 0.0135 |
|  | S2 | 0.0194 | 0.0441 | 0.0201 | 0.0120 | 0.0106 | 0.0252 | 0.0192 | 0.0238 |
|  | S3 | 0.0150 | 0.0162 | 0.0467 | 0.0309 | 0.0153 | 0.0297 | 0.0085 | 0.0172 |
|  | S4 | 0.0172 | 0.0239 | 0.0137 | 0.0175 | 0.0070 | 0.0316 | 0.0107 | 0.0096 |
|  | S5 | 0.0246 | 0.0232 | 0.0208 | 0.0162 | 0.0048 | 0.0107 | 0.0098 | 0.0182 |
| Medium ( $\mathbf{3 0} \mathbf{~ d B \text { ) }}$ | S1 | 0.0091 | 0.0061 | 0.0211 | 0.0067 | 0.0206 | 0.0107 | 0.0254 | 0.0238 |
|  | S2 | 0.0385 | 0.0115 | 0.0280 | 0.0120 | 0.0779 | 0.0111 | 0.0529 | 0.0178 |
|  | S3 | 0.0465 | 0.0067 | 0.0279 | 0.0081 | 0.0159 | 0.0064 | 0.0168 | 0.0129 |
|  | S4 | 0.0233 | 0.0600 | 0.0193 | 0.0083 | 0.0190 | 0.0258 | 0.0337 | 0.0137 |
|  | S5 | 0.0540 | 0.0089 | 0.0104 | 0.0258 | 0.0356 | 0.0120 | 0.0388 | 0.0124 |
| High ( 50 dB ) | S1 | 0.0159 | 0.0049 | 0.0359 | 0.0067 | 0.0190 | 0.0151 | 0.0551 | 0.0262 |
|  | S2 | 0.0195 | 0.0130 | 0.0120 | 0.0099 | 0.0090 | 0.0109 | 0.0226 | 0.0135 |
|  | S3 | 0.0150 | 0.0110 | 0.0074 | 0.0039 | 0.0119 | 0.0061 | 0.0197 | 0.0062 |
|  | S4 | 0.0887 | 0.0557 | 0.0273 | 0.0072 | 0.0614 | 0.0122 | 0.0155 | 0.0158 |
|  | S5 | 0.0104 | 0.0061 | 0.0241 | 0.0081 | 0.0222 | 0.0108 | 0.0221 | 0.0099 |




Fig. 9. (a) Received SNR at base stations 6 and 9 along with the output SNR of four-base station SEC (continuous lines); (b) PDFs of the output SNR (circle symbols) of four-base station SEC and the received SNR (continuous lines) at base station 9 beyond the vertical line which represents path switching from base station 6 to 9. It should be noted that the received SNR at base stations 1 and 4 in group 3 are not shown in Fig. 10(a) for clarity.
during almost every single time slot when the switching threshold is high ( 5 dB ). This is particularly evident from Fig. 10, where the SEC scheme switched from the currently selected base station to another base station even if the presently selected base station had the highest SNR, causing a degradation in the overall performance. As a result of this, there was a significant increase in the spread of the output SNR of the SEC scheme as shown in Fig. 8(c). However, the SECps scheme does not follow this regime when the switching threshold is high as it favors the base station with the highest SNR when no acceptable signal base station is above the switching threshold (Fig. 10). As discussed in Section IV, in this scenario, the SECps scheme effectively operates as a PSC scheme. Therefore, unlike the SEC scheme, the majority of the SECps output SNR levels where in the reduced range from 25 dB to 45 dB , which resulted in an empirical probability density with a significantly reduced spread as shown in Fig. 8(f).

For both the SEC and SECps schemes, when the switching threshold was set at a medium value ( 30 dB ), the majority of
combiner output SNR levels ranged between 25 dB and 45 dB as shown in Fig. 8(b) and (e). These were almost identical to those obtained for the SECps scheme configured with a high switching threshold, i.e., a PSC scheme, although occasionally the SEC scheme still had instances where the combiner output SNR was below 15 dB . When compared in terms of the number of path examinations and achievable diversity gain, the SECps scheme operating with a medium switching threshold provided a more favorable alternative because it achieved sufficient performance with a lesser number of path examinations compared to the PSC scheme.

Further evidence of the benefits of having more than two base stations can also be provided by analyzing the fading statistics at the output of the switched diversity combiner. For example, Fig. 11 shows the PDFs of dual-base station SEC and SECps with group 2 and four-base station SEC and SECps with group 4 for scenario 2 when a medium switching threshold was adopted. As we can see, for both the SEC and SECps schemes, the four-base station configuration had a lower number of signal observations at low SNR levels and

TABLE III
Parameter Estimates for Four-Base Station SEC and SECps with Three Different Switching Thresholds for All of the Considered Movement Scenarios in Group 3 (Base Stations 1, 4, 6, and 9).

|  | 4-SEC |  |  |  |  |  |  |  | 4-SECps |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $m_{1}$ | $\overline{\gamma_{1}}$ | $m_{2}$ | $\overline{\gamma_{2}}$ | $m_{3}$ | $\overline{\gamma_{3}}$ | $m_{4}$ | $\overline{\gamma_{4}}$ | $m_{1}$ | $\overline{\gamma_{1}}$ | $m_{2}$ | $\overline{\gamma_{2}}$ | $m_{3}$ | $\overline{\gamma_{3}}$ | $m_{4}$ | $\overline{\gamma_{4}}$ |
|  | Low Switching Threshold ( 10 dB ) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| S1 | 2.9 | 52.7 | 6.4 | 13.3 | 15.0 | 6.8 | 1.6 | 2.9 | 0.9 | 46.7 | 12.8 | 11.2 | 15.0 | 54.6 | 4.4 | 3.8 |
| S2 | 9.0 | 14.6 | 4.1 | 59.4 | 15.0 | 7.1 | 15.0 | 9.0 | 1.5 | 53.5 | 15.0 | 13.2 | 12.0 | 13.2 | 14.1 | 7.9 |
| S3 | 2.1 | 100 | 4.2 | 39.3 | 9.3 | 11.6 | 15.0 | 2.1 | 1.3 | 34.0 | 15.0 | 2.0 | 2.1 | 6.3 | 15.0 | 2.3 |
| S4 | 8.0 | 14.3 | 3.8 | 64.2 | 15.0 | 7.1 | 15.0 | 7.5 | 1.8 | 68.1 | 15.0 | 18.8 | 9.3 | 16.9 | 14.1 | 88.1 |
| S5 | 4.2 | 73.6 | 3.1 | 100 | 7.5 | 21.1 | 15.0 | 8.7 | 1.6 | 61.4 | 15.0 | 10.8 | 15.0 | 62.9 | 7.6 | 15.4 |
|  | Medium Switching Threshold ( $\mathbf{3 0} \mathbf{~ d B}$ ) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| S1 | 3.9 | 58.3 | 0.5 | 0.1 | 10.0 | 1.5 | 0.8 | 62.9 | 4.2 | 61.2 | 0.5 | 48.9 | 15.0 | 7.1 | 15.0 | 7.1 |
| $\mathbf{S} 2$ | $2.5$ | 100 | 15.0 | 44.5 | 8.2 | 64.2 | 15.0 | 44.5 | 13.4 | 0.4 | 0.7 | 38.0 | 9.0 | 53.3 | 9.6 | 0.1 |
| S3 | $15.0$ | 1.8 | 11.7 | 1.1 | 0.6 | 80.6 | 6.1 | 58.1 | 0.5 | 30.5 | 7.6 | 59.7 | 15.0 | 19.6 | 15.0 | 19.6 |
| S4 | 9.8 | $64.7$ | 0.9 | 100 | 3.5 | 100 | 15.0 | 46.6 | 0.5 | 45.8 | 15.0 | 10.9 | 9.7 | 62.6 | 15.0 | 14.3 |
| S5 | 0.8 | 62.8 | 4.7 | 58.9 | 15.0 | 1.0 | 9.1 | 4.8 | 5.1 | 60.9 | 0.5 | 100 | 2.9 | 0.4 | 8.9 | 0.2 |
|  | High Switching Threshold (50 dB) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| S1 | 14.0 | 59.7 | 1.8 | 22.9 | 13.5 | 41.5 | 11.6 | 74.5 | 5.8 | 33.4 | 15.0 | 9.4 | 3.3 | 55.6 | 0.5 | 31.2 |
| S2 | 1.7 | 25.1 | 8.1 | 32.9 | 12.9 | 83.1 | 5.0 | 51.3 | 7.6 | 26.9 | 5.1 | 51.0 | 15.0 | 34.1 | 0.5 | 30.4 |
| S3 | 7.3 | 20.7 | 1.5 | 18.9 | 13.7 | 28.6 | 5.9 | 51.7 | 6.2 | 19.9 | 15.0 | 29.8 | 6.7 | 56.6 | 0.5 | 30.6 |
| S4 | 8.1 | 49.1 | 13.7 | 35.4 | 5.5 | 58.5 | 1.7 | 26.2 | 6.8 | 58.7 | 14.9 | 32.5 | 0.5 | 21.0 | 0.5 | 41.7 |
| S5 | 4.6 | 25.0 | 7.3 | 22.9 | 6.1 | 64.2 | 1.7 | 29.4 | 5.2 | 52.7 | 12.0 | 28.0 | 15.0 | 11.8 | 1.4 | 50.6 |



Fig. 10. Excerpt of the SNR time series obtained for scenario 5 comparing four-base station SEC and SECps with the received SNR at base stations 1, 4,6 and 9 .
a higher number of signal observations at high SNR levels than the dual-base station configuration. More specifically, as shown in Fig. 11(a), the dual-base station configuration had some output SNR levels which were less than 15 dB whereas the four-base station configuration had no output SNR less than 15 dB . This result indicates that an additional improvement in the signal quality can be achieved by implementing a four-base station macro-diversity configuration, in which case all SNR drops below 15 dB level will be eradicated. Again, it was observed that the theoretical PDFs provided an adequate fit to empirical PDFs with the exception of the dual- and four-base station SEC schemes at SNR levels below the switching threshold. Table IV provides a sample of the parameter estimates obtained for both dual- and four-base station SEC and SECps with a medium switching threshold
selected for scenario 2 to allow reader to reproduce the theoretical probability densities presented in Fig. 11.

## VI. Outage Probability

The OP is an important performance measure for wireless communication systems. It can be defined as the probability that the instantaneous SNR drops below a minimum threshold required to support acceptable performance, such that

$$
\begin{equation*}
P_{\mathrm{out}}=\operatorname{Pr}\left[\gamma \leq \gamma_{\text {Outage }}\right]=F_{\gamma}\left(\gamma_{\text {Outage }}\right) \tag{16}
\end{equation*}
$$

where $\gamma_{\text {Outage }}$ is the pre-determined SNR threshold. For the SSC, SEC and SECps schemes, the corresponding OP can be readily obtained by replacing $\gamma$ in (3), (7) and (12) with $\gamma_{\text {Outage }}$. As an example, Fig. 12 shows the OPs of the four-base station SEC and SECps schemes with group 3 for scenarios 3 and 5 when a medium switching threshold was adopted. For comparison, the OPs of four-base station PSC are also illustrated in Fig. 12. It is clear that the theoretical OPs provided a good fit to the empirical OPs for both the SEC and SECps schemes. Furthermore, it can be seen that the SECps scheme outperformed the SEC scheme for the lower outage threshold levels, particularly below the switching threshold $(30 \mathrm{~dB})$. Finally, it is also worth remarking that, similar to the results presented in Section IV, the four-base station SECps set-up provided almost the same performance as the four-base station PSC configuration.

## VII. CONCLUSION

The potential improvement in signal reliability for outdoor wearable communications at 868 MHz using macro-diversity arrangements based on dual-base station SSC, SEC and SECps


Fig. 11. Empirical (symbols) and theoretical (continuous lines) PDFs for scenario 2 for dual-base station configuration with group 2 (circle symbols) and four-base station configuration with group 4 (triangle symbols) for both (a) SEC and (b) SECps schemes with a medium switching threshold (30 dB).

TABLE IV
Parameter Estimates for Dual-Base Station SEC and SECps with Group 2 (Base Stations 5 and 10) and Four-Base Station SEC and SECps with Group 4 (Base stations 3, 5, 8, and 10) at the Medium Switching Threshold for Scenario 2.

|  | Dual-base Station |  |  |  |  |  |  | Four-base Station |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $m_{1}$ | $\overline{\gamma_{1}}$ | $m_{2}$ | $\overline{\gamma_{2}}$ | $m_{1}$ | $\overline{\gamma_{1}}$ | $m_{2}$ | $\overline{\gamma_{2}}$ | $m_{3}$ | $\overline{\gamma_{3}}$ | $m_{4}$ |  |
| SEC | 6.99 | 46.45 | 0.50 | 51.68 | 0.88 | 100.00 | 0.88 | 100.00 | 6.01 | 81.90 | 15.00 |  |
| SECps | 6.86 | 47.09 | 0.50 | 26.92 | 4.64 | 65.64 | 0.78 | 100.00 | 0.50 | 0.10 | 10.52 |  |

and four-base station SEC and SECps has been investigated. The benefit of having more than two signal base stations has been demonstrated by comparing the diversity gains between a range of dual- and four-base station configurations. It was found that for the scenarios considered here, switched diversity systems consisting of a four-base station configuration were less affected by the location of the base stations and thus provided a more stable performance (in terms of signal reliability). Among the three different switched diversity schemes, the SECps scheme provided the best performance for all scenarios and groupings. The results have shown that this type of switched diversity system can provide up to 19.5 dB diversity gain when using a four-base station arrangement. However, this improvement is not open-ended as it will add extra complexity to the design of the switched diversity system.

The impact of different switching thresholds on the diversity gain, the number of path examinations and the number of path switches of the various combiner outputs have been studied to emphasize the importance of selecting an appropriate switching threshold. It was observed that there exists an optimum switching threshold which maximizes the performance for this type of the wearable system. More specifically, at the optimum switching threshold, the switched diversity system can provide considerable performance with much fewer path examinations when compared to the PSC scheme. It was also found that while a four-base station switched diversity system provides higher diversity gain than a dual-base station switched diversity system, this comes at the cost of having a greater number of path examinations and switches. This result indicates that there exists a trade off between diversity gain (performance) and the number of path examinations and path
switches between base stations (energy consumption).
In direct contrast to this, an inappropriate switching threshold may cause not only the substandard performance of wearable systems but also greater energy consumption due to the unnecessary path examinations and needless path switches between base stations. In this case, no additional benefit is obtained using a switched combining based macro-diversity system. Consequently, the appropriate switching threshold must be carefully chosen so that the switched combining based macro-diversity system works as desired. In this study, each scenario was found to have a different optimum switching threshold. Nonetheless, among the three switching threshold levels which were considered, the medium switching threshold ( 30 dB ) was found to be quite close to the optimum switching threshold for all of the scenarios.

Finally, a statistical analysis of the switched diversity combiner output has been presented under the assumption of independent and non-identically distributed Nakagami- $m$ fading channels. Over all of the measurement scenarios considered in this study, the PDFs of the switched combiner including the SSC, SEC and SECps schemes have been shown to provide an adequate fit to the fading observed at the output of the virtual switched combiner. From the parameter estimates, it was found that each base station experienced non-identical Nakagami- $m$ fading. The parameter estimates also suggest that the fading conditions observed at each base station varied according to the user's movement.

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Fig. 12. Empirical and theoretical OPs for four-base station SEC and SECps with group 3 for scenarios 3 and 5 with a medium switching threshold ( 30 dB ) alongside the empirical OP for four-base station PSC. It is worth highlighting that the parameter estimates given in Table III are used for the theoretical OPs.

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[^1]:    ${ }^{1}$ For the case when $p$ is a Gaussian PDF with zero-mean and unit variance and $q$ is a Gaussian PDF with zero-mean and variance $\sigma^{2}$, we can have $\operatorname{KLD}(p, q)=0.5\left(\sigma^{-2}-1\right)+\ln (\sigma)$ and $\operatorname{KLD}(q, p)=0.5\left(\sigma^{2}-1\right)-$ $\ln (\sigma)$. By substituting these equations into (15), we can obtain as $\mathrm{RAD}=$ $\left(\frac{1}{0.5\left(\sigma^{-2}-1\right)+\ln (\sigma)}+\frac{1}{0.5\left(\sigma^{2}-1\right)-\ln (\sigma)}\right)^{-1}$.

