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Strength development of GGBS and fly ash concretes and applicability of fib model code's maturity function – a critical review

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Abstract

This paper is the joint work of working group 4 of the RILEM TC 238-SCM and the fib Task Group 4.6. It was the aim of this literature study to quantify the effect of ground granulated blast furnace slag (GGBS) and silicious fly ash (sFA) on strength development of concrete. For the strength development the approach of the *fib* Model Code was chosen, which is based on an e-function that can be adapted to the strength development of an individual binder by selecting the so-called s-value based on the strength class of the Portland cement used. No guidance is provided for s-values for supplementary cementitious materials (SCMs). In order to determine the s-values for mixes with SCMs, a database was set up with results of material testing from literature. A relationship between s-values and w/b plus SCM/b ratios has been determined. This has been tested on laboratory cast specimens with 50 and 30 % cement replacement with GGBS and FA respectively. These were cured at 20°C. The s-values from this relationship were compared to those obtained from regression analysis and they were found to be satisfactory. This increased confidence in their use for predicting the strength development of other curing regimes, i.e. adiabatically cured concrete cubes, using the maturity function in the *fib* Model Code. Predictions of the effect of curing temperature, i.e. the adiabatic temperature history, on the strength development were again satisfactory. These were not significantly affected by the fib model code's use of one value of "apparent" activation energy.

Key words: strength development, maturity, fly ash, ground granulated blast furnace slag

1 Introduction

There has been a significant change in the types of cements used in the last decade. Whilst before the norm was a neat Portland cement, nowadays referred to as CEM I, environmental considerations, i.e. carbon footprint, has led to CEM II and CEM III cements becoming popular. Many of these cements contain fly ash (FA) or ground granulated blast-furnace slag (GGBS) which alter the compressive strength-time relationship. The designers usually use the 28-day characteristic compressive strength for structural calculations. Whilst SCMs may be used to design concretes of equivalent 28-day strength as neat Portland cement (CEM I) their early age strength development is not only significantly different but it is also affected to a greater extent by curing temperature.

High early age strength, e.g. 15 N/mm^2 at 16 hours, are needed by precast concrete factories for lifting operations in order to maintain their daily production of structural and non-structural elements. The factors affecting strength at early ages must therefore be considered. These factors include the composition of the concrete mixture, such as cement type and SCM addition and the use of retarding or accelerating admixtures. The strength development of the concrete is also influenced by temperature. Strength gain is more rapid at higher temperatures and slower at lower temperatures and if the temperature is too low then strength gain will cease altogether.

The need to understand and quantify the effect of temperature on the early age strength development of concrete mixes has been recognised for a long time. This was mainly for:

- (a) determining elevated curing temperature needed to achieve the required early strengths for safely lifting precast concrete elements as early as sixteen hours after casting [1] and
- (b) predicting the in-situ strengths especially during cold weather concreting, to allow stripping of formwork and removal of props without a collapse like the one that occurred in Willow Island in 1978 which resulted in 51 deaths [2, 3].

This can be achieved with maturity methods which account for the combined effect of binder composition and temperature on the strength development of concrete [4 - 9].

2 Strength development

2.1 General

The replacement of Portland cement by GGBS or fly ash usually results in a reduced early strength, often coupled with an increase in late strength. According to the fib Model code [10] the strength of concrete at a certain point in time can be calculated from the strength at 28 days according to the following equation:

$$f_{cm}(t) = \beta_{cc}(t) \cdot f_{cm,28d} \quad \text{with} \quad \beta_{cc}(t) = e^{s \cdot (1 - \sqrt{\frac{28d}{t}})} \quad (1)$$

where

$f_{cm}(t)$ is the mean compressive strength in N/mm² at an age t in days,

$f_{cm,28d}$ is the average compressive strength in N/mm² at an age of 28 days,

$\beta_{cc}(t)$ is a function to describe the strength development with time,

t is the concrete age in days,

s is a coefficient, which depends on the strength class of the cement.

The model code gives the following benchmarks for the different strength classes defined in the European standard EN 197-1:

32.5 N: $s = 0.38$

32.5 R and 42.5 N: $s = 0.25$

42.5 R, 52.5 N and 52.5 R: $s = 0.20$

These values are valid for 20°C and water storage.

For concretes with high GGBS or fly ash contents strength development is slower, which leads to higher s -values. In order to quantify that effect, data on strength development of concretes with GGBS and/or fly ash were collected from research reports and literature [11 - 78] and internal reports of material testing at the Institute of Building Materials Research, RWTH Aachen University, (ibac) [65]. For comparison concretes with CEM I of different strength classes were also included in this study. The compressive strength of each concrete

was tested at least at three points in time, always including 28 days. The average number of testing ages was 4.5. The s -value of every binder was fitted using equation (1). Since all experimental data show some scatter, the measured 28 day strength was not taken as a fixed value. Instead a fitting was carried out, allowing a variation of the 28 d strength in the range of \pm half a strength class compared to the measured value in order to get the most appropriate s -value for the strength development. Fig. 1 shows two examples of the fitting, a typical and a bad example. The bad example shows that in a few cases the experimental data could not be described adequately with equation (1). 18 out of 1017 data sets were not considered, because the average discrepancy between measured and calculated strength was more than 2.0 N/mm². Results for very early ages (< 24 h) should not be considered in the fitting of the s -value because high discrepancies at later ages were found in this study. That means on the other hand that the strength at $t < 24$ h cannot be predicted by equation (1).

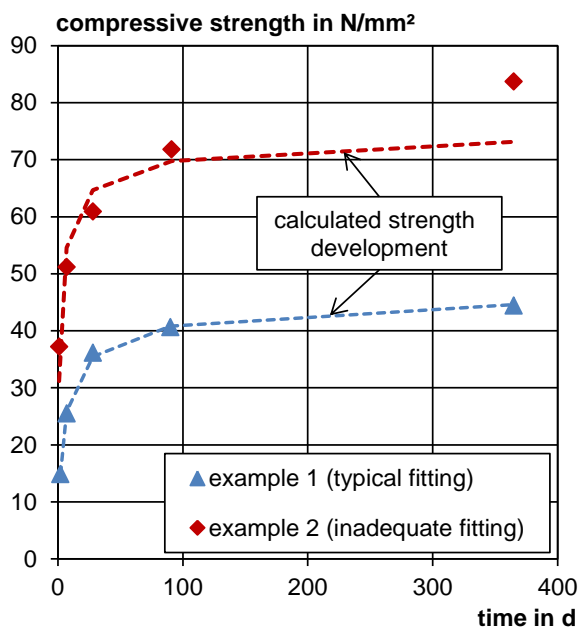


Fig. 1: Fitting of experimental data on strength development (example 1: B13, [25], example 2: no. 12, [15]); dots: experimental data, dotted lines: fitted curves

The database includes only concrete samples with a minimum dimension of 100 mm. The curing temperature was 20 ± 3 °C. The humidity storage conditions of the samples varied. Some samples were stored under water or in a fog room and others were stored under water for 7 days and at 65 % relative humidity afterwards. An overview of the available data is given in the Annex, Table A 1 to Table A 4. The tables give information on binder composition, strength class of the cement, the water/cement ratios (w/c) and the storage conditions.

Quite often the strength class of the cements is not specified in non-European literature, but in many cases results of mortar compressive strength tested according to ASTM C 109 are included in the papers. These results were used to classify the cements according to EN 197-1 (assuming a size factor of $f_{cm,51mm} / f_{cm,40mm} = 0.95$). Most of these cements were assigned to strength class 32.5 R or 42.5 N.

2.2 Influence of curing conditions, binder composition and w/b ratio

As mentioned above all concretes were cured at $20 \pm 3 \text{ }^\circ\text{C}$ but at different humidity conditions. The humidity may influence the subsequent hardening of concrete. Exemplarily Fig. 2 shows the s-values of concretes with different binders and similar w/b-ratios prepared with cements of strength class 32.5 R. The s-values show a large scatter, but nevertheless it can be seen that there is no systematic difference between 7 days of curing and water storage. There are a few results with only one or two days of curing in the data base and they show lower s-values indicating that the hydration of the cement is affected and the subsequent hardening is lower. Fig. 2 shows that for concrete samples with a minimum sample size of 100 mm 7 days of curing are sufficient to reach good subsequent hardening. For the further evaluation of the data no distinction was made between the curing conditions C7, W and FR.

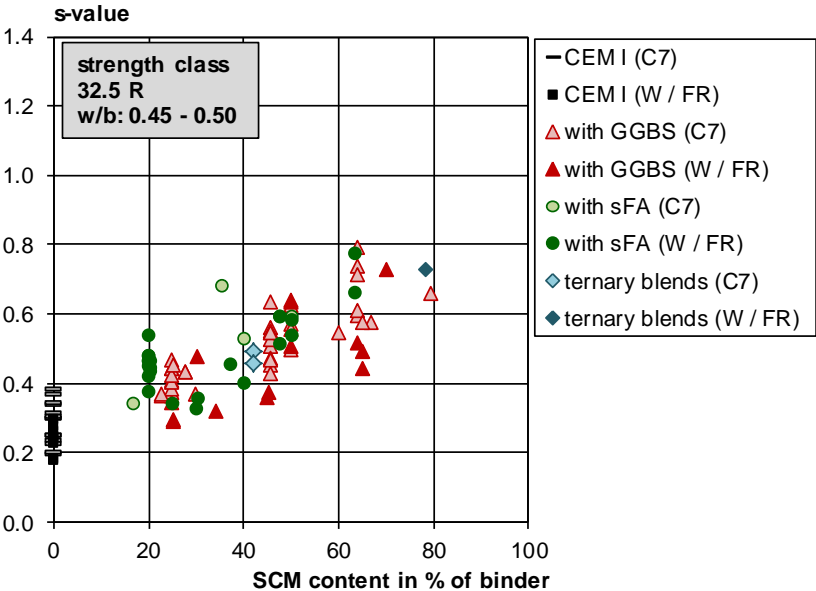


Fig. 2: Influence of curing conditions on the s-values of concretes with different binders (C7: 7 days of water curing and storage at 65 % r. h. afterwards, W: water storage, FR: fog room); data from [16, 17, 20, 21, 24 - 26, 30, 31, 45, 46, 47 - 49, 52, 55, 64, 65, 78]

Fig. 2 shows that s-values increase with increasing SCM content of the binder.

The influence of the strength class of the cement is shown in Fig. 3 exemplarily for Portland cement concrete and concrete with GGBS in a w/b range of 0.45 to 0.50. Cements with higher strength classes tend to show lower s-values as it was expected from [10]. For strength class 32.5 N there was only data available for CEM III and CEM II/B-S. The figure shows that the s-values of concretes with strength class 32.5 N cements do not exceed the values of class 32.5 R. Therefore it was decided to generate only two groups of strength classes:

- 32.5 N, 32.5 R and 42.5 N
- 42.5 R, 52.5 N and 52.5 R

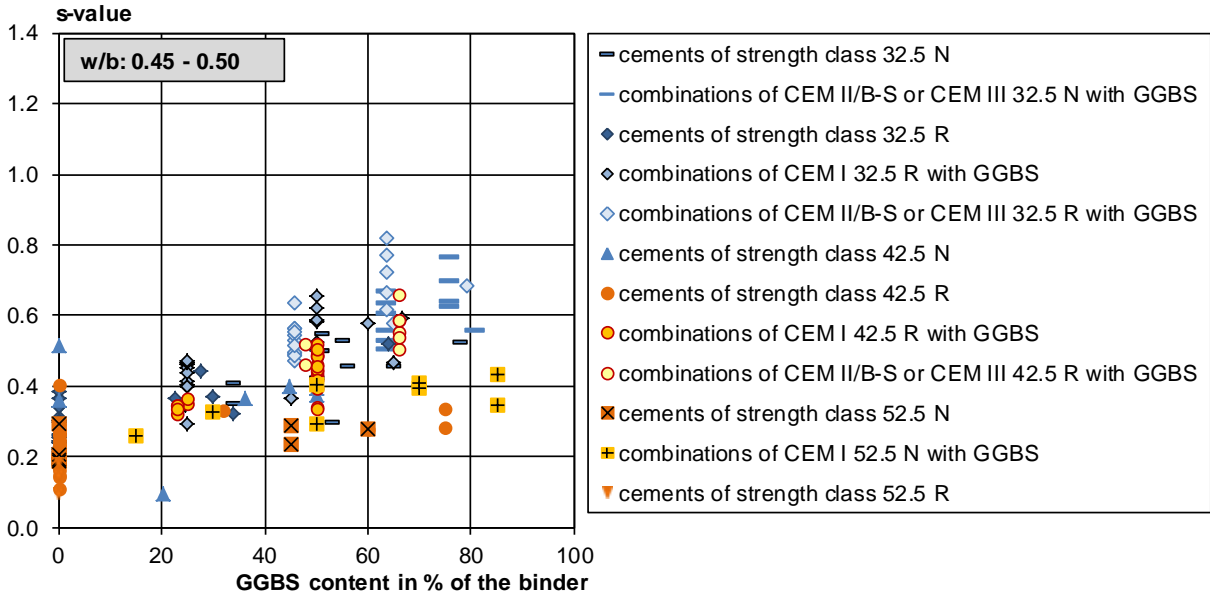


Fig. 3: Influence of the strength class of the cement on the s-values of concrete; data from [17, 21, 24 - 26, 41, 65, 78]

The influence of the type of binder is shown in Fig. 4 exemplarily for binders with GGBS and for Portland cements. Concretes made of CEM I and GGBS are in the same range as concretes with binders that contain GGBS in the cement. The use of blast furnace slag cements tends to result in slightly lower s-values, because the early age strength is usually optimised by the cement producer. But since almost all CEM III/A results are still within the scatter of CEM I with GGBS, it was decided not to draw a distinction between GGBS used in cement or as an additive to concrete.

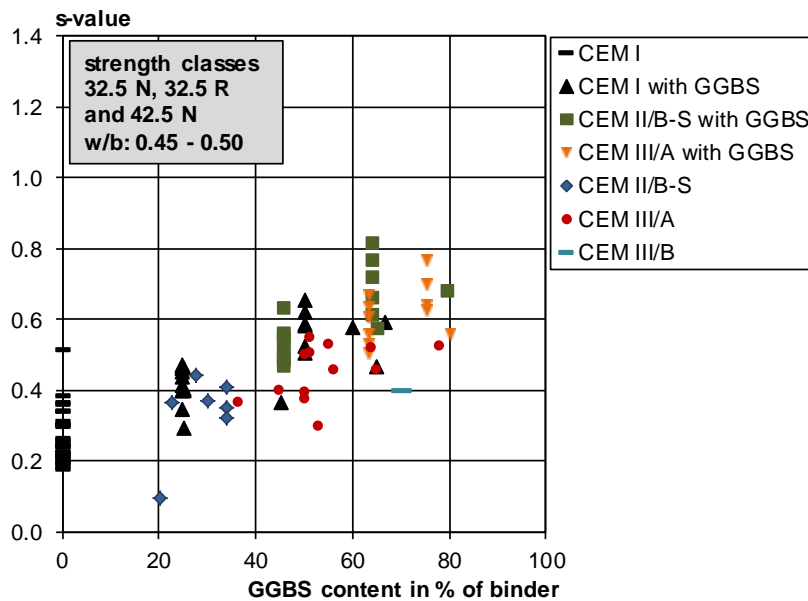


Fig. 4: Influence of binder composition and strength class of the cement on the s-values of concrete (*: strength class was not given in the paper, but could be determined from mortar compressive strength); data from [17, 21, 24 - 26, 41, 65, 78]

The influence of the water/binder ratio is shown in Fig. 5 for Portland cement. The s-value increases with increasing w/b ratio, but the scatter is quite high even within one strength class.

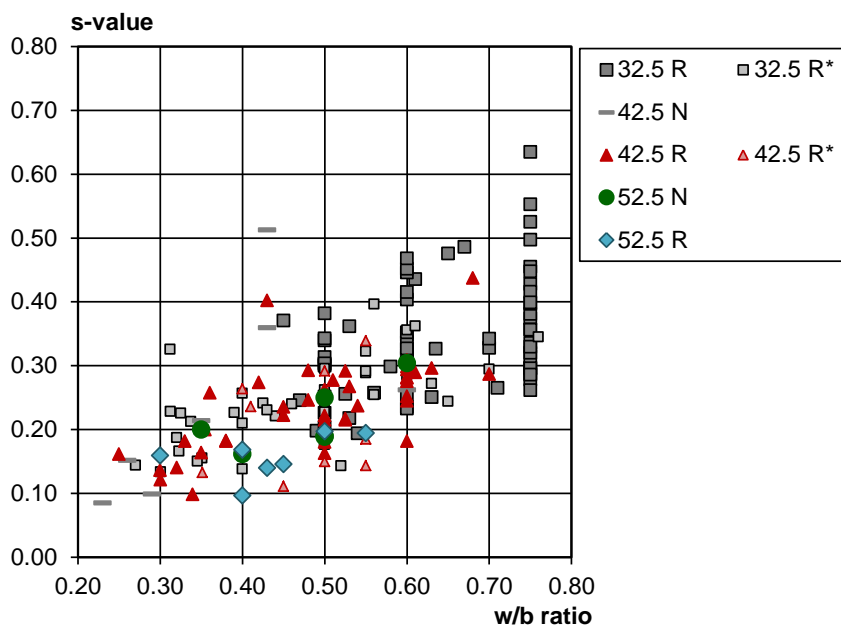


Fig. 5: Influence of the water/binder ratio on the s-values of concrete (*: strength class was not given in the paper, but could be determined from mortar compressive strength); data from [15 - 17, 20 - 25, 27, 30 - 32, 34, 36 - 41, 43 - 50, 52 - 62, 64, 65 - 68, 72 - 74, 76- 78]

In the following figures, the data was arranged according to the w/b ratio as follows:

- 0.25 – 0.39
- 0.40 – 0.54
- 0.55 – 0.69
- ≥ 0.70

An average s-value was calculated for binders that were tested with several w/b ratios within the same w/b range.

Fig. 6 and Fig. 7 show the results of the statistical evaluation of the s-values. The available data was summarised according to the w/b ratio and the strength class of the cement and plotted against the SCM content. A best fit line was calculated for all data points as well as a 90 % range. The figures show that the scatter is high even for pure Portland cement concrete. The s-values given in the fib Model Code (see paragraph 2.1) do not consider the influence of w/b-ratio. For pure Portland cement concrete made with cements of strength class 32.5 R or 42.5 N the s-value of 0.25 is appropriate for a rough estimation, but only in a w/b-range of 0.40 to 0.55. For 42.5 R and 52.5 N the s-value of 0.20 fits more or less for a w/b-range of 0.40 to 0.50. For 52.5 R the s-values are lower than predicted by the Model Code. For concretes with SCM the s-values from the Model Code are usually too low.

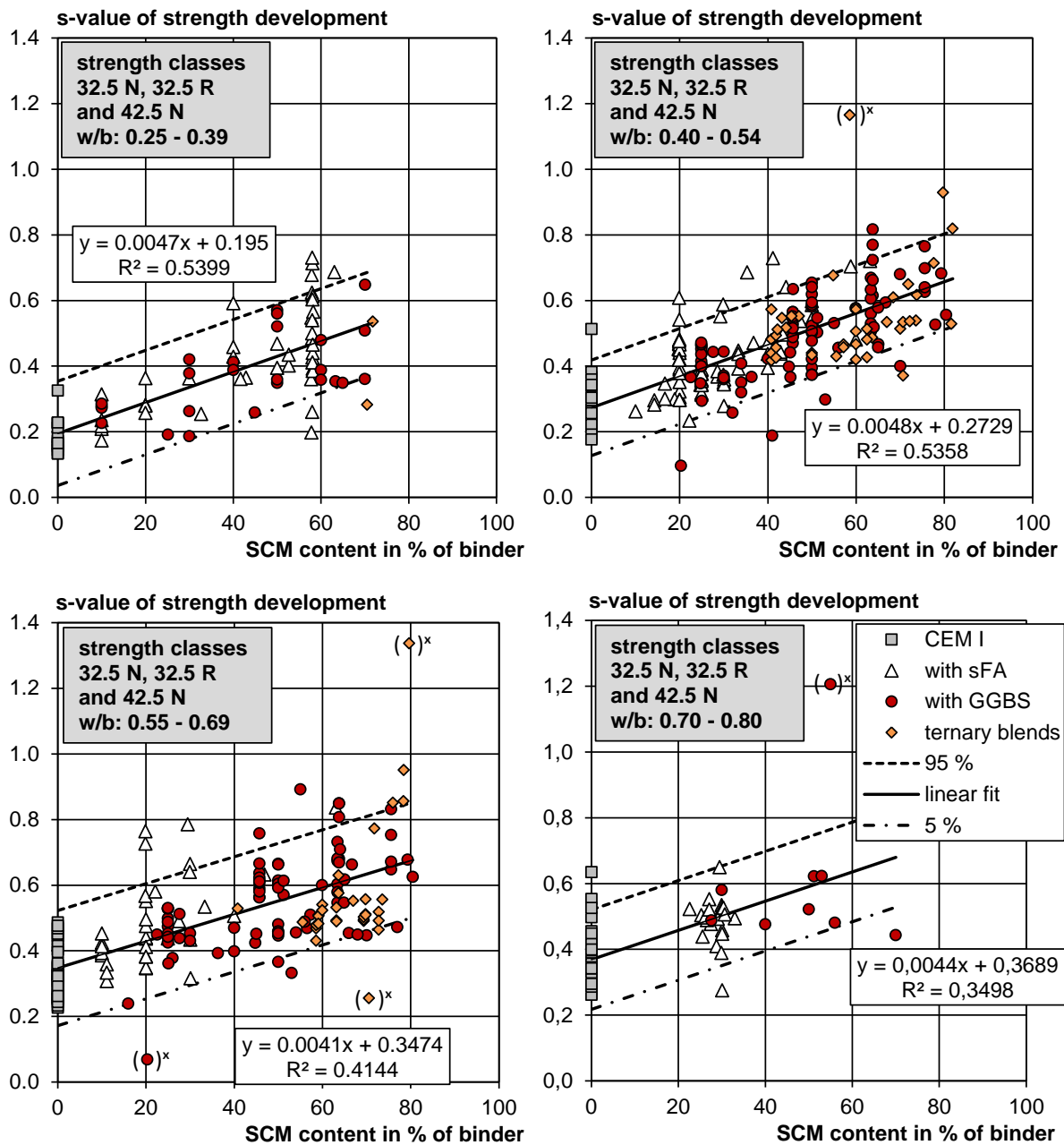


Fig. 6: Statistical evaluation of the s-values of concretes with cements of the lower strength classes in dependence of w/b ratio and SCM content *: outliers, identified with the outlier test of Dixon

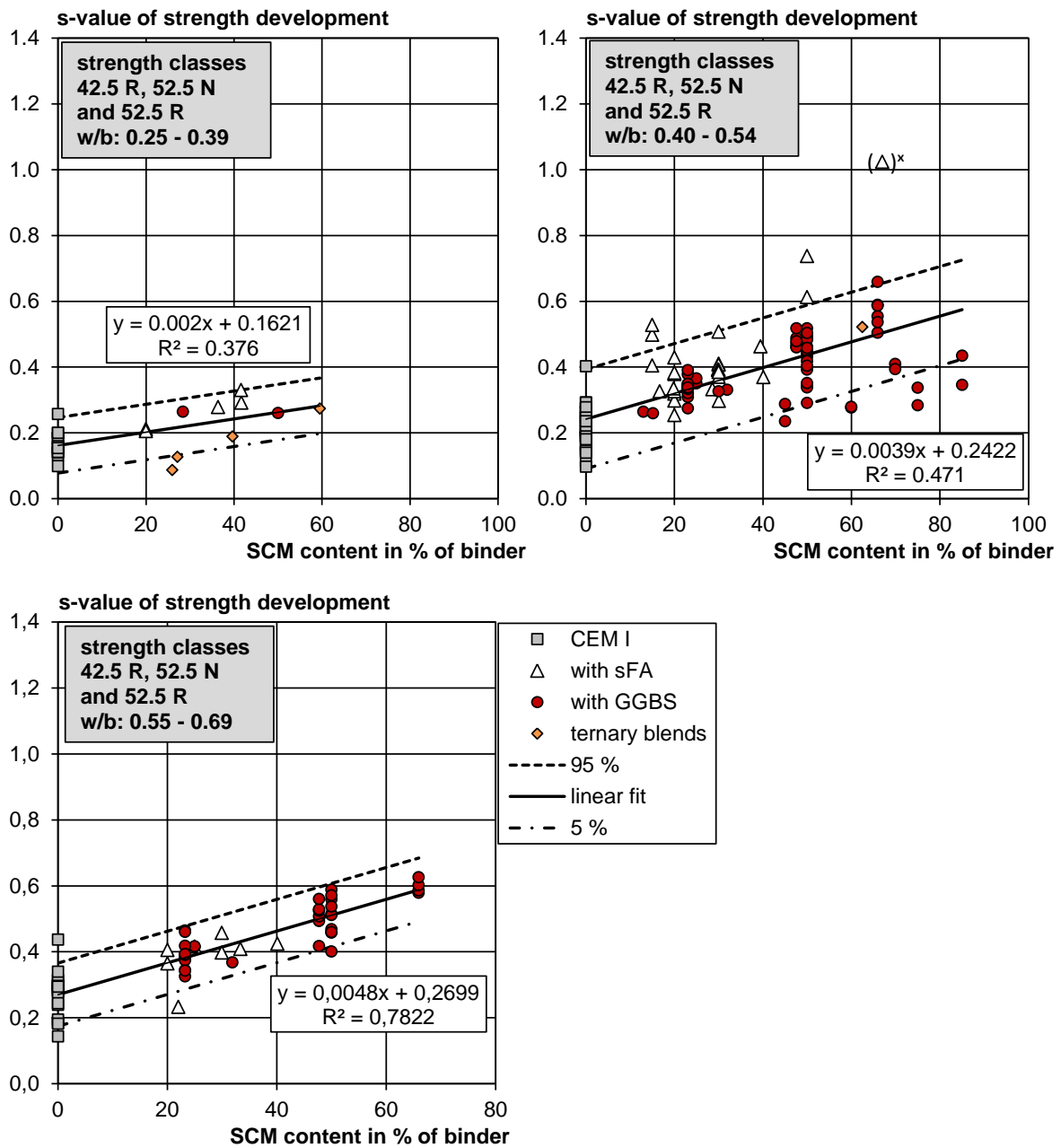


Fig. 7: Statistical evaluation of the s-values of concretes with cements of the higher strength classes in dependence of w/b ratio and SCM content ^x: outliers, identified with the outlier test of Dixon

2.3 Prognosis of strength development with the s-value

Fig. 6 and Fig. 7 show that the s-value depends on w/b ratio and SCM content. The correlations seem to be linear. A multiple linear regression analysis was carried out to quantify the influence of the two factors leading to equation (2). The implementation of a constant summand c_3 does not improve the fitting. Therefore c_3 was neglected to keep the equation as simple as possible.

$$s = c_1 \cdot w/b + c_2 \cdot scm/b \quad (2)$$

where

w/b is the free water to binder ratio (non-dimensional),

scm/b is the mass proportion of SCM in the binder (non-dimensional),

c_1 , c_2 are coefficients depending on the strength class of the cement.

The factors c_1 and c_2 were fitted with the least square method using all the available data (606 concretes for the lower strength classes and 255 concretes for the higher strength classes). The following results were obtained:

32.5 N, 32.5 R, 42.5 N: $c_1 = 0.528$, $c_2 = 0.527$

42.5 R, 52.5 N, 52.5 R: $c_1 = 0.481$, $c_2 = 0.441$

The correlation between the s-value determined according to paragraph 2.1 and the s-value calculated according to Eq. (2) is shown in Fig. 8. The correlation leads to a R^2 of 0.466, which is rather low. It has to be assessed how this is reflected in the prognosis of strength development.

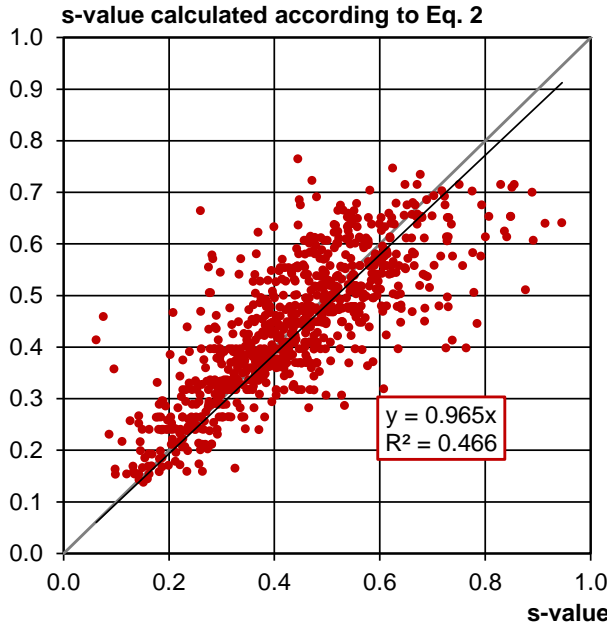


Fig. 8: Evaluation of the accuracy of Eq. (2) for the calculation of the s-value

Another option to determine the s-value of a specific concrete is an individual calculation based on early age strength and the 28 d strength by transforming Eq. (1) to Eq. (3):

$$s = \frac{\ln(f_{cm}(t)) - \ln(f_{cm,28d})}{1 - \sqrt{\frac{28d}{t}}} \quad (3)$$

where

t is the concrete age (1 to 3 days)

This individual fitting is supposed to give a good approximation of the strength development.

Both approaches were used to calculate the s-value and predict the compressive strength at 7 d, 56 d and 91 d using Eq. (1). Fig. 9 shows the correlation of these predicted values and the measured compressive strength. A statistical evaluation of the errors ($\Delta f_{cm} = f_{cm,measured} - f_{cm,predicted}$) gave the following standard deviations:

7 d: s calculated according to Eq. (2): 2.99 N/mm²
s calculated with early age strength (Eq. (3)): 2.22 N/mm²

56 d: s calculated according to Eq. (2): 2.51 N/mm²
s calculated with early age strength (Eq. (3)): 2.88 N/mm²

91 d: s calculated according to Eq. (2): 3.58 N/mm²

s calculated with early age strength (Eq. (3)): 4.18 N/mm²

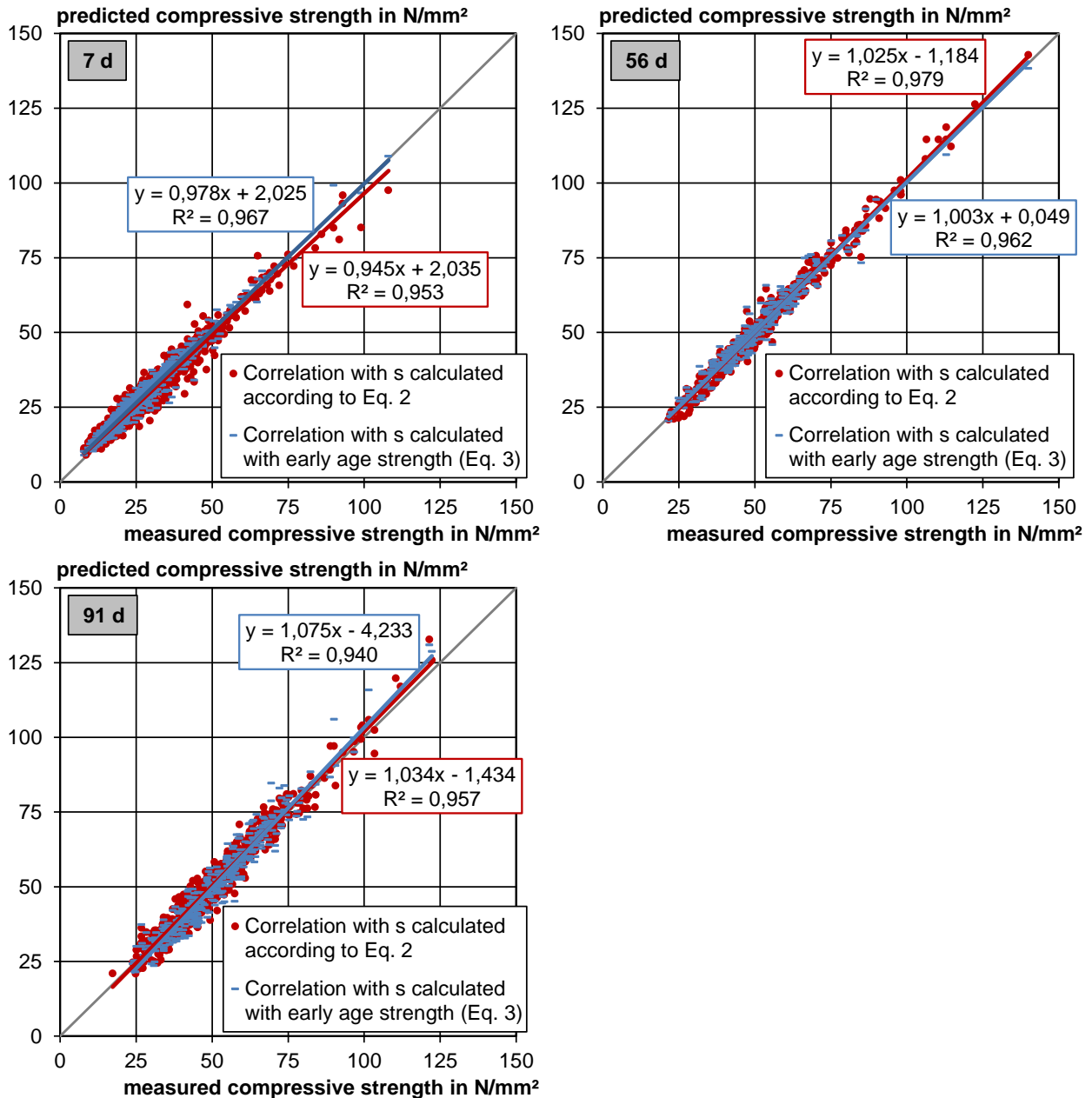


Fig. 9: Correlation between predicted and measured compressive strength at different concrete ages (7 d, 56 d and 91 d)

Considering the typical standard deviation of compressive strength testing, which is about 4 N/mm², both approaches are quite reliable. For the prediction of the strength between 3

and 28 days the calculation based on early age strength is a bit more precise. Therefore it is recommended to use Eq. (3) to calculate curing times.

For later ages the accuracy of the prediction with Eq. (3) decreases, because the s -value was calculated based on early age strength. Some countries, like Germany or Japan, allow higher assessment ages for concretes with high SCM contents for special applications like mass concrete. Eq. (2) can be used to predict the compressive strength at these later ages (usually 56 or 91 days).

3 Maturity function

All maturity functions require first the determination of a strength-time relationship. The fib model code uses Eq. (1). The applicability of this relationship for concrete mixes with SCMs has been discussed above. It has been suggested that more appropriate values for the s parameters for mixes with SCMs can be obtained from Eq. (2). This has been investigated for Portland cement (PC) concretes of 30 and 50 MPa 28-day cube compressive strength and results are reported in this section. Mixes with 30 % cement replacement with fly ash (FA) and with 50 % cement replacement with ground granulated blast furnace slag (GGBS) have also been investigated.

3.1 Materials and experimental methods

3.1.1 Materials

Portland cement (PC) CEM I 52.5 N, conforming to the requirements of BS EN 197-1:2000 and having a 28-day compressive strength of 57 MPa (tested according to the method described in BS EN 196-1-2005), was supplied in bags by British Lime Industries. PC was partially replaced with ground granulated blast furnace slag (GGBS) and fly ash (FA) conforming to BS EN 15167-1:2006 and BS EN 450-1:2005, respectively. GGBS was supplied in bags by the Appleby Group whereas FA was supplied in sealed plastic buckets by Fiddlers Ferry, a coal-fired electricity-generating station, in Warrington, UK. The chemical composition of PC, GGBS and FA are shown in Table 1.

Table 1: Chemical composition of PC, GGBS and FA

chemical constituent	PC	GGBS	FA
	w.-% (dried samples)		
SiO ₂	20.11	35.35	48
Al ₂ O ₃	5.16	14	27
Fe ₂ O ₃	3.14	0.36	9
CaO	65.49	41.41	3.3
MgO	0.8	7.45	2
SO ₃	3.22	0.1	0.6
K ₂ O	0.59	-	3.8
Na ₂ O	0.13	-	1.2
CaCO ₃	4.47	-	-
Equiv. Alks Na ₂ Oe	0.52	-	-
Free Lime	1.79	-	-
Chloride	0.0071	-	-
LOI	2.8	0.31	4.9

The coarse aggregate initially used was 5 - 20 mm uncrushed round gravel from the Fagl Lane quarry, which is located in Wales. Its specific density and water absorption were 2.64 g/cm³ and 1.7 %, respectively. The fine aggregate used was well graded fine aggregate also obtained from the Fagl Lane quarry having a specific density of 2.60 g/cm³ and a water absorption of 2.6 %.The combined grading curve for the Fagl Lane gravel and sand is shown in Fig. 10.

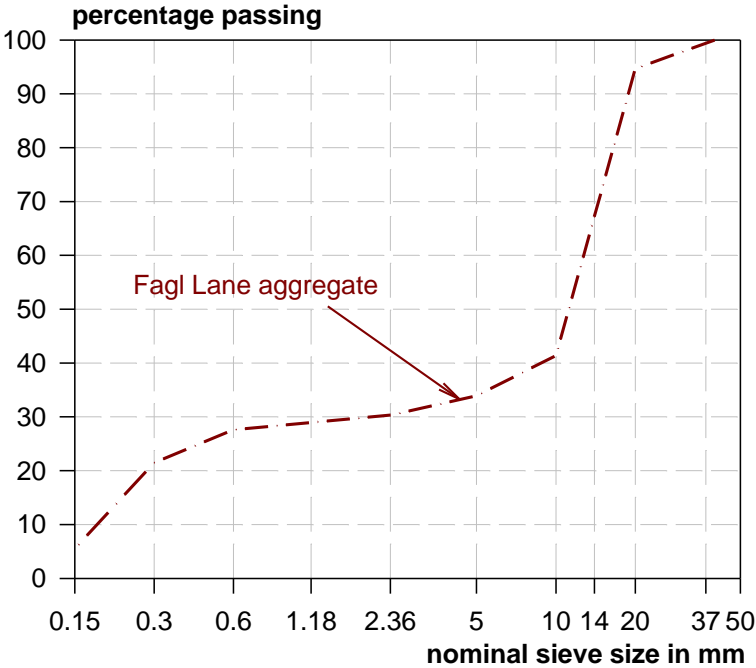


Fig. 10: Combined grading for coarse and fine aggregate

3.1.2 Concrete mixes investigated

The concrete mixes investigated aimed to have 28-day compressive strengths of 30 and 50 N/mm². The neat Portland cement mixes were named PC30 and PC50. FA30 and FA50 were mixes with 30% cement replacement by FA whilst GGBS30 and GGBS50 were mixes with 50% cement replacement by GGBS. The mix proportions of these are shown in Table 2.

Table 2: Mix proportions and slump of concrete mixes investigated

material / parameter	unit	PC30	GGBS30	FA30	PC50	GGBS50	FA50
cement*	kg/m ³	240	115	193	345	165	270
GGBS		-	115	-	-	165	-
FA		-	-	82	-	-	115
gravel		1102	1187	1319	1205	1151	1250
sand		799	721	560	615	683	533
free water		158	150	144	160	165	135
total water		198	190	181	197	203	171
free w/b	-	0.66	0.65	0.52	0.46	0.50	0.35
slump	mm	150	120	120	135	120	100

* Cement used was CEM I 52.5 N

3.1.3 Mixing, casting, curing and testing procedures

All concrete mixes were batched using a 0.1 m³ capacity horizontal pan mixer. Binder and aggregate were placed first in the mixing pan and dry-mixed for one minute. Water was then added and mixing continued for a further five minutes. The workability was assessed by carrying out the slump test according to BS EN 12350-2:2000. Concrete cube specimens (100 mm size) were subsequently cast in two layers in single- and three-gang steel moulds, and each layer was compacted using a vibrating table.

Two different curing procedures were used:

- **Standard curing** for which the concrete specimens, inside single cube moulds, were covered with wet hessian and a polythene sheet immediately after casting and left to

cure at room temperature conditions (approximately 20 °C) for a day. They were subsequently demoulded and placed inside a water bath set at 20 °C.

- **Adiabatic curing** - The adiabatic temperature rise due to hydration of cement will occur if there are no heat losses from the fresh concrete. To achieve this state it is necessary to either heavily insulate the concrete or alternatively to ensure that the environment in which the concrete is stored is at the same, or nearly the same, temperature as the concrete. The latter approach was adopted in this study. Concrete (150 mm cube) was cast in a steel box lined with 20 mm expanded polystyrene for insulation and heavy duty polythene to prevent moisture loss. The specimen was then placed into a programmable computer controlled curing tank and two copper/constantan thermocouples were inserted in it through a hole in the top of the box. Two more copper/constantan thermocouples were used to monitor the temperature of the water in the tank. The thermocouples were all connected to a computer which not only recorded the temperatures but also was set to activate the water heating system when the temperature difference between the water and the concrete was >1 °C. It can be assumed, based on the fact that there was no temperature drop after the maximum had been reached, that there was only very little heat loss and thus no adjustment was needed for the results. A schematic diagram of the setup of the programmable computer control curing tank used for adiabatic tests is shown in Fig. 11. In addition, concrete specimens, inside three-gang moulds, were sealed using a cling film and tape and placed inside the programmable computer controlled curing tank so that the compressive strength could be determined for the adiabatically curing regime. The adiabatically cured concrete specimens remained in the computer controlled tank until the concrete reached its maximum adiabatic temperature, usually one week after casting. Once the adiabatic temperature rise stopped, the remaining concrete specimens were removed from the tank, demoulded, wrapped with wet Hessian and polythene sheet and placed inside curing cabinets set at the final adiabatic temperature.

The testing ages for the standard cured specimens were 1, 2, 3, 5, 7, 14, 28, 42, 84, 156 and 365 days, while adiabatically cured concrete specimens were tested at 1, 2, 3, 5, 7, 14 and 28 days. At each testing age 3 specimens from each curing regime were tested in order to determine a mean compressive strength.

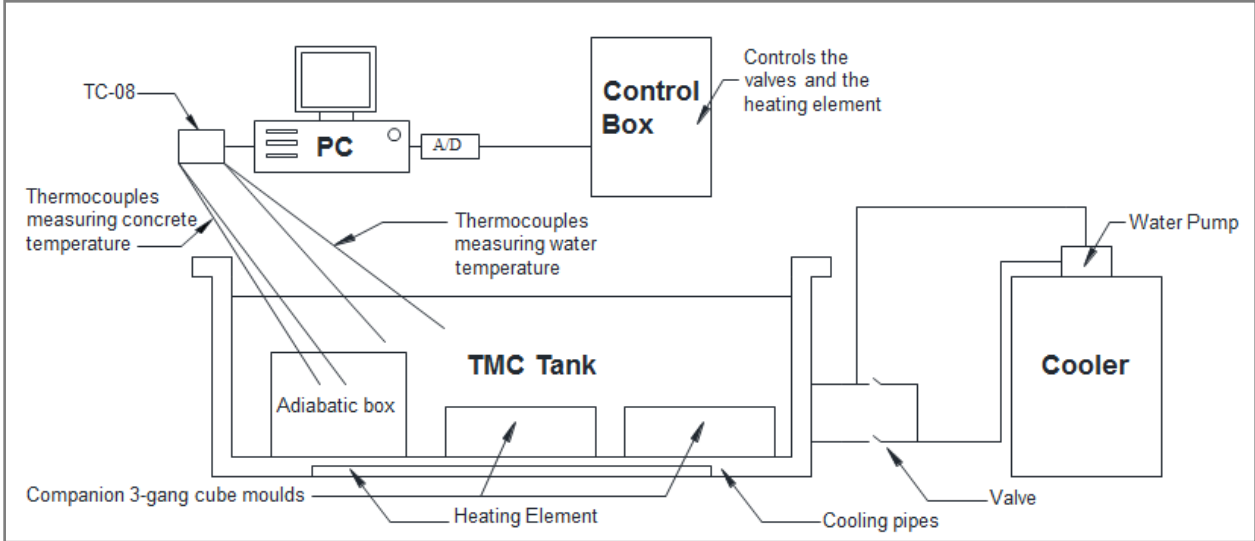


Fig. 11: Setup of the adiabatic test apparatus

3.2 Results and discussion

The cube compressive strengths of all the mixes investigated are first presented. The *s*-values from their strength development with time determined by regression analysis are then compared to the values from Eq. (2). The maturity function is then shown to be based on the Arrhenius function with the “apparent” activation energy being fixed at 33.3 kJ/mol irrespective of the binder type used. Adiabatic temperature histories are then presented and subsequently used with the maturity functions for estimating the strength development for non-isothermal curing temperatures.

3.2.1 Cube compressive strength development

Table 3 shows the compressive strengths obtained for 20 °C and adiabatic curing regimes. Not all concretes had the intended 50 and 30 N/mm² strength; most notably the GGBS50 that had only 42 N/mm² at 28-days.

Table 3: Compressive strength of the concrete mixes for 20 °C and adiabatic curing regimes

testing age	PC30		GGBS30		FA30		PC50		GGBS50		FA50	
	20 °C	Ad.	20 °C	Ad.	20 °C	Ad.	20 °C	Ad.	20 °C	Ad.	20 °C	Ad.
d	N/mm ²		N/mm ²		N/mm ²		N/mm ²		N/mm ²		N/mm ²	
1	7	13	2	3	7	12	21	31	5	12	13	24
2	13	22	4	9	13	20	30	35	10	28	22	38
3	18	25	7	14	17	25	35	37	15	37	28	46
5	20	26	10	21	21	32	41	39	21	43	34	53
7	23	29	13	25	24	34	43	39	26	42	38	56
14	28	29	19	29	28	39	47	41	34	45	43	56
28	31	31	25	31	35	39	50	49	42	47	51	57
42	32	-	28	-	37	-	53	-	43	-	58	-
84	33	-	31	-	46	-	55	-	51	-	59	-
156	33	-	34	-	47	-	59	-	-	-	66	-
365	32	-	37	-	47	-	56	-	-	-	67	-

Ad.: adiabatic curing

-: not determined

3.2.2 s-value

The s-values for all the different concretes have been obtained from Eq. (2) and by regression analysis of the actual strength development data. A commercially available statistical analysis software has been used to obtain the best fit of Eq. (1) by keeping the s-value as variable. The results are shown in Table 3.

At first sight the s-values obtained with the two approaches may appear to be quite different. The values obtained for PC concretes from Eq. (2) (last column) are higher than those from regression analysis (second-last column) whilst those for GGBS are lower. The ones for FA mixes are lower but less than those for GGBS.

The fit of the strength-relationships with s-values from Eq. (2) was therefore expected not to be very good. Nonetheless, the fit appears to be quite good, see Fig. 12 (a) and the improvement from using actual regression s-values is not significant.

Table 4: Comparison between s-value determined from Eq. (2) and regression analysis for 20 °C curing (c_1 and c_2 are 0.481 and 0.441 respectively since the cement used was CEM I 52.5 N)

mix ID	SCM replacement	28-day compressive strength	s-value obtained from regression	$s = c_1 \cdot w/b + c_2 \cdot scm/b$
	w.-%	N/mm ²	-	-
PC30	0	31	0.263	0.317
PC50	0	50	0.183	0.221
FA30	30	35	0.401	0.382
FA50	30	51	0.327	0.301
GGBS30	50	25	0.589	0.533
GGBS50	50	42	0.489	0.461

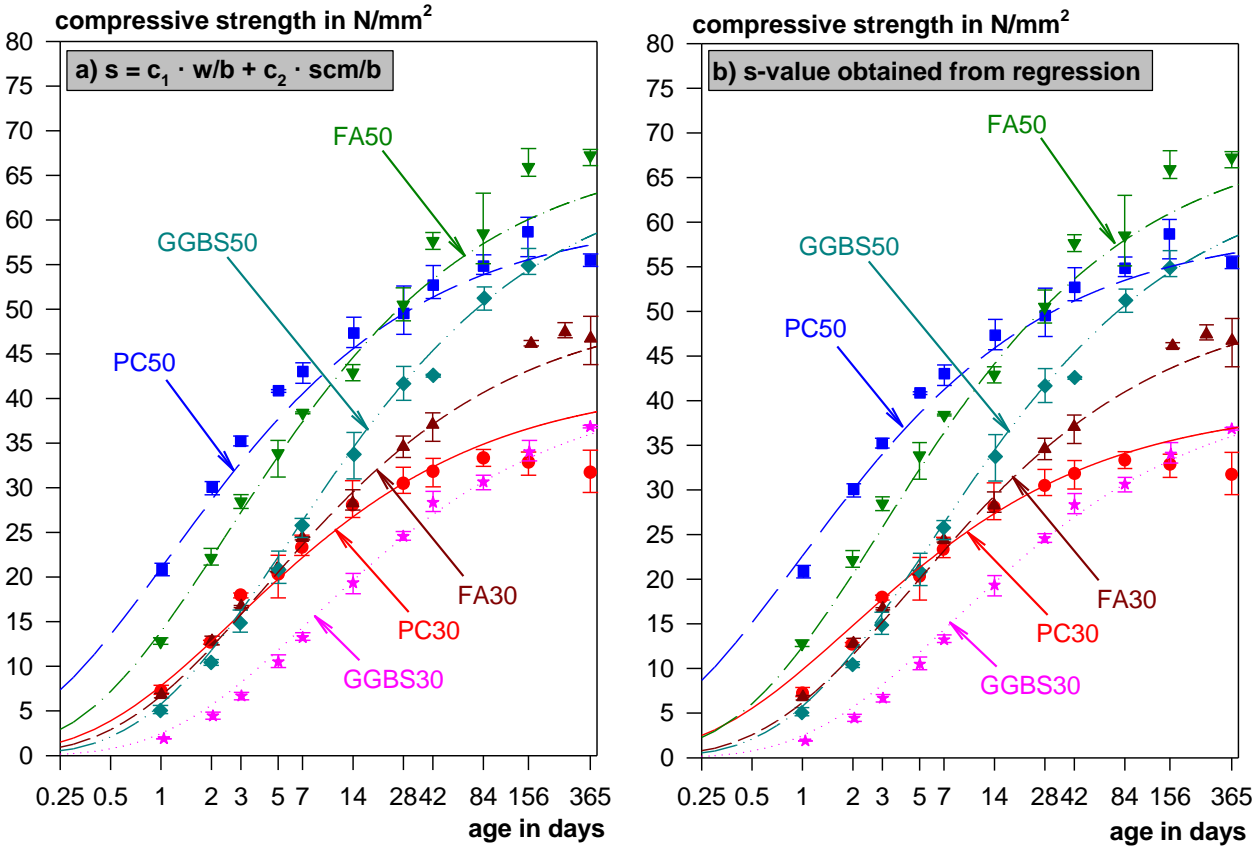


Fig. 12: Regression through experimental data at standard curing temperature (20 °C) using Eq. (1)

For FA50 the discrepancy between prediction and measurement was relatively high, whereas for FA30 the fit is good. To check whether long term strength can be predicted adequately, strength data for a concrete age of one year were taken from the data base (239

concretes) and analysed analogously to paragraph 2.3. Fig. 13 shows the results separately for the different binder types.

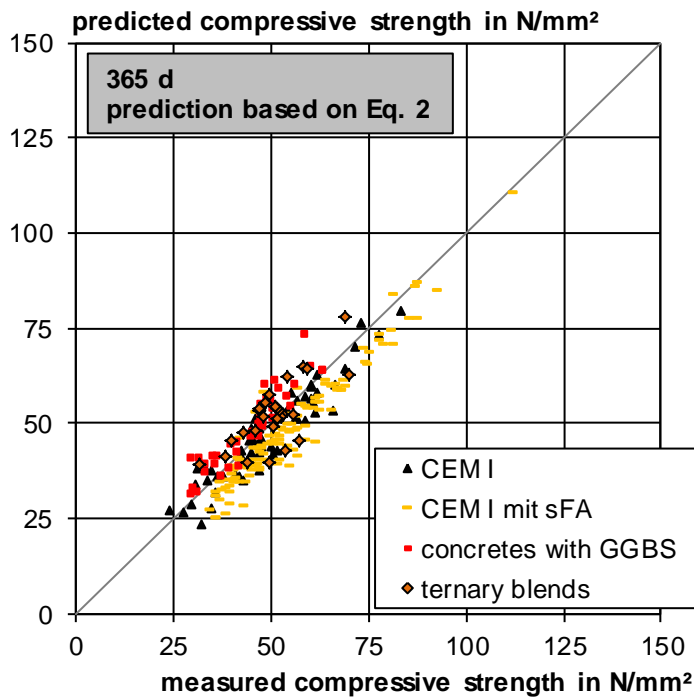


Fig. 13: Correlation between predicted and measured compressive strength at an age of 365 d

There are systematic differences between the different types of binders. The average errors

($\Delta f_{cm} = f_{cm,measured} - f_{cm,predicted}$) of the available data were calculated:

CEM I concretes: average $\Delta f_{cm, CEM I} = 2.4 \text{ N/mm}^2$

GGBS concretes: average $\Delta f_{cm, GGBS} = -4.8 \text{ N/mm}^2$

FA concretes: average $\Delta f_{cm, FA} = 5.5 \text{ N/mm}^2$

Concretes with ternary blends: average $\Delta f_{cm, ternary} = -1.6 \text{ N/mm}^2$

It can be concluded that on the long term, there is a difference between the two SCM. For concretes with GGBS the late strength is overestimated with the model based on Eq. 2, whereas for fly ash, the late strength is underestimated. Therefore for ternary blends the fit can be quite good.

3.2.3 Maturity function for estimating the strength development for adiabatically cured concretes

Eq. (1) in combination with the s -value calculated from Eq. (2) might be used to predict early age strength based on 28-day strengths. The latter are normally specified for design purposes, but the former are important to contractors e.g., (1) for accelerated construction schedules that put a new, repaired or overlaid pavement into service and which require adequate concrete strength to withstand traffic loads and (2) in structural elements, for the early removal of forms and props or the application of post-tensioning, and the termination of curing in cold weather. The factors affecting strength at early ages must be considered. These include, amongst others, (a) the composition of the concrete mixture, such as cement type and percentage of SCM in the binder and (b) the curing temperature of the concrete. The latter depends not only on the binder type used, but also on the size and shape of the structural element, the ambient temperature and whether thermal insulation is used or not. The concrete temperature inside a structural element is unlikely to be 20 °C. The adiabatic curing regime is an extreme situation, since it is assumed that no heat is lost, but nonetheless it is useful in quantifying the accuracy in the estimations of maturity functions. Maturity functions aim to account for the combined effect of time and temperature on strength development. They account for the “sensitivity” of different binders to temperature in different ways but these can be compared with “equivalent age” which represents “the duration of curing period at the reference temperature that would result in the same maturity as the curing period at other temperature”. For example, the maturity function proposed by Hansen and Pedersen [79], that assumes the rate of strength development obeys the Arrhenius law (referred to as Arrhenius in this paper):

$$t_e = \sum e^{-\frac{E_a}{R} \left(\frac{1}{T_a} - \frac{1}{T_s} \right)} \cdot \Delta t \quad (4)$$

Where

t_e is the equivalent age in days,

T_α is the average temperature of concrete during time interval Δt in K,

T_s is the specified reference temperature in K,

E_a is the apparent activation energy in J/mol and

R is the universal gas constant in J/K·mol.

In this case the age conversion factor is:

$$\alpha = e^{-\frac{E_a}{R} \left(\frac{1}{T_\alpha} - \frac{1}{T_s} \right)} \quad (5)$$

The fib model code's maturity function is based on the Arrhenius function with $E_a = 33,256$ J/mol, $R = 8.314$ J/ (K·mol) and specified reference temperature $T_s = 20$ °C:

$$t_T = \sum_{i=1}^n \Delta t_i e^{\left[13.65 - \frac{4000}{273 + T_\alpha(\Delta t_i)} \right]} \quad (6)$$

Where

t_T is the temperature-adjusted concrete age with replaces t in Equation 1 in days.

(Δt_i) is the number of days where a temperature T_α prevails in days,

$T_\alpha(\Delta t_i)$ is the average temperature of concrete during time interval Δt_i in °C,

The main difference to Eq. (4) is therefore the “apparent” activation energy that is fixed at 33.3 kJ/mol whilst the Arrhenius function allows different values for this. Apparent activation energies are normally determined for isothermally cured strength development data of “equivalent” mortars. The procedure, which is described in ASTM C1074-11, requires the “equivalent” mortars to have the same w/b ratio as the concretes and the sand to binder ratios need to be equal to the coarse aggregate to binder ratios of the concrete. Values from the “equivalent” mortars for concretes described here have been reported in Soutsos et. al (2016) [80]. These are shown in Fig. 14 and it can be seen that the fib model code's selection of 33.3 kJ/mol as apparent activation energy is between those of PC50 and PC30.

The FA ones are slightly below those of the equivalent PC concretes whilst those for GGBS are considerably higher. The effect these have on the strength estimates will be examined next.

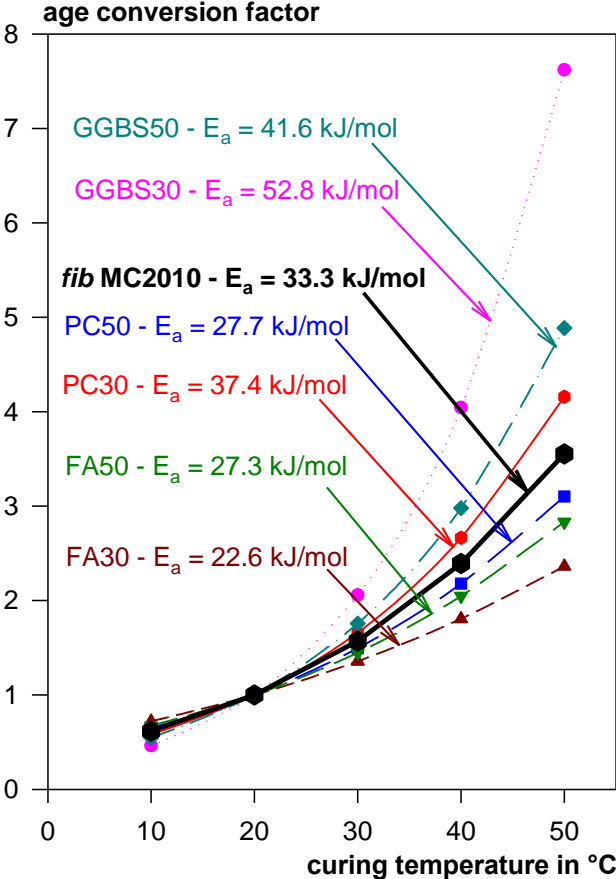


Fig. 14: Effect of temperature and binder composition on the age conversion factor

3.2.4 Adiabatic temperature history

The adiabatic temperature history of all the concretes is shown in Fig. 15. The Portland cement concretes of 50 and 30 N/mm² strengths had a temperature rise of 48 °C and 32.5 °C respectively from a casting temperature of approximately 20 °C. GGBS at 50 % of total binder is effective in reducing the adiabatic temperature rise considerably, i.e. down to 38 °C and 24 °C for grades 50 and 30 N/mm² respectively. FA at 30 % of total binder reduces the peak temperature rise of 50 N/mm² concrete down to 39 °C but there was no reduction for the 30 N/mm² concrete. This appears to be abnormal except that similar trends have been

obtained from in-situ temperature rises during the DTI Core project [9]. A possible explanation for this could be that the contribution to heat by FA has been affected by the low water to binder ratio of 0.35 for the 50 N/mm² concrete. This suggestion is made because FA has been shown to have lower strength contribution at lower water to binder ratios [81]. The higher strength mixes reach higher temperatures, as expected. It must also be noted that the binder contents of FA50 and FA30 are higher, at 385 and 275 kg/m³, from the equivalent PC concretes which had 330 and 240 kg/m³ of cement. The heat output of the binder, which was experimentally determined through isothermal calorimeter as described in [81], has been estimated to be 314 kJ/kg and 331 kJ/kg for PC50 and PC30, 240 kJ/kg and 256 kJ/kg for FA50 and FA30 and 220 kJ/kg and 257 kJ/kg for GGBS50 and GGBS30 respectively. As can be seen, the heat output per kg of binder is slightly reduced at lower water to binder ratios which confirms previous findings [82, 90, 91, 92, 93].

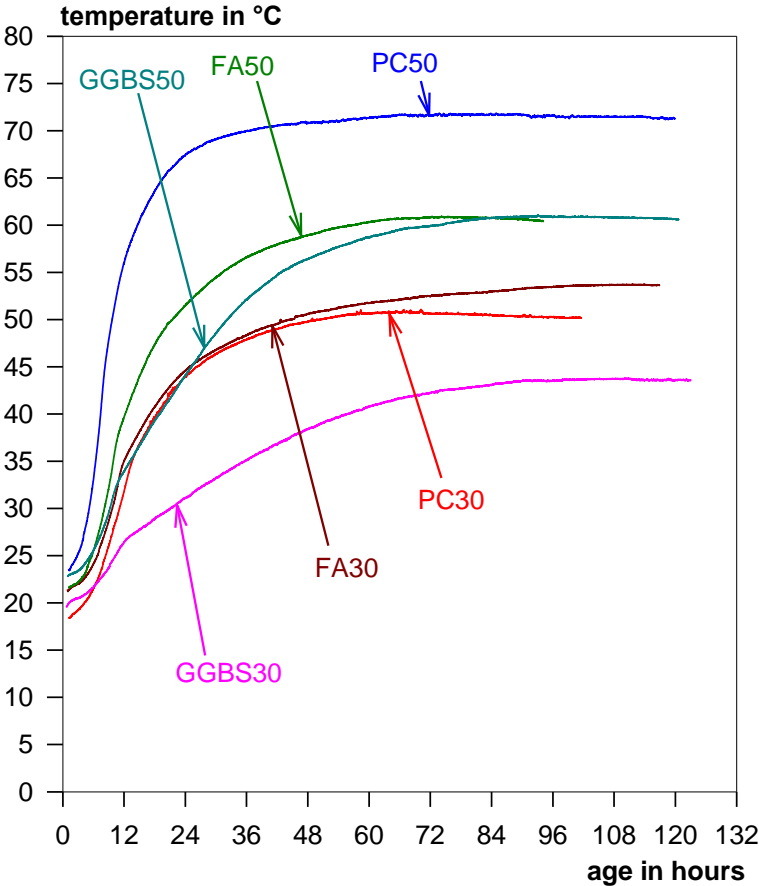


Fig. 15: Adiabatic temperature of investigated concretes

3.2.5 Concrete strength estimates

The Arrhenius function required the apparent activation energies of all six concretes which were previously determined [80, 82] according to ASTM C1074-11 method and they were PC30 = 37.4 kJ/mol, GGBS30 = 52.8 kJ/mol, FA30 = 22.6 kJ/mol, PC50 = 27.7 kJ/mol, GGBS50 = 41.6 kJ/mol and FA50 = 27.3 kJ/mol as shown in Fig. 14. These were found to be in good agreement with values in literature [83 - 87]. The equivalent age t_e at time t was calculated using Eq. (4). The specified reference temperature, T_s , used was 293 °K (20 °C). The fib model code's procedure requires that the temperature-adjusted concrete age t_T , which is the equivalent age, is calculated from Eq. (6) with T_a being the average temperature (in °C) of concrete during time interval Δt_i , which is the temperature history the concrete is subjected to (in this case, these were the temperature histories recorded during the adiabatic tests). The value of t_T obtained was then substituted for t at Equation 1 with the s-value as previously determined from Eq. (2). The value of equivalent age obtained, t_e , was then substituted for t in Eq. (1) with s-value as previously determined for the strength data obtained for the concrete cured at 20 °C.

The adiabatic temperature histories, Fig. 15, were thus converted into estimated strength development curves and these are shown in Fig. 16 and Fig. 17. The "Arrhenius" labelled indicates that (a) the s-value was obtained by regression of the strength data obtained for the concrete cured at 20 °C and (b) the "apparent" activation energy was determined according to ASTM C1074-11. The "Modified fib" labelled one indicates that (a) the s-value was obtained from Eq. (2) and (b) the "apparent" activation energy was 33.3 kJ/mol irrespective of the binder. The calculated strength values estimated using the "Modified fib" are considerably good especially at early ages, for all tested mixtures except the PC50, thus increasing confidence in the use of Eq. (2) for estimating the s-value without determining this by regression of actual strength development data. It is most noticeable for the PC50 that the maturity functions overestimate long term strength. This is due to the inability of maturity

functions to account for the detrimental effect that high early age temperatures have on later age strength.

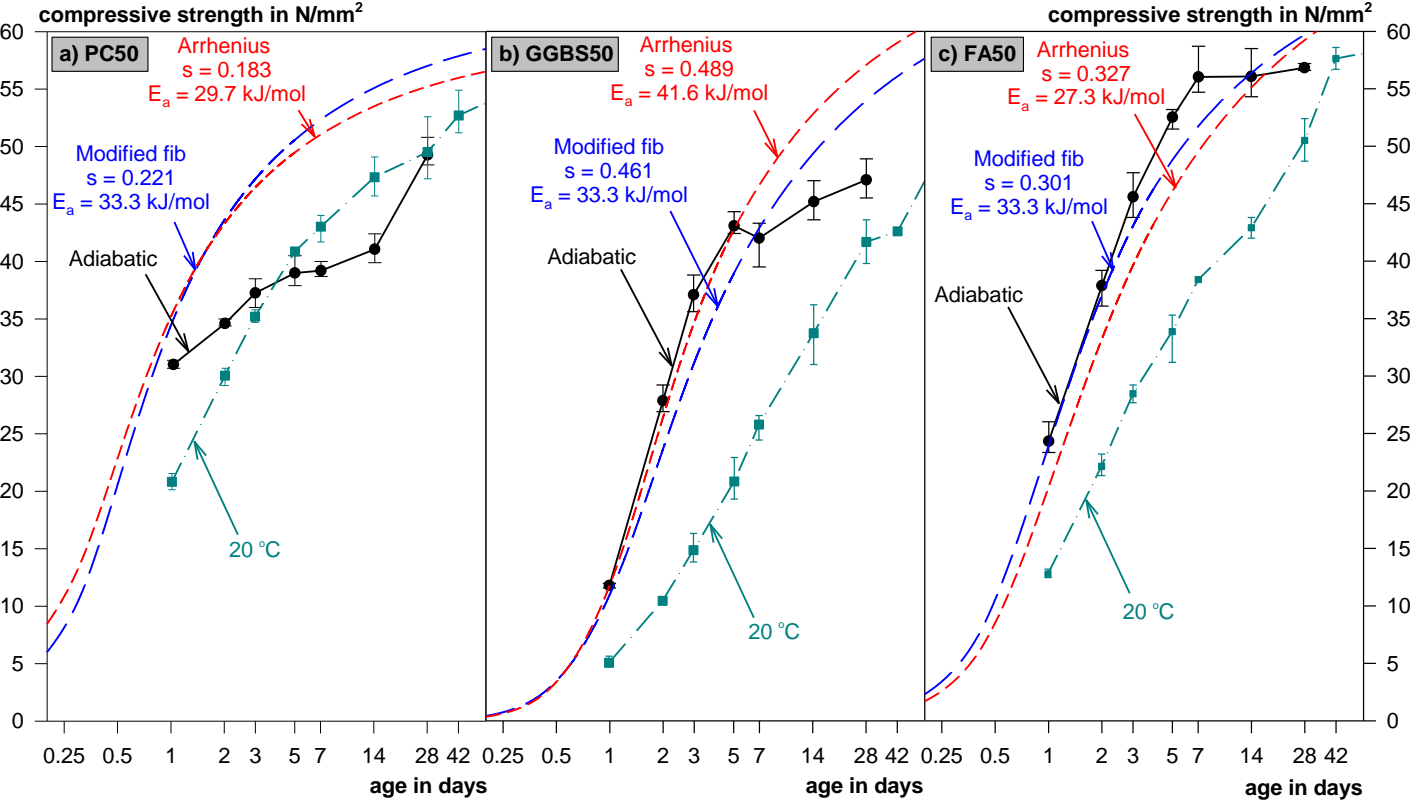


Fig. 16: Adiabatic strength estimates for 50 N/mm² strength concretes

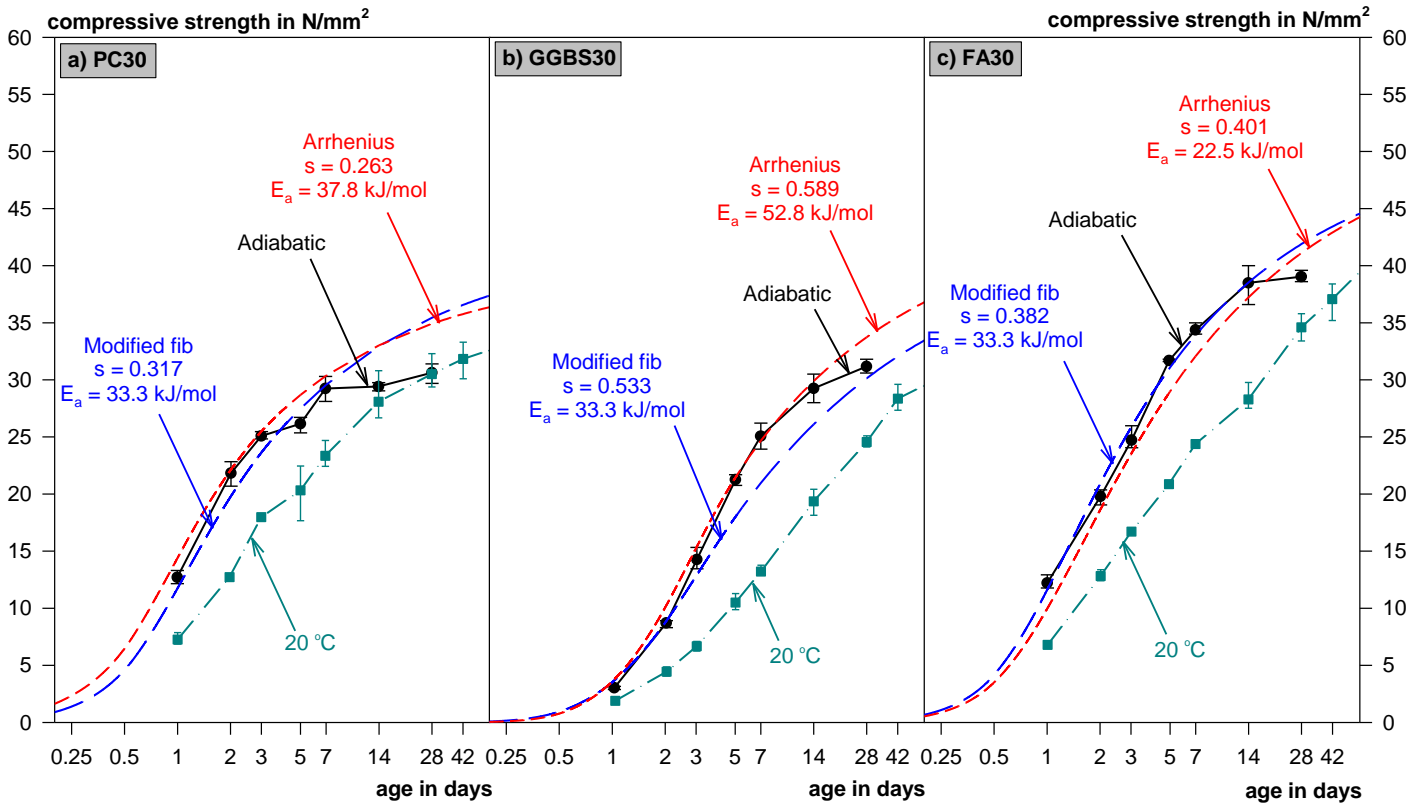


Fig. 17: Adiabatic strength estimates for 30 N/mm² strength concretes

The temperature of the PC50 rises above 60 °C, within 12 hours after casting. This is approximately the highest temperature recorded for FA50 and GGBS50 but these occur much later at 48 and 72 hours respectively. The temperature rise under nearly adiabatic curing regime relies on the heat evolution from the binder. The increase in temperature for FA50 and GGBS50 is delayed by several hours and significant rises only occur even more hours later as a result of the induction period [88]. As the hydration reaction is required to have progressed significantly before high temperatures occur, the detrimental effect to long term strengths is significantly reduced. It is for this reason that it is recommended that curing cycles, e.g. for precast concrete products, should have a “delay period” before the “temperature rise period” [89].

The early age temperature rise of the PC50 appears to have had significant detrimental effect to the ultimate strength and strength estimates do not improve after 1 day but become worse. This detrimental effect of high early age curing temperature on later age strength has become known as the “cross-over” effect (firstly reported by McIntosh in 1956 [94]) and is

believed be due to the formation of dense hydrated phases around the unreacted cement particles, preventing further hydration [95, 96]. Furthermore, this deviation of strength estimates from the actual measured values is less pronounced for especially the FA and GGBS concretes because of (a) the longer “delay period” and (b) the “cross-over” effect occurring much later than Portland cement, i.e. beyond 28-days as can be seen from Fig. 16 and Fig. 17.

The above discussed trends can be also seen in Fig. 18 and Fig. 19 where the estimated to actual strength ratio is plotted versus age. These figures also show that the Arrhenius labelled estimates do not considerably improve with the use of specific coefficients of the particular concrete, i.e. the s -values determined from regression analysis and the use of “apparent” activation energies. The improvements are mainly for the GGBS concretes which have considerably higher “apparent” activation energies, i.e. 41.6 and 52.8 kJ/mol for GGBS50 and GGBS30 respectively, from the 33.3 kJ/mol used in the fib model code. The small differences in “apparent” activation energies, as well as the “delay period” for PC and FA concretes, may have made the improvements in strength estimates appear to be small. This may be different if the concretes were cured isothermally at an elevated temperature especially if these high temperatures were applied immediately after casting.

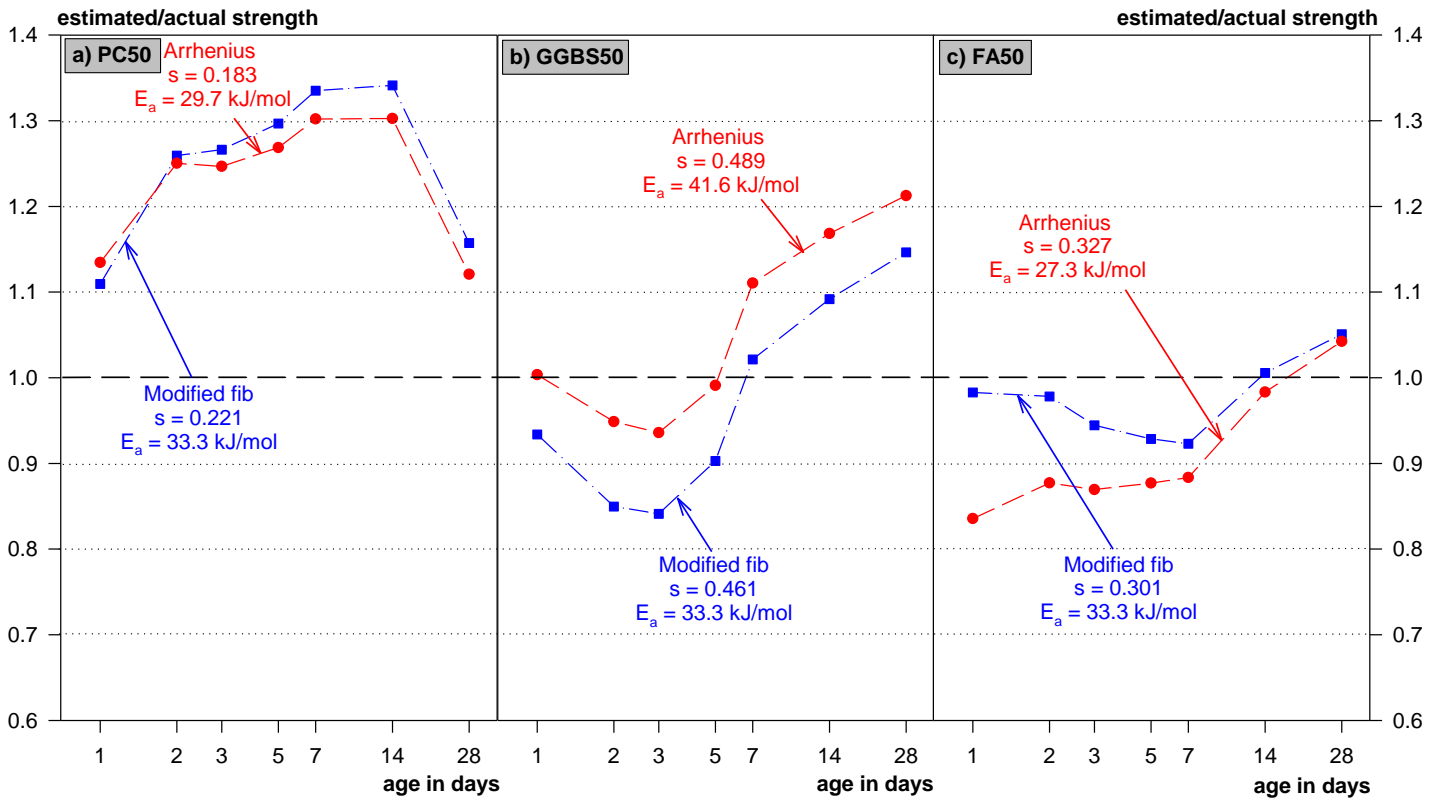


Fig. 18: Estimated vs. actual strength ratios for 50 MPa strength concretes

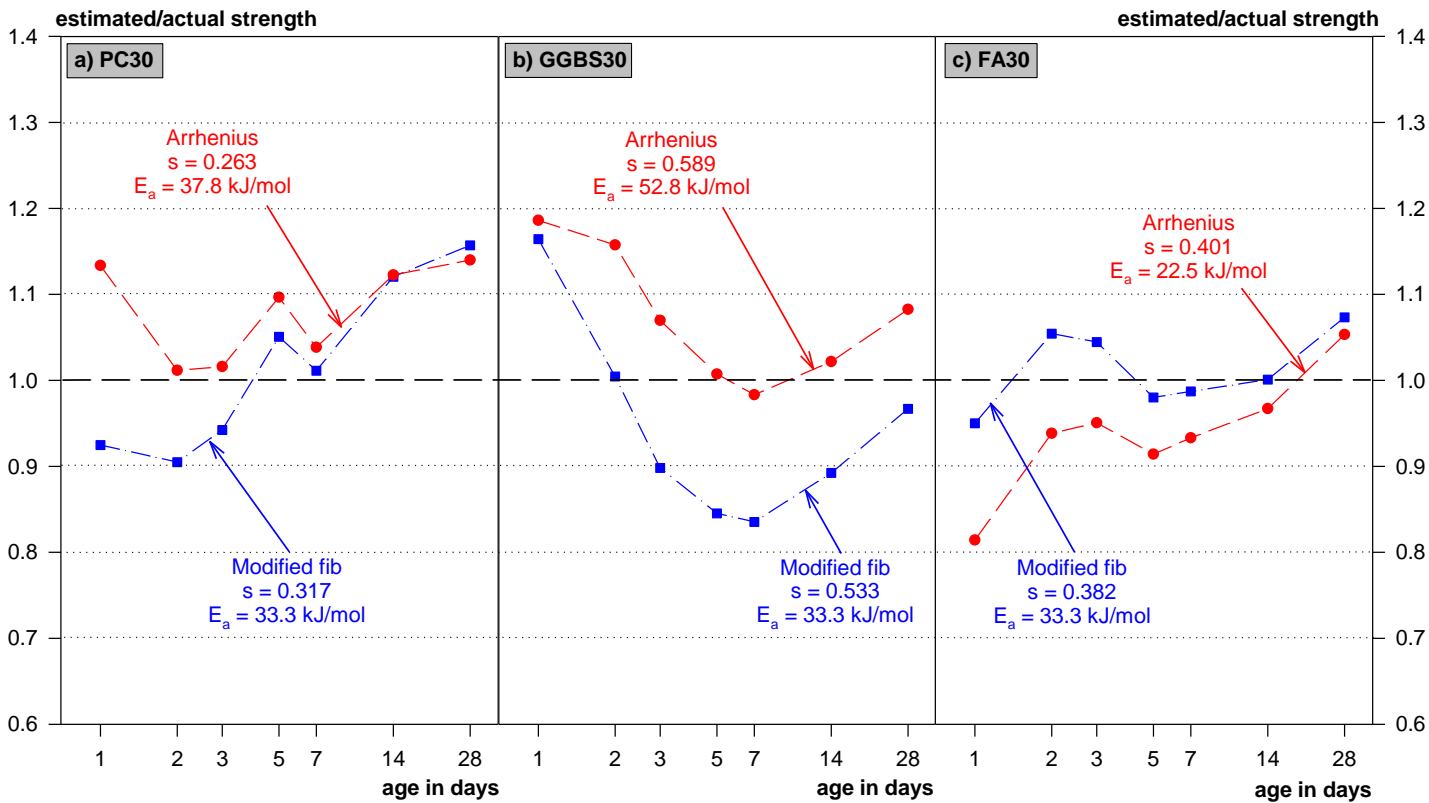


Fig. 19: Estimated vs. actual strength ratios for 30 MPa strength concretes

4 Summary and outlook

This paper provides an approach to predict the compressive strength development of concrete with GGBS and silicious fly ash including ternary blends. The calculation is based on an e-function that is defined in the fib Model code. The Model code considers the strength class of the cement with a so-called s-value. In this paper the effect of GGBS and fly ash on the s-value was quantified based on a large concrete database. The fly ash content of the selected concretes ranges from 10 to 63 wt.-% related to the binder. Most of the concrete mixes are in a range of 20 to 35 wt.-% fly ash, The GGBS concretes range from 7.5 to 85 wt.-% GGBS in the binder, most of them having 25 to 60 wt.-% GGBS,

The s-value of a specific concrete can be calculated based on the SCM content and water/binder ratio. This relationship between s-values and w/b plus SCM/b ratios has been tested on laboratory cast specimens with 50 and 30 % cement replacement with GGBS and FA respectively. These showed that:

- The s-values from this relationship, when compared to those obtained from regression analysis, did differ but the estimated strength development with time was quite good up to an age of 91 d and the improvement from using actual regression s-values was not significant.
- Late strength predictions will lead to an overestimation of the strength of concretes with GGBS and an underestimation of the strength of concretes with FA. The absolute error is in the order of 5 N/mm² after one year for both types of binders.
- The fib model code's maturity function is based on the Arrhenius function with a fixed apparent activation energy of $E_a = 33.3$ kJ/mol. This apparent activation energy is between those of PC50 and PC30.
- The E_a of the FA concretes are slightly below those of the equivalent PC concretes whilst those for GGBS concretes are considerably higher.
- Use of these different "apparent" activation energies that are specific to the concrete mix constituents do not considerably improve the strength estimates.

- The small differences in “apparent” activation energies, as well as the small “delay period” for PC and FA concretes, may have made the improvements in strength estimates from the use of “apparent” activation energies specific to the particular concrete appear to be small.
- The use of “apparent” activation energies specific to the particular concrete may result in more accurate estimates for concretes cured isothermally at an elevated temperature especially if these high temperatures were applied immediately after casting.

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6 Annex

Table A 1: Summary of the collected data on strength development of Portland cement concretes

binder	storage conditions	number of cements	range of w/c-ratio	number of concrete mixes
CEM I, unspecified*	W or FR	23	0.27 - 0.80	56
	C7	1	0.32	1
CEM I 32.5 R	W or FR	1	0.47 - 0.67	3
	C7	42	0.45 - 0.75	71
CEM I 42.5 N	W or FR	4	0.23 - 0.60	9
CEM I 42.5 R	W or FR	5	0.42 - 0.68	6
	C7	22	0.25 - 0.70	46
CEM I 52.5 N	W or FR	2	0.50	2
	C7	2	0.35 - 0.60	4
CEM I 52.5 R	W or FR	1	0.55	1
	C7	4	0.30 - 0.50	6

* No strength class given (ASTM or Australian standard). Based on the compressive strength of mortar five Portland cements were assigned to strength class 42.5 R or higher [27, 37 - 39, 43, 46]. Eighteen cements were assigned to strength class 32.5 R or 42.5 N [15, 16, 30, 31, 37, 39, 44, 46 - 48, 50, 52, 53, 55, 56, 62]

W: Storage under water until testing at 20 ± 3 °C

FR: Storage in a fog room with ≥ 95 % r. h. at 20 ± 3 °C

C7: Storage under water until an age of 7 d for curing, afterwards air storage, 20 ± 3 °C and 60 % or 65 % r. h.

Table A 2: Summary of the collected data on strength development of concretes with sFA

binder	storage conditions	number of cements	number of sFA	number of binder combinations	range of w/b-ratio	number of concrete mixes
CEM I, unspecified*, with sFA	W or FR	12	29	50	0.27 - 0.80	86
	C7	1	2	2	0.31	2
CEM I 32.5 R with sFA	W or FR	1	1	3	0.39 - 0.56	12
	C7	17	31	54	0.29 - 0.67	78
CEM I 42.5 N with sFA	W or FR	1	1	3	0.26 - 0.36	6
CEM I 42.5 R with sFA	W or FR	2	5	7	0.42 - 0.48	7
	C7	11	13	18	0.31 - 0.75	24
CEM I 52.5 N with sFA	W or FR	2	4	7	0.40 - 0.50	7
	C7	1	1	1	0.40 - 0.60	3
CEM II/B-V 32.5 R	C7	18	-	18	0.60 - 0.75	21
CEM II/B-V 42.5 R	C7	1	-	1	0.60	1

* No strength class given (ASTM or Australian standard). Based on the compressive strength of mortar eleven of these cements could be assigned to strength class 32.5 R or 42.5 N [15, 16, 29 - 31, 39 (cement C), 44, 55, 62]. One cement was assigned to strength class 42.5 R [39 (cement B)].

w/b: water / binder ratio (b = cement content + SCM content)

Table A 3: Summary of the collected data on strength development of concretes with GGBS

binder	storage conditions	number of cements	number of GGBS	number of binder combinations	range of w/b-ratio	number of concrete mixes
CEM I, unspecified*, with GGBS	W or FR	6	8	21	0.29 - 0.76	64
CEM I 32.5 R with GGBS	C7	2	12	19	0.45 - 0.62	54
CEM I 42.5 N with GGBS	W or FR	1	1	3	0.26 - 0.38	8
CEM I 42.5 R with GGBS	C7	5	10	28	0.33 - 0.60	86
CEM I 52.5 N with GGBS	W or FR	2	2	8	0.50	8
CEM I 52.5 R with GGBS	C7	1	1	1	0.26 - 0.42	3
CEM II/A-S 42.5 N	C7	1	-	1	0.58	1
CEM II/A-S 42.5 R	W or FR	1	-	1	0.43	1
CEM II/B-S, unspecified*	W or FR	3	-	3	0.50	3
CEM II/B-S 32.5 R	W or FR	1	-	1	0.43	1
	C7	4	-	4	0.45 - 0.70	12
CEM II/B-S 42.5 N	W or FR	1	-	1	0.43	1
	C7	1	-	1	0.47 - 0.67	3
CEM II/B-S 42.5 R	C7	1	-	1	0.50 - 0.60	3
CEM II/B-S 32.5 R with GGBS	C7	3	12	18	0.45 - 0.60	53
CEM II/B-S 42.5 R with GGBS	C7	1	6	12	0.43 - 0.59	36
CEM III/A, unspecified*	W or FR	3	-	3	0.50	3
CEM III/A 32.5 N	W or FR	2	-	2	0.50 - 0.70	6
	C7	13	-	13	0.30 - 0.75	25
CEM III/A 32.5 R	W or FR	1	-	1	0.50 - 0.69	3
	C7	1	-	1	0.60 - 0.67	2
CEM III/A 42.5 N	W or FR	2	-	2	0.43 - 0.52	3
	C7	4	-	4	0.50 - 0.60	11
CEM III/A 42.5 R	C7	3	-	3	0.5	3
CEM III/A 52.5 N	C7	3	-	3	0.5	3
CEM III/A 32.5 N with GGBS	C7	2	6	11	0.45 - 0.61	33
CEM III/B, unspecified*	W or FR	3	-	3	0.50	3
CEM III/B 32.5 N	C7	4	-	4	0.50 - 0.75	7

* No strength class given (ASTM or Australian standard). Based on the compressive strength of mortar five CEM I and one CEM II/B-S could be assigned to strength class 32.5 R or 42.5 N [46 - 48, 52, 53, 55]. One CEM I was assigned to strength class 42.5 R [38]. Two CEM II/B-S and one CEM III/A were assigned to strength class 32.5 N [46]. Four cements (one CEM III/A and three CEM III/B) did not reach 32.5 N/mm² after 28 days and were neglected [46].

w/b: water / binder ratio (b = cement content + SCM content)

Table A 4: Summary of the collected data on strength development of ternary blends containing GGBS and sFA

binder	storage conditions	number of cements	number of SCM	number of binder combinations	range of w/b-ratio	number of concrete mixes
CEM I 42.5 R with GGBS and sFA	C7	1	1 / 1*	1	0.42 - 0.51	2
CEM II/A-S 52.5 R with sFA	C7	2	2	2	0.25 - 0.29	2
CEM II/B-S 32.5 R with sFA	W or FR C7	1 2	1 5	2 5	0.44 - 0.52 0.43 - 0.60	2 8
CEM II/B-S 52.5 R with sFA	C7	1	1	1	0.25	1
CEM II/B-S 42.5 N with sFA	W or FR	1	1	1	0.47 - 0.55	2
CEM II/B-S 32.5 R with GGBS and sFA	C7	1	1 / 1*	1	0.42 - 0.51	2
CEM III/A 32.5 N with sFA	W or FR C7	2 6	2 4	2 14	0.42 - 0.61 0.42 - 0.65	7 39
CEM III/A 32.5 R with sFA	W or FR C7	1 1	1 3	2 6	0.45 - 0.67 0.60 - 0.67	7 9
CEM III/A 42.5 N with sFA	C7	1	2	2	0.43 - 0.47	5
CEM III/A 52.5 N with sFA	C7	1	1	1	0.32	1
CEM III/B 32.5 N with sFA	C7	3	4	8	0.47 - 0.67	12

* number GGBS / number sFA

w/b: water / binder ratio (b = cement content + SCM content)