Taking Baby Steps in Molecular Logic-based Computation


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Taking Baby Steps in Molecular Logic-based Computation

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Molecular logic-based computation is a broad umbrella covering molecular sensors at its simplest level and logic gate arrays involving steadily increasing levels of parallel and serial integration. The fluorescent PET (photoinduced electron transfer) switching principle remains a loyal servant of this entire field. Applications arise from the convenient operation of molecular information processors in very small spaces.

1. Introduction

Since molecular logic-based computation arrived in the primary literature,1 it has been embraced by around 250 laboratories in many different parts of the world (Figure 1).2 It has been supported by six dedicated books3-7 and by substantial chapters in several other volumes.8-13 A large number of review articles are also available,14-40 including article collections in special journal issues.41-43 A series of biennial conferences dedicated to the field has completed the fourth edition.44 The first commercial product is serving worldwide in life-critical situations,45,46 with sales of 120M $ so far. We are grateful for this opportunity to outline the journey of the field and to describe the lessons learned over the past two decades.

2. A robust design tool for molecular switches is available

Our story starts with the heart of plant photosynthesis - photoinduced electron transfer (PET).47 Following Weller's insights into intermolecular PET process,48 intramolecular 'fluorophore-spacer-receptor' systems could be developed.49-51 These have two distinct states, one where the receptor is free of the target species and another where the receptor has captured the target. Usually, the fluorescence emission of the first state is switched 'off' (output 0) and that of the second state is switched 'on' (output 1). This is the fluorescent PET sensor/switch principle. It is Boolean single input - single output YES logic,2,7 where the fluorescence output is driven by the target species input. Similarly, single input - single output NOT logic2,7 can also be arranged.

If we examine the two states a bit more closely, the excited state energy of the fluorophore is larger than the numeric sum of the oxidation and reduction potentials of the receptor and fluorophore respectively. When the receptor captured the target species, the oxidation potential is raised, to the point that PET is not possible so that we have fluorescence resurrection. This photoelectrochemical mechanism shows the modular behaviour52,53 of the 'fluorophore-spacer-receptor' system, which is molecular engineering in action. It is gratifying that such a design tool with several quantitative features52,53 has been taken up by around 300 laboratories.2 A snapshot of the developments of this tool during the past year or two is contained in a recent review.54

Figure 1a and 1b. Approximate world maps of the sources of molecular logic devices. Single input - single output devices have been omitted.

Figure 2. Stimulus-response curve for a molecular device. Reprinted from ref. 2.

3. Sensors are the simplest logic gate devices operated in the analog regime

The 'off-on' or '0-1' switching language of the previous section suggests binary digital molecular behaviour is being discussed. Indeed, the commonest and simplest 'mass action'-type equilibria

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clearly pass a molecule between bound and free states when it is confronted with a target species. At the limits of no and excess target species, the observable properties of the system are substantially different and distinguishable so that the binary digital aspect persists in the experimental output, even at the single molecule level.\textsuperscript{10,55-59} Additionally, many chemical tests in a clinical/commercial/managerial setting aspire to deliver a 'well/ill', 'pass/fail' or 'go/no go' decision which is binary digital anyway.

When the usual situation of large populations of molecules is considered, it is clear that the binary digital output is given up when the target species concentration is finite. Now the output property becomes smoothly tunable. Such a stimulus-response curve for a molecular device is shown schematically in Figure 2. This is the analogue regime, which is well-known in electronics.\textsuperscript{60} Indeed, the building blocks of digital electronics, e.g. diodes, triodes and transistors have their own analogue regimes. Even molecular versions of triodes show this behaviour.\textsuperscript{2,61,62}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure3.png}
\caption{Schematic representation of three common fluorescence sensing scenarios, with their Boolean logical designation.}
\end{figure}

The large literature on fluorescent sensing,\textsuperscript{50,63-66} for example, has a small number of scenarios. Three of the most common of these are shown in Figure 3. The ‘off-on’ or ‘turn on’ or ‘CHEF’ type corresponds to Boolean single input - single output YES logic. The ‘on-off’ or ‘turn off’ or ‘CHEQ’ type corresponds to Boolean single input - single output NOT logic. The ‘wavelength shift’ type corresponds to superposed YES/NOT logic.\textsuperscript{3} Superposition is a foundational concept in quantum information processing.\textsuperscript{67} Overall, it is clear that most molecular sensors (fluorescent or not) have a Boolean basis, even though they are operated in an analogue fashion.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure4.png}
\caption{‘Fluorophore-spacer$_1$-receptor$_1$-spacer$_2$-receptor$_2$’ system exemplified by 1.}
\end{figure}

A recent example would be in order at this point. This concerns a key analogue device invented during the growth of the electronics industry – the triode.\textsuperscript{60} We arrange\textsuperscript{62} a molecular photonic emulation of it, similar to an all-photonic emulation presented by Gust’s laboratory.\textsuperscript{61} It is well-known that fluorescent pH sensors possess a sigmoidal intensity-pH profile.\textsuperscript{68} As mentioned above, the input-output characteristic of the triode is also quasi-sigmoidal.\textsuperscript{69} However, this characteristic function is tunable with a third variable. Similar tuning of the sigmoidal intensity-pH profile can be arranged by employing a ‘fluorophore-spacer$_1$-receptor$_1$-spacer$_2$-receptor$_2$’ system,\textsuperscript{53} where the second receptor is not capable of engaging in any major interactions with the fluorophore (Figure 4). Now, the pK$_A$ value of the sensor becomes adjustable by electrostatic repulsion between the receptor$_1$-bound H$^+$ and another cation held by receptor$_2$ provided that the two receptors actions are orthogonal. The amine and 15-crown-5 ether receptors in 1\textsuperscript{50} satisfy this requirement. Protonation of the amine arrests PET from the amine to the anthracene fluorophore and leads to switching ‘on’ of fluorescence.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure5.png}
\caption{Fluorescence micrographs demonstrating molecular computational identification (MCID) of polymer beads. The beads are tagged with different logic gates and treated with (top) acid and (bottom) alkali in aqueous methanol (1:1, v/v) under ultraviolet (366 nm) irradiation. The logic gate types of some of the beads are discussed in the text. Reprinted from ref. 72.}
\end{figure}
The problem being solved here is one of individually identifying a large number of small objects. Being sub-millimetric, these small objects cannot be conveniently tagged with RFID chips.\textsuperscript{73} The latter, when operated with sensible electromagnetic frequencies, cannot be easily miniaturized below this size-scale. On the other hand, as shown in the previous paragraph, molecular tags can handle far smaller-sized objects. Though molecular fluorescent tags are known, the broad fluorescence signatures do not permit the handling of more than a hundred objects.\textsuperscript{74} The needs of combinatorial chemistry laboratories concern much larger numbers of objects.\textsuperscript{75,76} So we propose the use of logically-enabled molecular fluorescent tags so that each colour can produce a large diversity, each with its own logic signature, e.g. H\textsuperscript+-driven YES (6) and H\textsuperscript{2+}-driven PASS 1 (7). Their carboxylic acid groups are converted to peptide links during the object-tagging procedure. This is the technique of molecular computational identification (MCID).\textsuperscript{72} Both these gates 6 and 7 employ the same fluorophore with the same emission and excitation profiles. Since 7 contains only the fluorophore, its emission is unaffected by pH and retains PASS 1 logic. Since 6 additionally contains an amine receptor, it permits PET unless blocked by the application of ‘high’ levels of H\textsuperscript{2+}. This leads to strong fluorescence only in acid solution, i.e. H\textsuperscript{2+}-driven YES logic. These logic signatures of 6 and 7 are manifested experimentally by observing the fluorescence intensities of the tagged objects with a microscope after gentle exposure to the ‘high’ and ‘low’ levels of H\textsuperscript{2+} (Figures 5a and 5b respectively). The YES gate shows strong emission only in acid solution (beads E and I) whereas the PASS 1 gate glows constantly whatever the pH (beads A, C and G), i.e. the two gates are clearly distinguishable even though they are both displaying the same coloured fluorescence. At the level of this demonstration, there is some redundancy, i.e., several beads are carrying the same tag.

Figures 5a and 5b also contain the case where one bead D has equimolar PASS 1 and YES logic tags attached so that the summed fluorescence is seen. This produces the logic array PASS 1 + YES (1:1) where the fluorescence intensity in acid solution is double that seen in alkaline solution. This case opens up the use of various molar ratios of a given pair of logic gates so that a series of distinguishable logic signatures will result. Such double-tagging seriously increases the diversity addressable by this method. This also opens the door to ternary logic\textsuperscript{77} which, though more information rich than binary, is not trusted in conventional computers. This is because ternary and higher logic deal with numbers which are not as different as the simple ‘0’ and ‘1’ of binary. For instance, the numbers ‘1’ and ‘2’ only differ by a factor of 2. When both numbers accumulate errors of say 50\%, which can happen easily during long series of elementary computing steps within a conventional computer, they overlap and become indistinguishable, i.e., 1\textsuperscript{\pm}0.5 and 2\textsuperscript{\pm}1.\textsuperscript{78} However, our experiment involves only a few steps and the errors stay less than 10\%. So the numbers ‘0’, ‘1’ and ‘2’ are well tolerated. de Ruiter and van der Boom also exploit this low-error situation during their use of ternary logic for data storage.\textsuperscript{79,80}

![Figure 6. Effective local H\textsuperscript{2+} density (as measured by the shift of acidity constant relative to bulk water, ΔpK\textsubscript{a}) as a function of position of 7 (as measured by the local dielectric constant, \(\varepsilon\)) within an aqueous micelle solution of Triton X-100. Plotted from data in ref. 79.](image)

Even smaller space resolution within small spaces is achievable in useful contexts.\textsuperscript{79} This involves the mapping of H\textsuperscript{2+} near membranes on sub-nanometric length scales. The basic ‘fluorophore-spacer-receptor’ system is expanded by adding two terminals which allow gross and fine positional targeting respectively. Such a molecule, e.g. 8 will take up an average position in an aqueous detergent micelle which depends on the nature of these targeting units. This position can be related to the polarity that the molecule sees, since the polarity increases gradually as we move away from the micelle center along a radial line. By employing a push-pull fluorophore with substantial internal charge transfer (ICT) character in its excited state, the local polarity becomes determinable from the emission wavelength.\textsuperscript{50,65,66} Separately, the expanded ‘fluorophore-spacer-receptor’ system can measure the local H\textsuperscript{2+} density via its emission intensity. More such local H\textsuperscript{2+} density-position pairs can be obtained by employing variants of 8 with other targeting groups. Thus the spatial distribution of H\textsuperscript{2+} in the micellar milieu is revealed (Figure 6). The pK\textsubscript{a} shift in the micellar medium versus bulk water gives the local H\textsuperscript{2+} density (referred to that in bulk water). It is seen that the H\textsuperscript{2+} density decreases rapidly as we approach the micelle from bulk water.

5. Molecular logic gate arrays of increasing complexity are accumulating

The Boolean insight into the logical power of the symbols ‘0’ and ‘1’ was developed by his followers into a family of logic operations of gradually increasing complexity.\textsuperscript{81,84} Furthermore, all-electronic semiconductor logic gates can be integrated\textsuperscript{85} serially and in parallel into arrays of dizzying complexity and power which drive our current technologies. So the challenge for molecular logic-based computation is to build useful molecular logic arrays.
Parallel integration is relatively straightforward since several gates can be present in one solution so that each gate can receive its inputs respectively. The first small-molecule half-adder was built in this way. H⁺, Ca²⁺-driven AND gate 9 has a fluorescence output and functions on PET principles. H⁺, Ca²⁺-driven XOR gate 10 is used in transmittance mode at a carefully selected wavelength of 390 nm. This XOR logic action depends on the ICT (internal charge transfer) excited state of 10 being stabilized by bound H⁺ and destabilized by bound Ca²⁺ in nearly equal amounts. Though simple, this case showed that small molecules could be numeral like children by expressing the ascending number hierarchy 0, 1 and 2.

Unlike parallel integration, serial integration presents a stumbling block since most molecular logic devices use distinguishable inputs and outputs. Such input-output heterogeneity prevents the output of one logic device to be passed as input into another gate. However, there are several general avenues along which progress is being made.

The commonest of these avenues is functional integration. Instead of physically linking elementary gates, relatively complex input-output patterns are arranged within molecules outfitted with several supramolecular interactions. Several switching pathways are also allowed for. Computer science textbooks have procedures which can analyze an input-output truth table according to a minimal array of 2⁵.

Physical linking of simpler gates to result in more complex arrays is also possible. Light has been demonstrated to serve as the linker via electronic energy transfer (EET) between two gates. When such systems are endowed with separately switchable optical properties, e.g. H⁺-switched photochromics, rather complex arrays of elementary gates can emerge. Chemical species, e.g. H⁺, metal ions and O₂, have also been shown to serve as the linker between gates. For instance, once switched with a dose of uv light, the photochromic 11 transfers a H⁺ to 12. This H⁺ transfer is signalled by a change in the uv-visible absorption spectrum of 12, which is the origin of the output(s).

The use of Zn²⁺ as a gate linker is illustrated by Akkaya's 13 and 14. 13 represents 'caged' Zn²⁺ which is released upon the supply of a dose of uv light absorbable by 13. Once liberated into solution, Zn²⁺ has the chance to bind to the receptor moiety of 14, so that its fluorescence can be switched 'on' and be observed as the output.

Akkaya goes further by applying a non-ionic messenger, O₂, between gates. H⁺, light dose-driven AND gate 15 produces O₂ as output only under acidic conditions when light of a carefully selected wavelength (660 nm) is light applied. 15 absorbs this light only when it is in the protonated (phenol) form but not when it is in the deprotonated (phenolate) form. Upon light absorption, the lowest singlet excited state of 15 quickly evolves to its lowest triplet excited state owing to the heavy atom nature of the internal iodine atoms. This, in turn, transfers its energy to form O₂ from ubiquitous O₂.

The integration of gate 15 with gate 16 is facilitated by placing them in a soap micelle in D₂O (where the lifetime of O₂ is extended). 16 contains an intramolecular pair of fluorophores so that the donor’s emission at 537 nm is hardly seen due to EET to the acceptor. However, O₂ destroys the alkenic connection between the two fluorophores so that EET virtually ceases and 537 nm emission emerges strongly. Since glutathione would be a sacrificial protector of 16, we have a O₂, glutathione - driven INHIBIT(glutathione) gate where glutathione is the disabling input.

The Krebs cycle of early biochemistry classes is a reminder to us that the product from one enzyme can serve as the substrate for the next enzyme. Since enzyme-based logic is well-developed, this path can be used to cascade enzymes to produce biomolecular logic arrays. For example, Willner, Katz and their colleagues combine acetylcholine esterase, choline oxidase, microperoxidase and glucose dehydrogenase to achieve the minimized gate array shown in Figure 7. The selectivity of acetylcholine esterase is not so extreme. So it hydrolyzes acetylcholine and butyrylcholine with comparable efficiency in an OR logical manner. The product, choline, is seized by the next enzyme, choline oxidase, if dioxygen is supplied as the oxidant. H₂O₂ is produced from this step according to choline, O₂-driven AND logic. The third enzyme, microperoxidase, uses H₂O₂ to oxidize NADH, while the fourth enzyme, glucose dehydrogenase, processes glucose with the aid of NAD⁺. Another publication from the same laboratory shows how a combination similar to the third and fourth enzymes leads to XOR logic behavior when the NADH concentration is monitored under certain conditions.

The success of enzymes outlined in the previous paragraph can be emulated by oligonucleotides. DNA-based logic gate arrays with serial integration depend on strand displacement by another strand with a longer run of hybridization. This depends on a duplex containing an overhang region, which can serve as a toehold for the encroaching strand. Indeed, the inputs, outputs and devices are all composed of oligonucleotides. Even solid-phase versions are available.

At a larger scale-size, cuvet arrays and microtiter plates are also playing a part in the drive towards higher serial integration of molecular gates. Raymo and Giordani employ photochromics in cuvet arrays and measure optical transmittance of the reading light through the queue of cuvets, while dosing each cuvet independently with the writing light as inputs. Choosing such queues in 2- and 3-dimensional cuvet arrays can extend this approach further. Szcaliowski uses environmentally-sensitive
colour-forming reactions towards the same end via a similar tactic, but creates more complexity through the environmental variables, e.g. ion concentration, ionic strength etc. Schiller translates each serial connection of a chosen logic array expressed exclusively in terms of IMPLICATION gates into an algorithm for pipetting input species into wells containing the molecular IMPLICATION logic device in a microtiter plate, while exploiting the ‘universal’ or ‘complete’ nature of the gate pair of IMPLICATION and PASS 0. The ‘universal’ nature of the NAND or NOR gates are widely exploited in the semiconductor industry during integrated circuit manufacture.

6. Molecular logic-based computation at the human level is now possible

A part of our (and animal) visual attention process is the rapid detection of edges of approaching objects. This is critical for our survival and hence its presence deep within our nature. This is how we quickly judge approaching objects according to our expectation from memory so that we can make an appropriate response. Here is an experiment that the reader can do to directly feel this truth. This is an experiment that many of us do often, rather inadvertently. We sit in a bus shelter waiting for the bus to come round the corner in the road some distance away. Sometimes we spot a tall profile growing around the corner within milliseconds, and our leg muscles tense and raise us off the seat. This is the edge detection in our eyes and brains kicking-in, concluding rapidly that the tall profile seeking round the corner matches the tall profile of a bus (as compared to the many cars on the road). But then, as more of the object emerges from round the corner, its details show that it is not the bus but only a lorry. We sink into the seat again. This is the slower, but more comprehensive, computation being conducted centrally in our brains. We refer the reader to detailed psychological tests concerning objects approaching at moderate speeds, which confirms this analysis.

Edge detection is also an important activity in machine vision, as well as in image processing software. For instance, the Canny algorithm exploits the large gradient of light intensity at the edge. When the Canny algorithm is run on a picture, pixels are raster-scanned and central differences are taken (meaning the intensity of the pixel ahead minus the intensity of the pixel behind in the horizontal line) after each pixel has been averaged in a Gaussian distribution with intensities in pixels vertically above and below. Then all pixels which display a higher central difference than a chosen threshold are declared as edge pixels. A further check of contiguity is applied so that isolated edge pixels are declared as ‘false positive’ and rejected. It is crucial to note that the Canny (and similar) algorithms require a substantial ‘stored program’ computer with a graphical user interface. A small-scale integrated logic gate array will not suffice. This relative complexity is in keeping with the deep-seated human/animal nature of edge detection.

Amazingly, such edge detection can be arranged in genetically-engineered bacteria and also in reactive DNA networks. Still, it would be remarkable if small molecules devoid of any connection with life could perform the same feat. This has been achieved very recently by employing a small molecular logic system composed of a fluorescent pH ‘off-on’ sensor (of the YES logic type) and a photoacid generator on oligonucleotides, enzymes and small molecules to come together and pool intellectual resources. Such a common front would provide usable insights for gene-, cell- and DNA reaction network-based information processing. Then the baby steps that we all have taken until now could develop into bigger strides.

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Notes and references

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Constructs of fluorophores, receptors, spacers, $^{1}O_2$ sensitizers, enzymes and oligonucleotides play their part in advancing the field of molecular logic-based computation.

Biography

The authors came to study for their PhD at Queen’s University Belfast, Northern Ireland, from places as far apart as Zhenjiang, Belfast, Carrickfergus and Colombo. Besides the chemistry day jobs, Brian (back left) brings up his two daughters, Jue (back centre) plays basketball, Victoria (front) rides her horses and AP (back right) plays percussion with an Irish traditional band.