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Seismic damage detection for a steel braced frame structure

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A new approach for global detection of seismic damage in a single-storey steel concentrically braced frame (CBF) structure is presented. The filtered lateral in-plane acceleration response of the CBF structure is integrated twice to provide the lateral in-plane displacement that is used to infer buckling and yielding damage. The level of interstorey drift of the CBF during a seismic excitation allows the yield and buckling of the bracing members to be identified and indirectly detects damage based on exceedance of calculated lateral in-plane displacement limits. A band-pass filter removes noise from the acceleration signal followed by baseline correction being used to reduce the drift in velocity and displacement during numerical integration. This pre-processing results in reliable numerical integration of the frame acceleration that predicts the displacement response accurately when compared to the measured lateral displacement of the CBF structure. Importantly, the structural damage is not assumed through removal of bracing members, rather damage is induced through actual seismic loading. The buckling and yielding displacement threshold limits used to identify damage are demonstrated to identify accurately the initiation of buckling and yielding.

Notation

a_g	peak ground acceleration
A	cross-sectional area of the section
b	width of the section
E	Young's modulus of the structural steel
F_c	brace member compression force
F_t	brace member tension force
G	torsional modulus
I	second moment of area of the section
I_y	minor axis second moment of area of the section
I_z	major axis second moment of area of the section
K	lateral in-plane frame stiffness
L_{cr}	effective length of a compression member
N_{cr}	Euler buckling capacity of a brace member
P	lateral in-plane frame force
r_y	radius of gyration about the weak axis
t	thickness
δ	lateral in-plane frame deflection
θ	angle of inclination of the bracing to the horizontal axis
$\bar{\lambda}$	bracing member's non-dimensional slenderness

1. Introduction

Seismic damage detection in building structures enables engineers to assess the safety and allowable occupancy of a building during/after an earthquake event. Seismic damage detection can be categorised as pre and post-damage methods (mostly performed offline) or structural health monitoring (SHM) methods (online). The detection methods can then be further categorised as global (detect storey location of damage) or local (detect location of damage in individual structural members). This paper presents an offline global damage detection strategy for a steel concentrically braced frame (CBF) structure.

In steel CBF structures the buckling of the bracing members is typically visually detectable after a moderate seismic event; however, it may not be obvious if the bracing has yielded, and to what extent. If buckling alone exists, the frame may have adequate capacity for moderate aftershocks/wind loading as long as the residual interstorey drift is sufficiently low. If bracing members had buckled but not yielded during a seismic event, the structure could be deemed to be safe to be occupied until repair or replacement could be performed. Therefore, it is important to know if buckling and/or yielding are present in the bracing members. The majority of previous damage detection research in steel CBF structures assumes damage in bracing members through removal of members. This assumes that the bracing member has fractured. Such an assumption ignores structural response up to fracture. However, many damage scenarios in small to moderate earthquakes exist where the bracing members do not fracture but either buckle and do not yield, or buckle and yield. In this paper, damage is induced through seismic excitation of the structure.

Global methods of damage detection that track model parameters such as mode shapes (Hearn and Testa, 1989; Yao *et al.*, 1992) interstorey drift (Skolnik and Wallace, 2010), storey stiffness (Koh *et al.*, 1992), finite-element model updating techniques (Wu and Li, 2006) and purely statistical approaches (Krishnan Nair *et al.*, 2006) have been shown to be successful, if sometimes problematic. The most common global method of damage detection is interstorey drift tracking because the double integration of readily available acceleration data can be performed. Such vibration-based methods are typically based on the principle that damage will cause detectable changes in the modal properties of the structure.

Changes in physical properties such as mass, stiffness or damping will result in detectable changes in modal properties such as frequency, mode shapes or modal damping (Fan and Qiao, 2011). Extensive literature reviews on vibration-based methods have been written by Doebling *et al.* (1996), Sohn *et al.* (2003) and Carden and Fanning (2004).

Many researchers (Ching and Beck, 2004; Johnson *et al.*, 2004; Kharrazi *et al.*, 2002; Mikami *et al.*, 2007) have investigated methods of SHM/damage diagnosis for the scaled four-storey, two-by-two bay, steel braced frame ASCE structural health monitoring task group benchmark damage structure (IASC-ASCE, 1999). Varying levels of damage scenarios were tested, with damage consisting of removal of single or multiple brace members. Kharrazi *et al.* (2002) studied the output-only vibration from the tests using finite-element model updating to identify global damage through changes in modal properties. Ching and Beck (2004) used pre and post-damage modal parameters based on Bayesian model updating to identify damage through hammer or ambient vibrations. The method was successful for member damage but less successful for connection damage. Mikami *et al.* (2007) tested blind excitation using a power spectral density data technique to identify a greater number of modes with the potential of improving the accuracy of detection. Hera and Hou (2004) investigated a non-modal-based method of damage detection using wavelets.

Aside from the IASC-ASCE benchmark structure, others have also investigated damage detection in steel braced frame structures. Morita *et al.* (2001) investigated damage in a scaled five-storey steel braced frame structure through variation of modal parameters pre and post-damage. Damage included loosening bolts, removal of brace members and cutting parts of beams. Sometimes their methods were successful at globally locating the storey damage, others not. Xiadong *et al.* (2007) simulated damage through removal of braces in a scaled two-storey steel braced frame structure. Mode shapes of the undamaged structure were modelled using finite-element models while the damage index method and damage locating vectors method were used to identify localised damage and severity. Sabatino and Ervin (2012) used the natural frequencies and mode shapes of an idealised steel/aluminium braced frame structure with/without damage to assess the effectiveness of different detection parameters. The baseline undamaged frequencies and mode shapes were compared to the structure with brace members removed (damaged). Six unique damage indicators were used to assess damage based on change in modal properties.

This paper describes a new practical strategy to assess initiation of global damage in a single-storey steel CBF structure using a single relative lateral in-plane acceleration signal. The acceleration signal is filtered and integrated twice to provide a reliable predicted lateral in-plane displacement response. Lateral in-plane displacement thresholds based on calculated buckling and yielding displacement limits are then used to identify the initiation of

buckling and yielding in the CBF structure. Test results of measured displacement and strains are compared to displacement limits and demonstrate the accuracy and applicability of the strategy. Importantly, damage is not initiated through removal of bracing members, but through actual seismic loading. The strategy proposed here does not rely on detectable changes in response; rather it measures the level of interstorey drift to infer damage. The offline procedure demonstrated has been shown to be successful and could, with a change to the filtering processes (e.g. use of a Kalman filter (Kalman, 1960)), potentially be implemented in an online procedure to detect damage globally.

2. Braced frame details

The structural frame investigated in this paper was designed as part of a larger three-storey CBF structure to resist an earthquake with a peak ground acceleration, $a_g = 3.5 \text{ m/s}^2$. The structure was designed using the lateral pushover method of analysis in BS EN 1998-1:2004 (CEN, 2004). The test frame comprises a ground-storey frame from the larger structure and comprises a $356 \times 140 \times 36 \text{ mm}$ universal beam (UB) beam and two $203 \times 203 \times 46 \text{ mm}$ universal column (UC) columns (as per Figure 1). Two sets of tests were conducted with bracing tested as follows; $30 \times 30 \times 3 \text{ mm}$ square hollow section (SHS) with normalised slenderness, $\bar{\lambda} = 1.68$ or $50 \times 30 \times 3 \text{ mm}$ rectangular hollow section (RHS) with $\bar{\lambda} = 1.57$. The section properties of the bracing members are shown in Table 1. The brace sizes are within the BS EN 1993-1-1:2005 (CEN, 2005) normalised slenderness limits of $1.3 < \bar{\lambda} \leq 2.0$. The steel properties are $f_y = 235 \text{ N/mm}^2$, $E = 210\,000 \text{ N/mm}^2$ and $G = 150\,000 \text{ N/mm}^2$. The $203 \times 203 \times 46 \text{ mm}$ UC stub column sections located at the support and beam-column connections were used to replicate pinned connections. A series of displacement controlled seismic tests was performed that is described in more detail in the next section. The strain gauges are located on the front and top face of the bracing sections at locations of suspected buckling as shown in Figure 1. Strain gauge (SG) 4 is located on the front face of the brace section and SG 5 is located on the top face of the brace section. SG 4 and 5, SG 6 and 7, SG 8 and 9 and SG 10 and 11 are located on the front and side of the bracing members at the

Figure 1. Steel concentrically braced test frame with idealised pinned connections and test instrumentation details

Section dimensions: mm	t : mm	A : cm ²	b/t	d/t	I_z : cm ⁴	I_y : mm ⁴	r_y : cm	λ
30 × 30	3	3.01	8	8	3.5	3.5	1.08	1.68
50 × 30	3	4.34	8	14.7	13.6	5.94	1.16	1.57

Table 1. Hot-rolled steel bracing cross-sectional properties

expected location of plastic hinge formation. These strain gauges are located to record the maximum strain in the bracing members. The location of the displacement sensors (linear variable differential transformer (LVDT) 1 and LVDT 2), load cell (LC 1) and numerically modelled lumped masses (LM 1 and LM 2) can also be seen in Figure 1. LVDT A measures the in-plane lateral frame displacement and is located internally in the actuator. LVDT B is an external LVDT and measures the out-of-plane brace displacement at the crossing of the bracing members as shown in Figure 1. SG 1 and SG 3 measure the axial strain in the columns, whereas SG 2 measures the axial strain in the beam.

In order to provide context, the structural behaviour of a pin-ended single brace member subjected to low cycle loading, during one load cycle is briefly described herein. Initially when a brace member is loaded in compression, the member axially shortens and deflects out of plane at mid-span as a result of initial imperfections. When the maximum compressive load is reached, the brace buckles and continues to deflect out of plane at mid-span to accommodate increased axial displacement. A plastic hinge forms at mid-span, leading to reduced axial load capacity. On load reversal to tension loading, elastic recovery occurs and the brace straightens. The unloaded branch from compression to tension has a lower stiffness than the initial compression loading phase owing to the presence of residual displacements. Tensile yielding then occurs when the loading continues past yield and the brace has straightened. Elastic unloading then occurs when the load reverses to compression. Buckling of the brace will then occur at a reduced load below the maximum compression load owing to the residual deflections in the brace member.

3. Test procedure

The hybrid test method adopted in this paper is a dynamic testing method that combines physical testing and simultaneous numerical modelling (McCrum and Broderick, 2013a, 2013b). A hybrid test was performed with the masses numerically modelled and the CBF physically tested (essentially a pseudo-dynamic test (refer to Shing and Mahin, 1984). The single-storey CBF structure was supported off a reaction frame as shown in Figure 2, and therefore the measured displacements and thus accelerations are absolute frame accelerations. The test frame is located between two side-by-side reaction frames. The actuator applies the command displacement to the frame as shown in Figure 2. The lumped masses were numerically modelled at the ends of the beams (refer to Figure 1).

The inertial displacement resulting from the excitation was applied to the structure in a displacement controlled test using closed-looped proportional integral derivative control. The MTS actuator has a 150kN capacity with a stroke of ± 125 mm. An internally mounted displacement sensor provides the actuator displacement and an internal load cell provides the force feedback. Tests are performed at an expanded timescale, with the acceleration and velocity numerically calculated from the equation of motion using the measured force and displacement from each time step of the time history. At the first time step, the target displacement of the test frame resulting from the earthquake ground motion is calculated from the equation of motion. The first time step target displacement is purely numerically calculated. The target displacement is applied by the actuator and the resulting force and displacement are measured at the end of the time step. In the second time step, the resulting force and displacement that have been measured by the actuator load cell (LC 1) and displacement sensor (LVDT A), respectively, at the end of the first time step are then input into the equation of motion as a physically measured force and displacement. The third time step uses the displacement and force measured from the end of the second time step to calculate the next target displacement. The procedure continues until the end of the earthquake record. Each time step is 0.01 s. The test

Figure 2. Experimental set-up showing side-by-side reaction frames with braced frame and actuator inset in between reaction frames

runs for approximately 700 s in actual time, which equates to 40 s of the input earthquake record. The test is referred to as a pseudo-dynamic test because it does not occur in real time.

The Taiwan (1986) earthquake time history scaled to 0.4, 1.0 and 2.0 was used as the input ground acceleration as shown in Table 2. The Taiwan earthquake had a magnitude of 7.3, was recorded a distance of 39 km from its epicentre and had a peak ground acceleration (PGA) of 0.153g. Two different numerically modelled masses were applied to the braced frame as shown in Table 2. The 50 × 30 × 3 mm RHS frame has a larger seismic demand due to the increased lumped masses. P-delta tests at low amplitude elastic displacements were performed to obtain lateral in-plane frame stiffnesses as shown in Table 2. Tests 1 to 3 used the same bracing specimen during all tests and likewise tests 4 to 6 used the same bracing specimen during all tests. The re-use of the test frame in subsequent tests is evident as the stiffness softens slightly after each test, as shown in Table 2.

4. Damage detection strategy

The proposed damage detection strategy consists of three parts: (a) filtering and baseline correction of acceleration response and then double numerical integration of the corrected signal to give the predicted displacement; (b) identification of buckling by checking the predicted displacement against buckling displacement threshold limits; and (c) identification of tension yielding by checking the predicted displacement against yield displacement threshold limits.

The brace members have been designed according to BS EN 1998-1:2004 (CEN, 2004) and are designed to resist seismic loading through tension only; however, in practice compressive resistance exists. The low cycle fatigue and residual deformations in the bracing result in reduced buckling capacity of the bracing during multiple compression loading cycles. Also, tension yielding in the bracing results in yielding occurring at a reduced stress in subsequent load cycles, thus reducing the tension carrying capacity of the bracing member in subsequent load cycles. As the structure has been designed to resist lateral loading through tension only the yielding identification is

Test no.	Test type	Scaling factor	Brace size: mm	Nodal masses: kg	Stiffness: N/mm ²
1	Elastic	0.4	30 × 30 × 3	45 634	9805
2	Inelastic	1.0	30 × 30 × 3	45 634	9846
3	Inelastic	2.0	30 × 30 × 3	45 634	9379
4	Elastic	0.4	50 × 30 × 3	46 924	11 408
5	Inelastic	1.0	50 × 30 × 3	46 924	11 157
6	Inelastic	2.0	50 × 30 × 3	46 924	10 733

Table 2. Experimental programme and details

more important than the buckling identification in terms of damage detection of the CBF structure.

4.1 Procedure

The methodology of the damage detection strategy is outlined as follows.

- Filter recorded acceleration signal using a band-pass filter to remove noise from the relevant frequency band of interest.
- Perform a polynomial baseline correction on the acceleration signal and numerically integrate the corrected acceleration twice to yield the predicted displacement.
- Compare predicted displacement with measured test displacement and ensure within acceptable error bounds.
- Calculate the buckling displacement and compare to predicted displacement to identify buckling. The Euler buckling capacity, N_{cr} is calculated from

$$1. \quad N_{cr} = \pi^2 EI / L_{cr}^2$$

where E is the Young's modulus, I is the second moment of area of the section and L_{cr} is the effective length of the compression member. The brace member end connections are assumed as pinned-pinned. $N_{cr} = 37.4$ kN for 30 × 30 × 3 mm SHS and $N_{cr} = 41.61$ kN for 50 × 30 × 3 mm RHS. These forces correspond to a lateral frame displacement calculated as follows.

- The tension force in the tension bracing member, F_t and compression force in the compression bracing member, F_c are assumed to be equal up until buckling that is $F_c = F_t$. Therefore, the lateral frame force, P (actuator force) corresponding to yield is equal to

$$2. \quad P = (F_c + F_t) \cos \theta$$

$$\text{as } F_c = F_t$$

$$3. \quad P = (N_{cr} + N_{cr}) \cos \theta = 2N_{cr} \cos \theta$$

where θ is the angle of inclination of the bracing to the horizontal axis.

- Using Equation 3, the lateral frame force is $P = 41.47$ kN for the 30 × 30 × 3 mm SHS frame and $P = 66.46$ kN for the 50 × 30 × 3 mm RHS frame. Knowing the lateral frame stiffness, K (from Table 1) and using; $\delta = P/K$, the lateral displacement inducing buckling can be calculated. For example, the expected buckling displacement for test 3 is 4.44 mm.

- The first yield displacement of the frame can be calculated in a similar manner to step (d); however, the tension and compression forces in the bracing cannot be assumed to be

equal as the yield capacity of the brace member is greater than its buckling capacity. The initial buckling capacity of the brace member reduces during subsequent load cycles as a result of residual out-of-plane deformation. The maximum compressive force in the bracing members therefore reduces in subsequent load cycles. In Goggins (2004), cyclic tests were performed on similar brace members 1.1 m long of section size $20 \times 20 \times 2.0$ mm SHS ($\bar{\lambda} = 1.6$, $r_y = 0.727$ cm), $50 \times 25 \times 2.5$ mm RHS ($\bar{\lambda} = 1.2$, $r_y = 0.994$ cm) and $40 \times 40 \times 2.5$ mm SHS ($\bar{\lambda} = 0.8$, $r_y = 1.52$ cm); where r_y is the radius of gyration about the weak axis. The average buckling capacity in subsequent load cycles of the $20 \times 20 \times 2.0$ mm SHS (total of 22 cycles), $50 \times 25 \times 2.5$ mm RHS (total of 14 cycles) and $40 \times 40 \times 2.5$ mm SHS (total of 12 cycles) was approximately 52%, 58% and 67% that of the initial buckling capacity, respectively. These values were then used as a guide to estimate the reduced buckling capacity of the bracing members in this paper. Therefore, for the $30 \times 30 \times 3$ mm SHS and $50 \times 30 \times 3$ mm RHS sections used in these tests, the buckling capacity was reduced by an average estimated 50% and 60% for the $30 \times 30 \times 3$ mm SHS ($\bar{\lambda} = 1.68$ and $r_y = 1.08$ cm) and $50 \times 30 \times 3$ mm RHS ($\bar{\lambda} = 1.57$ and $r_y = 1.16$ cm), respectively. For example, $F_c = 0.5N_{cr}$ for $30 \times 30 \times 3$ mm SHS and the lateral frame force corresponding to yield is

$$4. \quad P = (F_c + F_t) \cos \theta$$

and as $F_c = 0.5N_{cr}$

$$5. \quad P = (0.5N_{cr} + F_t) \cos \theta$$

Using Equation 5, the lateral frame force is $P = 69.37$ kN for test 3 for the $30 \times 30 \times 3$ mm SHS frame and $P = 101.4$ kN for test 6 for the $50 \times 30 \times 3$ mm RHS frame. Knowing the lateral frame stiffness, K (from Table 1) and using; $\delta = P/K$, for test 3 for example, the $30 \times 30 \times 3$ mm SHS bracing tension yielding occurs at 7.38 mm corresponding to a brace tension force of 73.8 kN. Similarly, for test 6 the $50 \times 30 \times 3$ mm RHS bracing tension yielding occurs at 9.45 mm corresponding to a brace tension force of 101.99 kN.

- (f) Compare predicted displacements with displacement limits for buckling and yielding in order to infer the existence of structural damage.

4.2 Reconstruction of displacement response from acceleration data

Reliable reconstruction of displacement time history from noise-corrupted experimental acceleration signals requires careful design of an appropriate pre-processing procedure, in order to 'clean' the data from errors introduced by measurement noise and numerical manipulation. In this paper, the recorded signal is firstly filtered and baseline corrected to

eliminate random high-frequency noise and low-frequency trends. The corrected acceleration is then integrated twice to retrieve the corresponding displacement signal. Subsequently, it is shown that a scaling gain can be conveniently applied to cater for numerical integration errors and further improve the agreement between the measured and the predicted displacement.

The first step in reconstructing the displacement signal is to deal with the issue of noise. Measurement noise in the acceleration signal results in inaccurate integration of undesired components of vibration, which are associated with intrinsic instrument error and non-linearities. In order to mitigate the effect of low-frequency drift and high-frequency measurement noise, a band-pass filter with appropriate cut-off frequencies is designed and applied to the acceleration signal. The frequency content of the recorded waveform is therefore analysed to select the cut-off frequencies of the filter.

Figure 3(b) shows the fast Fourier transform of the test frame acceleration recorded during the time history for test 3 (Figure 3(a)). As shown in Figure 3(b), the fundamental frequency of the structure was approximately 3 Hz. A band-pass filter with cut-off frequencies of 0.01 Hz and 25 Hz was applied to all acceleration signals. This filtering is beneficial for the reconstruction of the displacement time history from measured acceleration as it allows the useful signal to be separated from the noise and a linear frequency response to be obtained. Figure 4 shows the original and filtered acceleration signal for test 3. As expected, the band-pass filter is shown to smooth the signal and removes the higher frequencies.

In general, linear filtering alone is not sufficient to correct recorded acceleration signals that are integrated to give displacement. It is well known that direct integration of acceleration data may lead to unrealistic results for velocity and displacement, owing to initial baseline errors (Boore, 2001; Chiu, 1997; Trifunac, 1971; Wang, 1996). Chiu (1997) discusses different sources of errors that can be identified to explain the drifts in velocities and displacements computed by directly integrating raw acceleration records, including digitisation errors, low-frequency instrument noise, low-frequency background noise and mechanical or electrical hysteresis in a sensor. Baseline errors in particular have been shown to cause severe drifts if appropriate pre-processing schemes are not adopted (Yang *et al.*, 2006). In fact, although the shifts in the baseline (zero level) are negligible in the acceleration signal, they may have a dramatic impact in computing the corresponding velocity and displacement waveforms. The double integration of the raw acceleration signal in test 3 is shown in Figure 5(a). A significant drift in the numerical displacement is clearly observed when compared to the measured frame displacement.

A comparison of different filtering techniques for dealing with baseline offsets in seismic accelerograms can be found in

Figure 3. (a) Taiwan ground acceleration time history scaled to 2.0 PGA for test 3; and (b) fast Fourier transform of the measured acceleration time history for test 3

Figure 4. Original and filtered lateral in-plane acceleration signal with band-pass filter for test 3; (a) full signal and (b) close up

Crespellani *et al.* (2003). In this paper, a signal pre-processing scheme consisting of (a) band-pass filtering and (b) polynomial baseline correction of the acceleration and velocity time series is implemented in order to reconstruct the lateral displacement of the test frame. Correction of the baseline is performed using a polynomial least squares approach. The baseline component in the acceleration is fitted with a fifth-order polynomial and subtracted from the original waveform. The baseline-free acceleration is then integrated twice to obtain the corresponding displacement response. The double integration of the corrected acceleration signal in test 3 is shown in Figure 5(b). As is evident in the comparison of Figure 5(a) and (b), baseline correction represents an essential step in retrieving useful information from low-frequency acceleration signals.

For the purpose of illustration, the numerical (predicted) and the measured lateral in-plane frame displacement in test 3 are plotted in Figure 6(a). A high level of agreement between the predicted and the measured response is observed. For the six tests considered in this paper, the results of the application of the proposed methodology, denoted as filtered corrected integrated (FCI) scheme, are illustrated in Table 3. By comparing the measured and the FCI reconstructed displacement, a mean peak displacement error of 13.6% and a mean root mean square (RMS) displacement error of 13.5% are attained. The proposed scheme is therefore capable of providing a realistic quantitative prediction of the actual displacement response of the structure. Online implementation of the FCI scheme is also straightforward, as the data can be filtered during acquisition

Figure 5. Direct double integration of lateral in-plane acceleration signal (numerical) compared to measured displacement for test 3; (a) without baseline correction and (b) with baseline correction

Figure 6. Lateral in-plane frame displacement plotted against time in test 3 from 20 to 25 s; (a) without scaling gain (FCI); and (b) with scaling gain (FCIG)

Test no.	Peak disp. measured: mm	Peak disp. filtered: mm	Peak disp. Error: %	RMS disp. measured: mm	RMS disp. filtered: mm	RMS disp. error: %
1	3.92	4.44	13.46	0.59	0.68	15.22
2	9.94	11.41	14.77	1.95	2.25	15.20
3	19.59	22.77	16.23	2.97	3.42	15.24
4	4.03	4.51	12.03	0.78	0.88	11.58
5	10.24	11.57	12.99	1.93	2.17	12.10
6	20.24	22.69	12.09	3.53	3.95	11.82
		Mean	13.6		Mean	13.53
		COV	2.24		COV	2.89

Table 3. Peak and RMS error between measured and FCI displacement

and a windowed baseline correction operation can be easily performed. Online drift compensation methods based on wavelets (Hui *et al.*, 2003) or Kalman filtering (Mneimneh *et al.*, 2006; Wenzel *et al.*, 2011), could be also applied.

Observation of the results in Table 3 indicates that a slight overestimation of the response is obtained using the FCI method for the cases considered. This observation suggests the presence of an error in the numerical integration of the acquired acceleration samples. In fact, the use of a finite time step for the numerical integration causes an approximation in the solution that depends on the size of the integration time step with respect to the time constants of the system. The time step during the tests was 0.01 s and a smaller time step would have resulted in improved accuracy of the numerical integration.

An additional parameter can therefore be introduced to mitigate the integration errors that affect the predicted displacements obtained with the FCI method. To this end, a constant scaling gain is applied to the FCI reconstructed displacements to improve further the agreement between the measured and the predicted numerically computed response. As shown in Figure 6(b), excellent improvement of the performances can be achieved by appropriately scaling the integrated displacement. The proposed method with application of the scaling gain is referred to as filtered corrected integrated gain (FCIG). The results illustrated in Table 4 show that for the cases considered in this paper a scaling gain of 0.88 provides excellent agreement between the measured and the predicted response, with peak displacement errors and RMS displacement errors in the order of 1%. A high level of accuracy is therefore achieved in reconstructing the lateral displacement of the frame structure starting from the measured acceleration data.

4.3 Verification of damage identification strategy

The in-plane lateral displacement response of the CBF in test 3 subjected to a 2.0 scaled Taiwan excitation is shown in

Figure 7(a). Peak displacements of 16.3 mm and −19.7 mm occur at approximately 15 s of the time history. The out-of-plane displacement of the crossing point of the bracing members (LVDT B in Figure 1) can be seen in Figure 7(b) to peak at approximately ± 10 mm also after 15 s duration of the time history.

4.3.1 Identification of brace member buckling

Figure 8(a) shows the first 7 s of the lateral in-plane displacement response of test 3. The actuator load against in-plane lateral displacement of the cycles for the first 6.5 s is shown in Figure 8(b) (up to the point of unloading after point D in Figure 8(a)). The Euler buckling load is highlighted in Figure 8(b). The hysteresis plot of Figure 8(b) indicates buckling at displacements of 4.44 mm corresponding above a lateral in-plane (actuator) force of 41.74 kN. The negative displacement at point D of −6.3 mm is slightly larger in amplitude than the displacement at point C, hence the skewed appearance of the hysteresis plot. No buckling is observed in the hysteresis plot at points A and B as the structure remains linear. For cycles above ± 4.44 mm at points C and D, slight non-linearity in the hysteresis plots can be seen in this compression and tension cycle. No yielding was observed in the strain gauge measurements (SG 4–11) during the first 7 s of test 3. Hence, the non-linearity in the hysteresis plot indicates buckling of the bracing members.

4.3.2 Identification of brace member yielding

Figure 9(a) shows the lateral in-plane displacement response of test 3 from 11 to 16 s of the time history. Figure 9(b) shows the hysteresis plot for the E to F displacement cycle occurring at approximately 12 s. The yield displacement was calculated at 7.38 mm. Point E corresponds to a displacement of 9.51 mm and is above the predicted yield displacement as can be seen in Figure 9(b). Point F corresponds to a displacement of −7.54 mm and is shown just to reach yielding as can be seen in Figure 9(b). During the positive displacement cycle yielding can be seen to occur as the hysteresis plot becomes non-linear.

Test no.	Peak disp. measured: mm	Peak disp. filtered: mm	Peak disp. error: %	RMS disp. measured: mm	RMS disp. filtered: mm	RMS disp. error: %
1	3.92	3.91	0.15	0.59	0.60	1.39
2	9.94	10.04	1.00	1.95	1.98	1.38
3	19.59	20.04	2.28	2.97	3.01	1.41
4	4.03	3.97	1.40	0.78	0.77	1.80
5	10.24	10.18	0.56	1.93	1.90	1.34
6	20.24	19.96	1.35	3.53	3.48	1.59
		Mean	1.12		Mean	1.49
		COV	0.46		COV	0.03

Table 4. Peak and RMS error between measured and FCIG displacement

Figure 7. (a) In-plane lateral displacement response of test 3 frame at LVDT A (refer to Figure 1); and (b) out-of-plane displacement of bracing in test 3 at LVDT B (refer to Figure 1)

Figure 8. (a) Lateral in-plane displacement plotted against time for test 3 from 0 to 7 s; and (b) lateral in-plane load (actuator) plotted against displacement hysteresis plot for test 3 from 0 to 6.5 s

The hysteresis plot straightens on load reversal and some non-linearity can then be seen towards the peak of the negative displacement cycle at point E.

Strain results are shown for SG 4, 5, 8 and 9 in Figure 10 because these sections of the bracing members have a slightly larger effective length than the upper portion of the bracing (refer to Figure 1 for strain gauge locations). The effective length of the bracing between the column and central connection is greater than the effective length of the bracing from the central connection to the beam. First yielding was observed in the hysteresis plot for test 3 at approximately 12 s (see Figure 9). From Figure 10(a) and (b), it can be seen that the peak strain is close to yield at this point in time (points G and H in Figure 10(a) and (b), respectively), however does not

quite reach yield. The error between the calculated and measured strain at SG 9 is 8.1% (point H in Figure 10(b)).

As can be seen from Figure 10(a) and (b), yielding occurs in the bracing member at approximately 15 s in all strain gauges. Tension yielding was calculated to occur at a lateral in-plane displacement of 7.38 mm and should have been observed at point G in Figure 10(a) and point H in Figure 10(b) corresponding to point E in Figure 9(a). The strain data in Figure 10 demonstrate the accuracy of the lateral displacement at almost predicting first yield in the bracing. As can be seen in Figure 10(a) and (b), the large amplitude displacement cycles at 15–16 s result in considerable permanent damage in the bracing as the permanent strain remains above yield in all strain gauges.

Figure 9. (a) Lateral in-plane displacement plotted against time for test 3 from 11–16 s; and (b) lateral in-plane load (actuator) plotted against displacement hysteresis plot for first yield cycle in test 3 at approximately 12 s

Figure 10. Strain plotted against time for test 3 for: (a) strain gauges 4 and 5; and (b) strain gauges 8 and 9

The damage in the bracing at the end of test 3 can be seen in Figure 11(b). A comparison of the undamaged CBF structure before test 1 can be seen in Figure 11(a). Permanent in and out-of-plane buckling is evident in Figure 11(b) after test 3.

The qualitative and quantitative summary of the results of all six tests is shown in Table 5. Qualitatively, the first visual observation of buckling during the tests was noted during each test and coincided with the predicted buckling displacement. Quantitatively, the predicted yield displacement is compared to strain gauge data and shown on average to predict first yield with an error of 2.9% as can be seen in Table 5. No error was

observed in test 5 or test 6 as the measured yield strain coincided with the expected yield displacement.

5. Conclusion

This paper has presented a vibration-based seismic damage detection strategy for a single-storey steel CBF structure. A band-pass filter was used to remove noise from the acceleration signal followed by baseline correction being applied to reduce the drift in velocity and displacement during numerical integration. This pre-processing resulted in reliable numerical integration that predicts the displacement response accurately when compared to the measured lateral displacement of the

Figure 11. (a) Photograph of undamaged frame before test 1; and (b) photograph of damaged bracing after completion of test 3

Test no.	Calc. buckle disp.: mm	Damage observation	Peak test disp.: mm	Calc. yield disp.: mm	Meas. first yield: mm	First yield error: %
1	± 4.25	None	-3.94	± 7.07	—	—
2	± 4.24	Buckle (c. 11 s)	-10.01	± 7.05	10 (14 s)	3.4
3	± 4.44	Buckle (c. 6 s)	-19.69	± 7.39	9.1 (12 s)	8.1
4	± 5.82	None	4.53	± 8.89	—	—
5	± 5.96	Buckle (c. 15 s)	-10.28	± 9.09	-10.3 (15 s)	0.0
6	± 6.19	Buckle (c. 6 s)	-19.49	± 9.45	11.9 (14 s)	0.0
					Mean	2.9
					COV	11.0

Table 5. Qualitative and quantitative summary of test results

CBF structure. A constant scaling gain can also be applied to the predicted displacement to improve the accuracy of the prediction compared to the measured displacement.

A novel damage detection methodology is presented that detects initiation of damage by calculating relative lateral in-plane displacement threshold limits of buckling and yielding displacement of the CBF. The initial stiffness of the frame divided by the predicted threshold frame lateral force is used to identify if buckling and/or yielding have occurred in the bracing. Observation of the non-linearity in the hysteresis plot is used to verify the successful predictions of buckling in the bracing members. Strain data from seismic tests are used to verify the successful prediction of the tension yielding in the bracing members. The strategy was shown to predict buckling successfully in every test and predicted yielding with an average error of 2.9%.

Importantly, the strategy presented here does not rely on detectable changes in response; rather it measures the level of interstorey drift to infer damage. The structural damage is not

assumed through removal of bracing members, rather actual seismic loading on the structure induces structural damage. The damage detection strategy could also be easily extended to perform online to locate damage globally in a SHM scenario.

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