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Small strain behavior and crushability of Ballyconnelly carbonate sand under monotonic and cyclic loading

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ABSTRACT

In various parts of the globe, carbonate sands are found at shallow sea water depth. These types of sands are very susceptible to large scale particle breakage. Offshore structures like wind turbines and sea defences are constructed on these types of soils. From a design perspective, it is essential to assess the extent of particle breakage and the subsequent change in soil properties that occur under working load conditions. This paper presents the data obtained from a number of drained monotonic and cyclic triaxial tests on crushable carbonate sand ("Ballyconnelly sand") in conjunction with small strain shear stiffness (G_{max}) measurements using the bender element technique. The soils were allowed to shear under three different loading patterns in order to understand the factors influencing the breakage of particles.

The degree of crushing was quantified and analysed based on the total energy input. It was observed that, apart from applied stress, the total strain accumulation governs the amount of particle breakage. It was observed that G_{max} increased significantly under high stress ratio. G_{max} also increased noticeably during resting periods without any change in loading conditions as a result of creep, and subsequently during cyclic loading although at a reduced rate.

Key words: Carbonate sand, crushing, Ballyconnelly sand, stress path, stiffness and cyclic loading

INTRODUCTION

The mechanical behaviour of granular soils may be significantly affected by particle crushing. Soils that are more susceptible to crushing can range from skeletal carbonate sediments to highly weathered decomposed granite, mainly from coastal areas and offshore sea beds, and even recycled aggregates (Sivakumar *et.al.* 2003). Loose carbonate sands of biogenic origin tend to crush more easily and at relatively low pressures when compared to silica based sands, as their fragile shell particles fracture. When the soil is loaded, the fragile nature of the particles together with an initially loose state, results in a very high compressibility (Coop 1990). The engineering behaviour and properties of the carbonate sands have been examined in detail by a number of researchers (e.g. Houlsby et al. 1988; Golightly 1989; Coop 1990; Coop and Lee 1993; Yasufuku and Hyde 1995; Hyodo et al. 1998; Brandini and Coop 2001; Nakata et al. 2001; Coop et al. 2004; Tarantino and Hyde 2005; Leleu and Valdes 2007; Qadimi and Coop 2007; Donohue et al. 2009; Sadrekarimi and Olson 2010; López-Querol and Coop 2012; Miao and Airey 2013; Lui et al. 2016; Nardelli and Coop 2016).

The amount of particle breakage depends on several factors including stress level, particle grading, void ratio, size, shape, strength and mineral composition (Coop *et al.* 2004). In general, increases in particle size and angularity increases the amount of particle crushing (Lade et al. 1996; Vilhar et al 2013). Increases in stress levels in coarse grain soils enhance the chances of particle breakage but the amount of breakage also depends on the strain accumulation at that stress level, as particles may undergo significant amounts of rolling and sliding before crushing occurs.

Dynamic/cyclic loading of geotechnical structures may cause further particle crushing. Examples of cyclic loading on geotechnical structures include repeated axle loading of roads and railways (Vallejo *et. al.* 2006). Cyclic loading is also associated with offshore structures such as oil rigs and wind farms. This coincides with the work carried out by Cheng *et al.* (2001) and Vallejo *et al.* (2006) which showed that the force network through the particle contacts is not the same in every loading cycle. Particle crushing is therefore only associated with particles participating in the strongest force chains. Donohue *et al.* (2009), López-Querol and Coop (2012) and Lui et al. (2016) carried out studies on drained cyclic loading of carbonate sand. Donohue *et al.* (2009) observed that while particles may not be loaded to their full capacity in a given cycle, they could be crushed in subsequent cycles without any variation in the amplitude of cyclic loading. The above studies have focused mainly on cyclic loading at large strains; however for complex geotechnical design the behaviour of soils at small strains is often required.

This paper presents and discusses the data obtained from a series of drained triaxial tests on carbonate sand subjected to monotonic and cyclic loading in conjunction with small strain

measurements using bender elements. The amount of breakage that occurred was quantified in terms of a relative breakage factor proposed by Hardin (1984). The observed relative breakage factor further was analysed in terms of total input energy and mean effective stress.

METHODOLOGY

Characterisation of the material: For this study a crushable calcareous sand of biogenic origin was used. This sand, known locally as "Ballyconnelly sand" was collected from Clifden Bay, Connemarra in Ireland. The sand is whitish orange in colour with rounded grains and consists almost entirely of fragments of calcareous algae. The initial void ratio, e_0 of all tests carried out on Ballyconnelly sand was $0.68 \pm 5\%$. Physical characteristics of this material are: Sphericity 0.85; Roundness 0.8; CaCo₃ content $\approx 93\%$; Grain size D_{10} & D_{50} 1.0mm and 1.45mm; and Specific gravity (G_s) 1.72. For determining G_s, the procedure outlined in BS 812-2:1995, was adopted.

Sample preparation: The sand was initially soaked in water under vacuum for 1 hour prior to use. The samples were prepared using the procedure typically used for preparing sand samples for triaxial testing. A rubber membrane was secured on the pedestal and this was then surrounded by a split mould. A small amount of water was poured into the membrane and previously soaked sand was gently poured into the membrane. Membrane effects can cause errors in the volumetric strain measurements, particularly if the confining pressure was gradually increased. However, in all of the tests the confining pressure remained the same and therefore the effects are minimal. A gentle tap was applied to compact the sand in layers. Upon reaching the required height, the top cap was located and secured with "O" rings. As a single membrane punctured under higher loading in a trial test, an additional membrane was then carefully placed around the sample. A small amount of suction was applied in the drainage line prior to the removal of the split mould.

In order to measure the shear wave velocity (V_s) and the corresponding small strain shear stiffness during each test, the pedestal and the top cap were incorporated with bender elements, which are piezoelectric transducers capable of generating and detecting shear or compressional motion (Dyvik and Madshus 1985; Donohue *et al.* 2010; Blewett *et.al.* 2000; Kawaguchi *et al.* 2001; Bonal *et al.* 2012). A function generator and data logger, supplied by V J Tech, were used to generate and capture the transmitted and received signals respectively. In each test, the volume change, axial displacement and the deviator load were measured using standard devices.

Testing programme: The testing programme consisted of three stages: (A) monotonic loading until failure; (B) monotonic loading to a fraction of the anticipated failure load and subsequent cyclic

loading; and (C) monotonic and cyclic loading under various stress ratio μ (= q/p') values. All tests were conducted under drained conditions. The diameter and the height of the samples were 100mm and 200 mm respectively in the case of (A) and (B). The height of the sample was reduced to 100 mm in the stage (C) tests. In order to achieve a more reliable shear wave signal, the size of the samples were reduced in stage (C) to accommodate the bender elements, as a sample of 200mm height produced more scattering of the output signal. The samples were saturated using a back pressure and ensuring a pore water pressure parameter B value of at least 0.95. Table 1 includes details of the various tests carried out. In Stage A, four samples were subjected to effective consolidation pressures of 100kPa, 250kPa, 500kPa and 1050kPa. The samples were then sheared under drained conditions. Particle size analyses were carried out on the raw and tested samples. In Stage B, six tests were carried out in which the samples were loaded to one third or two thirds of the anticipated failure load based on samples initially consolidated to 100 kPa, 250 kPa and 500 kPa of mean effective stress. The samples were then subjected to cyclic loading of up to 1000 cycles. The cyclic loading amplitudes Δq (triangular wave form) were ±20kPa and 40kPa for samples consolidated to 100 kPa; ±40kPa and 80kPa for samples consolidated to 250 kPa; ±80kPa and 160kPa for samples consolidated to 500 kPa. Based on the triangular waveform, pressure was increased (and reduced) at a rate 50 kPa per minute.

In Stage C of the testing programme, five tests were carried out at various values of μ (=0, 0.25, 0.5, 1 and 1.25), as shown in Figure 1. In the case of μ >0, the samples were initially subjected to an effective consolidation pressure of 250 kPa under isotopic stress conditions (Point A in Figure 1) and then an axial load was applied to meet the required value of μ . The samples were then taken along the μ line (for example B^{μ =1} in the case of μ = 1.0) and the shear wave velocity was measured at four different stress states as illustrated in Figure 1 (C^{μ =1}, D^{μ =1} and E^{μ =1}). In the present investigation the shear wave velocity was consistently determined based on the peak-to-peak travel time, although this duration was very similar to the wave travel time based on the first arrival. A relatively high frequency (20kHz) sine pulse was adopted throughout in order to reduce the near field effects (Bonal et al 2012). All received signals were averaged 20 times in order to reduce noise. The shear modulus, G_{max} , was subsequently determined using the following equation:

 $G_{max} = \rho V_s^2$

(1)

where ρ is bulk density (kg/m³) and V_s is the shear wave velocity (m/s). It should be pointed out that G_{max} is influenced by a range of parameters, the most important of which are void ratio, e, and mean effective stress, σ' (Hardin and Dnervich 1972).

Upon reaching the maximum loading the samples were allowed to rest for 24 hours prior to cyclic loading. The amplitude of the cyclic loading was ± 100 kPa. In order to assess the effect of cyclic loading on particle size, a particle size analysis was also carried out at the end of each test (Figure 2). It should be pointed out that the sample tested under $\mu = 0$ did not undergo cyclic loading or shearing, and the relevant particle breakage is very marginal (Figure 2).

RESULTS AND DISCUSSION

Stage A, Monotonic loading: Figure 3 shows the responses of the samples subjected to monotonic loading under various initial effective consolidation pressures. The sample subjected to 100 kPa of initial consolidation pressure showed a prominent peak and then reached an assumed critical state at an axial strain of 20%. During this process the sample initially contracted and subsequently dilated by about 5.5%. The sample consolidated to 250 kPa also showed a marginal peak and a small amount of dilation (about 0.5%). There is no evidence of peak state in either of the samples consolidated to 500 kPa and 1050 kPa. This indicates simultaneous dilation and breakage of particles. In both cases the samples contracted significantly and the relevant magnitudes of contractions are 7% and 14% respectively for samples consolidated to 500 kPa and 1050 kPa (Fig 3b). A marginal volume change still continuing even after a vertical strain of about 20%. The failure envelope based on the ultimate state or assumed critical state is shown Figure 3c. Representing crushable soils under critical state framework is still difficult as uncertainty prevails for coarse grain soils to achieve constant volume change under all loading conditions. Experimental observations suggest critical state may be achieved by coarse grain soil either at very low stress (small amounts of particle breakage) or at very high stress (where complete breakage has occurred) (Ghafghazi et al. 2014; Lade and Yamamuro 1996; Russel and Khalili 2004). As shown in Fig. 3c, the assumed critical state line can be drawn by using test results under initial consolidation pressures of 100, 250 and 500 kPa as no volume change was noticed at the end of the tests. The result from the 1050 kPa test falls below this critical state line. Similar observation was reported by Ghafghazi et al. (2014) where the critical state line moves downward with particle breakage. It is clear from Fig. 3(c) that the assumed critical state line is not in fact linear (though the same could be expected for other types of granular material), and it may be affected by the intense crushing during shearing, altering the particle size distribution at each stress level. The angle of internal friction at low consolidation pressure is about 38° and it reduces to 35° at high pressures. The intense contraction observed during shearing is largely due to particle crushing and the particle size analysis carried out on the tested material, shown in Figure 3d, confirms this. The process of particle crushing produced more

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fine material, as the consolidation pressure increased from 100kPa to 1050kPa. The particle sizes retained 10% and 30% (D_{10} and D_{30}) of the original material were 1mm and 0.7mm, respectively, and they reduced to 0.7mm and 0.3mm when sheared under 1050 kPa of consolidation pressure.

Stage B, Cyclic loading: Figure 4 shows the responses of the samples subjected to cyclic loading. Six samples were tested under drained conditions (two samples each at initial consolidation pressures of 100 kPa, 250 kPa and 500 kPa). In the first set of tests, the samples were initially taken to one third of the peak load as identified from the monotonic tests (Figure 4). In the second set of tests, the samples were taken to two thirds of the peak load. The amplitudes of cyclic loading noted earlier are approximately 5 and 10% of the peak deviator stress identified from monotonic tests. The volumetric strain shown in Figure 4 is solely due to the cyclic loading, excluding the volumetric strain experienced by the sample leading up to the target deviator stress at which the cyclic loading began. The amplitude of the cyclic loading is indicated in the relevant figures. At a compression pressure of 250 kPa, the sample began to dilate after about 1000 loading cycles. It should also be noted that the recoverable strain in each loading cycle (indicated by the bandwidth) is highly variable. This is likely due to differences in loading amplitudes in each cycle although it could also indicate that the particle-particle loading is not necessarily the same in each loading cycle. This was also discussed by Donohue et al. (2009) and O'Neill (2005), who observed, through discrete element simulations that when loaded, the force network in granular soils is highly heterogeneous and that different particles experience the largest forces from cycle to cycle. It has been suggested that degradation in the form of breakdown of asperities and particle crushing is associated with particles participating in the strongest force chains (McDowell et al., 1996; Cheng et al., 2001; Vallejo et al., 2006; Donohue et al. 2009). If these force chains are not static, as shown by O'Neill (2005), then additional damage to the material should occur in each cycle.

The particle size analysis carried out on the tested material also indicated a small amount of crushing with increasing consolidation pressure and loading amplitude. The relative breakage factor Br (discussed further later) at 500kPa and $\pm q = 160$ kPa is 0.02. Similar observations were also reported by Querol and Coop (2012).

The development of shear strain with the cyclic loading could provide further insight into the particle crushing and reorientation etc. Figure 5 shows the shear strain developed during cyclic loading under the three consolidation pressures. There is clear evidence that the permanent shear strain begin to develop rapidly after a certain number of loading cycles. The most obvious case being, the sample subjected to 500 kPa of initial consolidation pressure (Figure 5c) which was subjected to two loading amplitudes: $\Delta q = \pm 80$ kPa and ± 160 kPa. Under a loading amplitude of ± 80 kPa, the plastic strain becomes noticeable after 200 loading cycles and reduced to 10 cycles when the loading amplitude was ±160 kPa. This "threshold" shear strain, where the rate of plastic strain increases appears to be affected by various factors including the loading amplitude and initial consolidation. In the case of the sample subjected to 100 kPa of initial consolidation pressure, the number of loading cycles required to initiate a significant shear strain is between 8-20 for both loading amplitudes, and, as expected, the threshold shear strains are larger for the higher value of Δq . In the case of the test with initial consolidation pressure of 250 kPa (Figure 5b), the number of loading cycles required to initiate a significant shear strain is generally similar to that of the sample subjected to 500 kPa. The threshold shear strains are, however, different (even though the $\Delta q/p'_0$ ratio's are directly comparable), with higher threshold strains measured at higher consolidation pressures. It is plausible that as the samples subjected to higher consolidation pressures would have tighter grain packing and be less prone to dilation (which can lead to an increase in volume in noncrushable soils), but such response in crushable soils may contribute to additional crushing. It should also be noted that although the number of loading cycles required to initiate rapid plastic shear strain is high under significant consolidation pressures, the rate of plastic shear strain, when expressed in terms of log cycle, is much higher. For example the rate of plastic shear strain for 1 log cycle is approximately 0.17 for $\Delta q = \pm 80$ kPa (250 kPa of consolidation pressure). Under the same amplitude of loading, the rate of plastic shear strain is 0.25 when the sample was subjected to 500 kPa of consolidation pressure.

Stage C, Cyclic loading and small strain behaviour: In this stage of testing, samples were taken through stress paths with various μ values. The initial dimensions of the samples together with the volume changes during loading were used to determine the bulk density at a given stress state. Figure 6 shows the deviator stress plotted against axial strain for various values of μ in which a maximum of 9% axial strain took place at μ =1.25 under the largest loading applied. The shear wave velocity was calculated at each stress state, corresponding to effective consolidation pressure (i.e. effective cell pressure) of 250 kPa, 500 kPa, 750 kPa and 1000 kPa. The bender tip-tip distance was corrected for the relevant axial compression of the sample. Figure 7a shows the relationship between G_{max} and the effective consolidation pressure. G_{max} is also plotted against p' (mean effective stress) in Figure 7b. As shown, G_{max} increases with the effective consolidation pressure (or mean effective stress), However the G_{max} -p' line at $\mu = 0.25$ falls slightly below the $\mu = 0$ line before regaining stiffness at approximately $\mu = 0.5$. The relationship between the shear modulus and the Page 9 of 28

consolidation pressure is approximately the same at μ of zero and 0.5. Further increases in μ resulted in significant increases in G_{max} . The angle of internal friction of the material varied from 35° to 38° and, based on the average angle of internal friction, the value of K_o (coefficient of earth pressure at rest) is about 0.45. This K_o value corresponds to a μ value of 0.55. It is possible that G_{max} reduces with increasing μ in the passive state (i.e. $\mu < \mu_{Ko}$) and increases with increasing μ in the passive state (i.e. $\mu < \mu_{Ko}$) and densification under active loading.

Upon reaching the maximum loading (at each μ value), the sample was allowed to rest until it stabilised its vertical and volumetric strain. Observations have shown that stabilisation occurred within a period of 24 hours. The relevant axial strain of the sample with time is shown in Figure 8a. The samples underwent significant axial compression and the magnitude of axial strain increased with the μ value. A maximum axial strain of 1.1% at a μ value of 1.25 was observed. This is significant as it has taken place during a resting period without any change in loading conditions. Particle breakage showed time dependant behaviour; similar behaviour was also reported by Yamamuro and Lade (1993), where particle breakage continued with time at a reducing rate, and by McDowell and Khan (2003) who suggested that creep of granular materials is accompanied by particle crushing. The axial strain during cyclic loading is shown in Figure 8b. The loading amplitude, Δq , was ±100 kPa in all four tests. In the case of $\mu = 1$, the cyclic loading was stopped temporarily for 12 hours (unintentionally) and during this additional resting period the sample continued to experience axial straining.

Figure 9 (a) shows G_{max}/G_i plotted against time (i.e. during the resting period), where G_i is the initial small strain shear stiffness (immediately prior to application of prerequisite load as shown in Fig.1) and G_{max} is the small strain shear stiffness measured at each time interval during the resting period. Figure 9(b) shows G_{max}/G_i plotted against number of cycles. Where, G_i is the initial stiffness immediately before application of cyclic loading and G_{max} is the stiffness after application of cyclic loading. An increase of about 6 to 10% in G_{max} can be seen at the end of the resting period. The increase in G_{max} as a result of cyclic loading was less than that observed during the resting period (only 2 to 5 % increase in G_{max}). It is suggested that the increase in G_{max} during both periods is associated with (a) an increase in density of the sample (Equation 1) and (b) a greater number of particle to particle contacts following particle crushing.

Particle size analysis was also carried out on the test material and is shown in Figure 2. The degree of particle crushing was significant at higher values of μ . The authors accept that some of this particle crushing may have been taken place during compression, however this aspect is minimal, as

shown in Figure 2. The sample tested under $\mu = 0$ did not undergo cyclic loading and the relevant particle breakage is marginal.

The tests conducted in this investigation to study the crushability of Ballyconnelly carbonate sand has been summarised in $e - \log p$, plane as shown in Figure 10. The line ABB*C represents the assumed critical state line obtained from Stage A testing. Line ABB* signifies the zone of small particle breakage, together with sliding/rolling actions, whereas line B*C signifies a very high degree of particle breakage together with sliding/rolling. Any stress conditions moving towards line B*C produced more particle breakage. For the Stage C tests, the results are also plotted on the same figure at different stress ratios (Figure 10), including for the resting period and cyclic loading. $\mu = 0$ represents the normal compression line (NCL). As μ increases, the state of the soil moves more towards the line B*C and produces higher particle breakage. Resting time may increase particle breakage by a small amount. The stress range for severe particle crushing found in this investigation is 600 to 2000 kPa, similar to the "breakage threshold" observed by Ghafghazi et al. 2014.

Particle breakage factors: In order to quantify the amount of particle breakage, various particle brakeage factors have been proposed using sieve analysis results (Marsal 1967; Lee and Farhoomand 1967; Hardin 1985; Lade et al. 1996). Marsal (1967) proposed a breakage index which depends on the difference in the percentage retained in each sieve between initial (without any load) and final (after shearing) grain size distribution. Lee and Farhoomand (1967) adopted the change in D₁₅ on the grain size curve to quantify particle breakage. Their main focus was to address the crushing of filter material in earth dams. Lade et al. (1996) proposed a particle breakage factor (B₁₀) which is defined as:

$$B_{10} = 1 - \frac{D_{10f}}{D_{10i}} \tag{2}$$

where D_{10f} is the effective grain size of final gradation and D_{10i} is the effective grain size of initial gradation. Lade et al. (1996) argued that grain size cannot be used to express the shear strength of soil but can effectively be used to express the soil permeability and therefore, using D₁₀ to describe the particle breakage, have some meaningful use. Hardin (1985) used three parameters to describe the particle brakeage: B_t , B_p and B_r , where B_t is the total breakage, B_p is the breakage potential and B_r is the relative breakage. B_t can be defined as the area between the initial and final grain size curve whereas B_p is the area between original grain size curve and particle size greater than 0.074mm. The relative breakage (B_r) is the ratio between the total breakage and the breakage potential.

$$B_r = \frac{B_t}{B_p} \tag{3}$$

The use of the relative breakage factor is limited to the particle size of 0.074mm (i.e not applicable to silt), Hardin (1985). Usually B_r has been preferred to represent the particle breakage as it covers the entire particles distribution curve which makes this method robust and stable (Coop and Lee 1993; Vilhar et al. 2013; Lade et al. 1996; Qadimi and Coop 2007; Querol and Coop 2012).

Lade et al. 1996 suggest that total energy input should be used to express relative breakage instead of effective mean normal stress. Crushing primarily depends on the amount of energy actually absorbed by the soil specimen. Another advantage of this approach is that it links both stress and strain to particle breakage. Lade et al. 1996 proposed that, during a drained shearing the total input energy is:

$$E_T = \sum_{SOT}^{BOS} \bar{\sigma}_c \dot{\varepsilon}_v + \left[\sum_{BOS}^{EOS} (\sigma_1 - \sigma_3) \dot{\varepsilon}_a + \sum_{BOS}^{EOS} \bar{\sigma}_c \dot{\varepsilon}_v \right]$$
(4)

where $\bar{\sigma}_c$ = average confining pressure; $\dot{\varepsilon}_v$ = corresponding volumetric strain increment; $\sigma_1 - \sigma_3$ = average stress difference; $\dot{\varepsilon}_a$ = axial strain increment; *SOT*= start of test; *BOS*= beginning of shearing; *EOS* = end of Shearing.

Figure 11 (a) represents the variation in particle breakage in terms of relative breakage with mean effective stress for Stage A and Stage C loading. The mean effective stress is based on the assumed critical state for Stage A testing and the corresponding value for Stage C testing was based on the stress conditions at the end of cyclic loading. The figure also includes the observations reported by Coop and Lee (1993) on Dogs Bay. In Stage A, the sample sheared in axial compression whereas Stage C sheared while maintaining equal stress ratio as shown in Figure 1. At a given mean effective stress Stage A produced more particle breakage compared to Stage C. The difference may be due to the difference in the accumulated strain, as Stage C testing produced less strain compare to Stage A. Thus the above observations underline the fact that the study of particle breakage using mean effective stress alone, ignoring strain accumulation may give a misleading intensity of breakage. The difference in particle breakage between Stage A and Stage C reduced with increase in mean effective stress. The particle breakage increased with the stress ratio which signifies the importance of deviator stress g and accumulation of vertical strain. In comparison to Dogs Bay Sand, Ballyconnelly Sand produced more breakage at a given mean effective stress (Figure 11). The higher crushability of Ballyconnelly sand may be due to its larger particle size than that of Dogs Bay Sand. Coop 1990 reported D₅₀ and D₁₀ for Dogs Bay Sand are 0.2 and 0.15 respectively. McDowell and Bolton (1998), reported that a significant reduction in tensile strength of the particles with increasing particle size of various crushable soils.

The energy approach given in Equation (4) is applied to Stage A and Stage C testing. The strain up to which particle breakage occurs should be considered for this particular analysis. From Figure 3 (a) it can be seen that peak deviator stress was reached at about 2.5 and 6 % of axial strain for p'₀ of 100 and 250 kPa initial consolidation pressure respectively. After passing the peak and moving towards the softening stage, this reduces the chance of crushing of particles but increases the likelihood of particle slip/roll occurring. Taking into account the flat peak q-axial strain relationship, for Stage A and p'_0 of 100 and 250 kPa, an energy calculation was done up to vertical strains of 12 and 17 % respectively. Figure 11(b) shows the relationship between B_r and the energy input calculated using Equation (4). There is a clear trend of increase in particle breakage with the total energy exhibited in both types of loading. A similar trend was also observed by Lade et al. (1996) from high pressure drain triaxial compression tests). Contrary to Fig 11 (a), Stage C loading produced slightly more particle breakage compared to Stage A loading at a given energy level. This may be due to the presence of higher effective mean stress at the same energy level and the smaller height of sample used in Stage C loading. The rigid boundary conditions (ie. the top cap and the pedestal) in triaxial testing will restrict the dilatancy of granular soil. Such boundary conditions may lead to higher level of particle breakage close to the rigid interface. If this is the case then the overall quantity of particle breakage in longer samples would be less than shorter sample for a given diameter. The approaches discussed above to describe particle breakage have advantages as well as disadvantages, but the total energy method may be considered an advancement on other methods as it includes volumetric and axial strain, which can be included conveniently into the constitutive behaviour of crushable course grain soils.

CONCLUSIONS

A number of drained monotonic and cyclic triaxial tests were carried out on crushable calcareous sand in conjunction with small strain stiffness measurements using bender elements. The degree of crushing was quantified using particle size analysis. The particle breakage observed during the investigation was quantified by using the relative breakage parameter, B_r. It was observed that intense contraction observed during monotonic loading was largely thought to be due to particle crushing, which was also more apparent at higher consolidation pressures. Overall, it appears that the degree of particle crushing was dependent on the effective confining pressure, deviator stress, the amplitude of cyclic loading and the accumulation of strains. Particle breakage usually increases with increases in these stresses and strain. Evidence was also presented that indicates the permanent shear strain develops rapidly after a certain number of loading cycles. In comparison to

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the well characterised Dogs Bay Sand, Ballyconnelly Sand produced more breakage at a given mean effective stress. The higher crushability of Ballyconnelly sand may be due to its higher particle size than that of Dogs Bay Sand.

Small strain shear stiffness (G_{max}) was observed to increase as a result of both creep and cyclic loading. This increase is associated with (a) an increase in density of the sample and (b) a greater number of particle to particle contacts following particle crushing. G_{max} also reduced initially with increasing stress ratio $q/p'(\mu)$, but increased significantly under high stress ratios, representing lateral expanding conditions. The condition of rest under constant stress resulted in a noticeable increase in the shear modulus (particularly at higher pressures), as the particles continued to crush. The corresponding effect under cyclic loading was less significant.

The total energy approach to express the relative breakage appears to be more reliable to understand the intensity of particle breakage as it includes volumetric and axial strain, which can be included conveniently into the constitutive behaviour of crushable course grain soils. A small contribution to particle breakage of Ballyconnelly sand was observed due to cyclic loading and creep action.

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Figure Captions

Figure 1. Stress paths during bender element tests

Figure 2. Particle size distribution of samples subjected to loading around stress ratio line (Stage C loading)

Figure 3. Stress-strain behaviour, failure state and particle crushing (Stage A loading)

Figure 4. Volumetric strain of samples subjected to cyclic loading (Stage B loading)

Figure 5. Shear strain of samples subjected to cyclic loading (Stage B loading)

Figure 6. Axial strain during loading along different stress ratio (Stage C loading)

Figure 7. Shear modulus along stress ratio line plotted against mean effective stress

Figure 8. Axial strain during (a) resting period and (b) cyclic loading

Figure 9. Shear modulus during resting period and cyclic loading

Figure 10. Pressure-volume relationship.

Figure 11. (a) Variation of B_r with effective mean stress, (b) Variation of B_r with total energy input.

Table-1

Test ID	Test type	Test description	Effective consolidation pressure (kPa)	Length of sample (mm)	Diameter of sample (mm)	Stress ratio μ	Cyclic load amplitude ± q (kPa)
A1	A	Monotonic loading	100	200	100	-	-
A2		until failure	250	200	100	-	-
A3			500	200	100	-	-
A4			1050	200	100	-	-
B5	В	Monotonic loading	100	200	100	-	20
B6		to a fraction of the	250	200	100	-	40
B7		anticipated failure	500	200	100	-	80
B8		load and	100	200	100	-	40
B9		subsequent cyclic	250	200	100	-	80
B10		loading	500	200	100	-	160
C11			250	100	100	0.00	100
C12	С	Monotonic and	250	100	100	0.25	100
C13		cyclic loading under	250	100	100	0.5	100
C14		various stress ratio	250	100	100	1.00	100
C15		μ	250	100	100	1.25	100

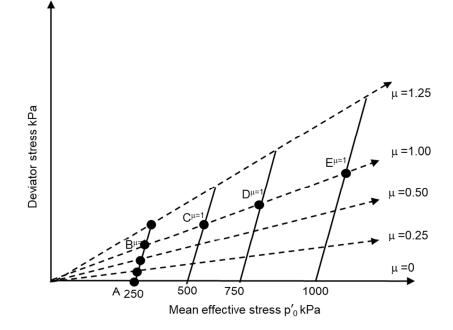


Figure 1 Stress paths during bender element tests



279x230mm (96 x 96 DPI)

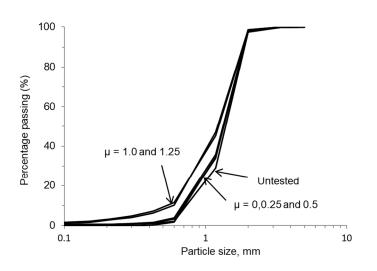


Figure 2 Particle size distribution of samples subjected to loading along stress ratio line (Stage C loading)



354x265mm (96 x 96 DPI)

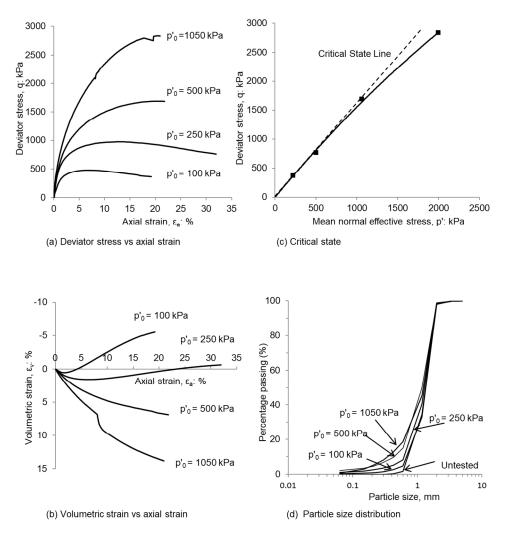


Figure 3 Stress-strain behaviour, failure state and particle crushing (Stage A loading)

Figure 3

396x455mm (96 x 96 DPI)

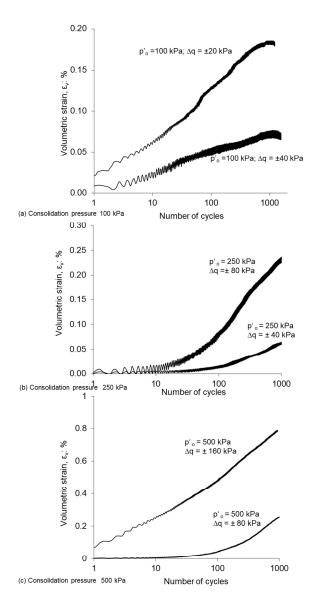
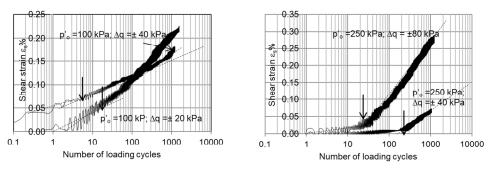


Figure 4 Volumetric strain of samples subjected to cyclic loading (Stage B loading)

Figure 4

345x524mm (96 x 96 DPI)



(a) Consolidation pressure 100 kPa

(b) Consolidation pressure 250 kPa

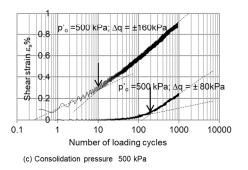
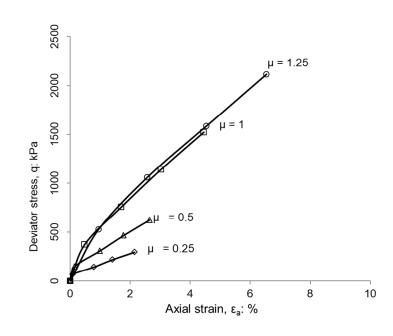


Figure 5 Shear strain of samples subjected to cyclic loading (Stage B loading)

Figure 5

380x339mm (96 x 96 DPI)



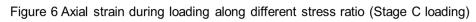


Figure 6 335x243mm (96 x 96 DPI)

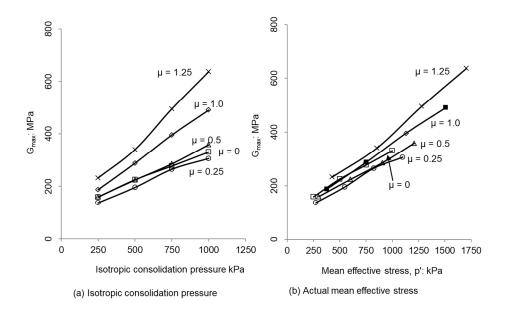
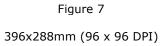


Figure 7 Shear modulus along stress ratio line plotted against mean effective stress



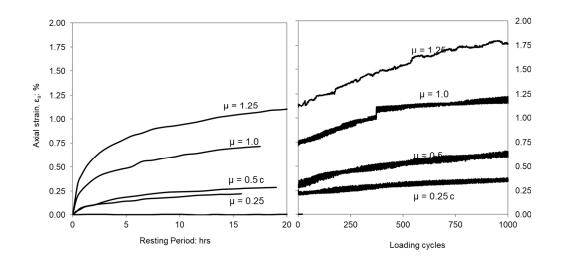
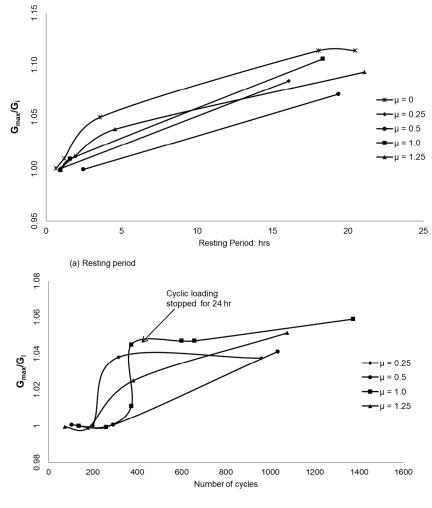


Figure 8 Axial strain during (a) resting period and (b) cyclic loading



396x250mm (96 x 96 DPI)



(b) Cyclic loading

Figure 9 Shear modulus during resting period and cyclic loading

Figure 9

396x529mm (96 x 96 DPI)

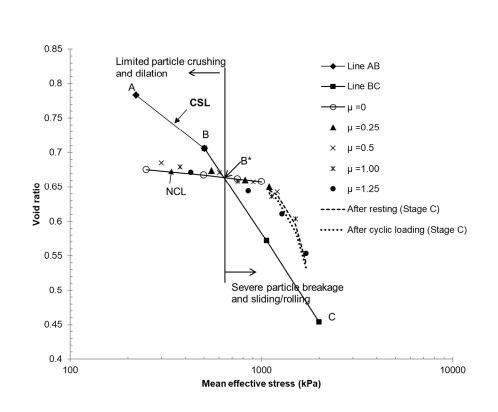


Figure 10 Pressure-volume relationship

Figure 10

396x340mm (96 x 96 DPI)

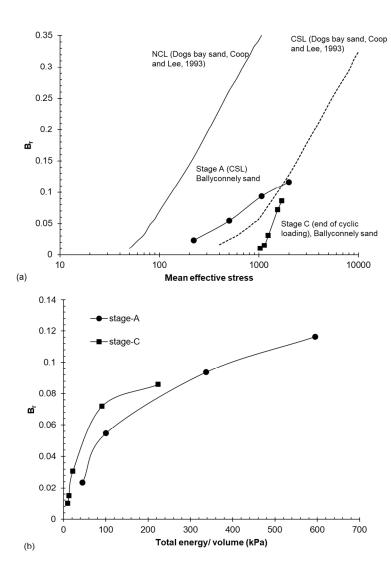


Figure 11 (a) Variation of B_r with effective mean stress (b)) variation of B_r with total energy input.

Figure 11

356x500mm (96 x 96 DPI)