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Safari Mugisho, M., Makarov, D. G., Rassokhina, Y. V., Krizhanovski, V. G., Grebennikov, A., & Thian, M. (2019). Generalized Class-E Power Amplifier with Shunt Capacitance and Shunt Filter. *IEEE Transactions on Microwave Theory and Techniques*, 67(8), 3464 - 3474. <https://doi.org/10.1109/TMTT.2019.2923514>

### **Published in:**

IEEE Transactions on Microwave Theory and Techniques

### **Document Version:**

Publisher's PDF, also known as Version of record

### **Queen's University Belfast - Research Portal:**

[Link to publication record in Queen's University Belfast Research Portal](#)

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# Generalized Class-E Power Amplifier With Shunt Capacitance and Shunt Filter

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**Abstract**—This paper presents a generalized analysis of the Class-E power amplifier (PA) with a shunt capacitance and a shunt filter, leading to a revelation of a unique design flexibility that can be exploited either to extend the maximum operating frequency of the PA or to allow the use of larger active devices with higher power handling capability. The proposed PA fulfills zero voltage switching (ZVS) and zero voltage derivative switching (ZVDS) conditions, resulting in a theoretical dc-to-RF efficiency of 100%. Explicit design equations for the load-network parameters are derived, and the analytical results are confirmed by harmonic-balance simulations. Two PA prototypes were constructed with one designed at low frequency and the other at high frequency. The first PA, which employs a MOSFET and a lumped-element load-network, delivered a peak drain efficiency (DE) of 93.3% and a peak output power of 37 dBm at 1 MHz. The second PA, which employs a GaN HEMT and a transmission-line (TL) load-network to provide the drain of the transistor with the required load impedances at the fundamental frequency as well as even and odd harmonic frequencies, delivered a peak DE of 90.2% and a peak output power of 39.8 dBm at 1.37 GHz.

**Index Terms**—Class E, GaN, harmonic suppression, harmonic tuning, high efficiency, lumped element, MOSFET, power amplifier (PA), series reactance, shunt capacitance, shunt filter, transmission line.

## I. INTRODUCTION

THE CLASS-E power amplifier (PA) with shunt capacitance and series filter, introduced by Ewing [1] and further analyzed by Sokal and Sokal [2] and Raab [3], has been widely used due to its simple topology and high-efficiency operation. The high efficiency is achieved by applying zero voltage switching (ZVS) and zero voltage derivative switching (ZVDS) conditions, producing a soft switching at the OFF-to-ON transition. One of the main drawbacks of this topology is that it employs an ideal RF choke (RFC), which in practice needs to be replaced by a large, hence lossy and bulky,

inductor. An improved variant of this PA topology with a finite dc-feed inductance instead of an RFC is reported in [4]–[8], also known as “Class E with parallel circuit.”

Subsequently, the Class-E PA with series inductance and shunt filter, with switch voltage and current waveforms being the duals to those in the Class-E PA with shunt capacitance and series filter, hence termed as “inverse Class E,” is introduced in [9] and [10]. In contrast to its predecessor, it adopts zero current switching (ZCS) and zero current derivative switching (ZCDS) conditions, producing a soft switching at the ON-to-OFF transition. Although it offers 20% lower peak switch voltage than that in [1]–[3] as well as has the ability to absorb device output inductance ( $L_{out}$ ), its implementation is limited to small-to-medium power levels as it does not inherently incorporate a shunt capacitance to absorb device output capacitance ( $C_{out}$ ). For simplicity, the “Class-E PA with shunt capacitance and series filter” and the “Class-E PA with series inductance and shunt filter” will be referred to as “Class E” and “inverse Class E,” respectively, hereinafter.

Another high-efficiency PA topology, i.e., the Class-E PA with shunt capacitance and shunt filter depicted in Fig. 1(a) is introduced in [11]. A similar variant shown in Fig. 1(b) disposing the need for the capacitance  $C_X$  placed in parallel with the shunt filter and load resistance is described in [12]. These two topologies adopt ZVS and ZVDS conditions, and importantly, incorporate both shunt capacitance  $C$  to absorb  $C_{out}$  as in the Class E and series inductance  $L$  to absorb  $L_{out}$  as in the inverse Class E, rendering it attractive for high-frequency implementations where device parasitics play a dominant role in deleteriously affecting the PA performance. Furthermore, in series-filter-based Class-E topologies such as [1]–[8], a large inductance value is required to implement the series filter, whereas in shunt-filter-based Class-E topologies such as [9]–[13], the value of the inductor that forms the shunt filter is considerably lower for the same loaded quality factor value. A large inductance is typically accompanied with a large parasitic equivalent series resistance (ESR) and a low self-resonant frequency (SRF), hence rendering the series-filter-based Class-E topologies unattractive.

In this paper, we present a generalized Class-E PA with shunt capacitance and shunt filter, which incorporates a series reactance  $X$  as illustrated in Fig. 1(c). The system of equations describing the behavior of this PA is derived and expressed in terms of parameter  $q$ , whose value can be chosen arbitrarily, leading to an infinite number of solutions for the load-network

Manuscript received March 13, 2019; revised May 9, 2019; accepted May 14, 2019. This work was supported by the U.K. Engineering and Physical Sciences Research Council (EPSRC) under Grant EP/P013031/1. (Corresponding author: Moïse Safari Mugisho.)

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Digital Object Identifier 10.1109/TMTT.2019.2923514



at  $n \times f_0$ . As a result, the PA load-network at  $f_0$  and  $n \times f_0$  reduces to that shown in Fig. 1(e) and (f), respectively.

To simplify the analysis of the generalized Class-E PA with shunt capacitance and shunt filter, we adopt the same assumptions used in [12].

The idealized optimum (nominal) Class-E switching conditions are given as follows:

$$v_{sw}(\omega t) \Big|_{\omega t=2\pi} = 0 \quad (1)$$

$$\frac{dv_{sw}(\omega t)}{d\omega t} \Big|_{\omega t=2\pi} = 0 \quad (2)$$

where  $v_{sw}(\omega t)$  is the voltage across the switch.

Let the sinusoidal fundamental-frequency voltage  $v_1(\omega t)$  across the shunt  $L_0C_0$  filter be expressed as follows:

$$v_1(\omega t) = V_1 \sin(\omega t + \varphi_1) \quad (3)$$

where  $V_1$  is the fundamental-frequency voltage amplitude and  $\varphi_1$  is the phase shift due to a complex load.

When the switch is turned ON for  $0 \leq \omega t \leq \pi$ , the voltage across the switch is

$$v_{sw}(\omega t) = V_{DD} - v_L(\omega t) - v_1(\omega t) = 0 \quad (4)$$

where  $v_L(\omega t)$  is the voltage across the series inductor. Using (7)–(13) from [12] and substituting  $V_1$ , i.e., the voltage across the series connection of the reactance  $X$  and load  $R$  (instead of the voltage  $V_R$  across the load  $R$  as in [12] where  $X = 0 \Omega$ ), a general nonhomogeneous second-order differential equation for the switch voltage  $v_{sw}(\omega t)$  is obtained

$$\omega^2 LC \frac{d^2 v_{sw}(\omega t)}{d(\omega t)^2} + v_{sw}(\omega t) - V_{DD} + V_1 \sin(\omega t + \varphi_1) = 0. \quad (5)$$

The normalized general solution of (5) is given as

$$\frac{v_{sw}(\omega t)}{V_{DD}} = C_1 \cos q\omega t + C_2 \sin q\omega t + 1 + \frac{q^2}{1 - q^2} \frac{V_1}{V_{DD}} \sin(\omega t + \varphi_1) \quad (6a)$$

where  $q$  is defined as

$$q = \frac{1}{\omega \sqrt{LC}} \quad (6b)$$

and coefficients  $C_1$  and  $C_2$  are obtained by substituting  $V_R$  in (17) and (18) of [12] with  $V_1$ . It is worth noting here that parameter  $q$  in (6b) has different physical meaning from  $q$  in [7], where  $L$  is connected in parallel with the transistor (instead of in series as in this paper).

For a prescribed supply voltage  $V_{DD}$ , (6a) contains three unknown parameters  $q$ ,  $V_1/V_{DD}$ , and  $\varphi_1$ . Parameter  $q$  is treated as a variable and the other two parameters  $V_1/V_{DD}$  and  $\varphi_1$  are determined from a system of two equations resulting from applying the two optimum conditions, i.e., ZVS and ZVDS, given in (1) and (2). Fig. 2 shows the dependency of parameters  $V_1/V_{DD}$  and  $\varphi_1$  on  $q$ , from which it can be seen that for  $q = 1.607$ ,  $\varphi_1 = -41.6^\circ$  and  $V_1/V_{DD} = 0.925$ , which agree with the results presented in (20)–(22) of [12].

The normalized switch voltage and current waveforms calculated for  $q = 1.3$  (as in [11]), 1.6 (as in [12]), 1.85 (as in the

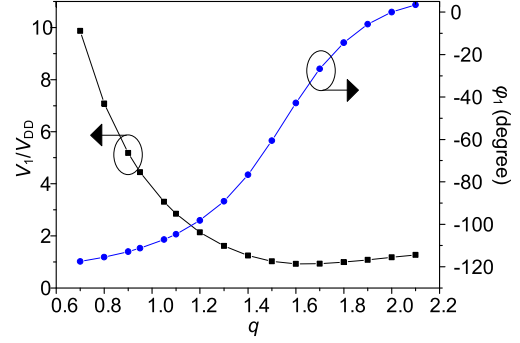


Fig. 2. Optimum Class-E parameters  $V_1/V_{DD}$  and  $\varphi_1$  versus  $q$ .

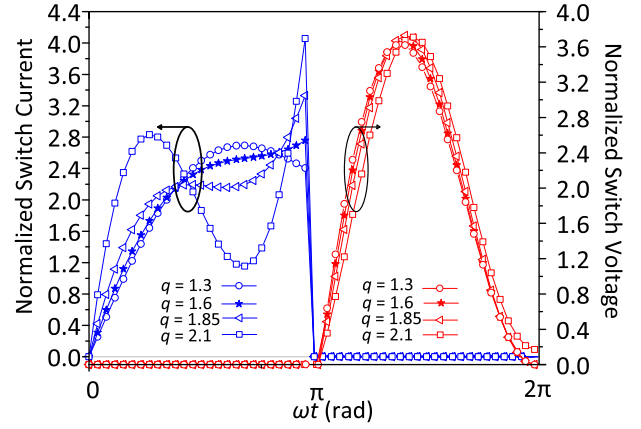


Fig. 3. Normalized switch voltage and current waveforms.

design example later treated in Section III), and 2.1 are shown in Fig. 3, where the switch voltage waveforms satisfy the optimum Class-E conditions for all  $q$  values. As  $q$  increases, the peak switch voltage does not vary as much as that in [7] while the current waveform changes its shape dramatically, creating a spike at the end of the turn-ON interval as in [7]. In ideal amplifier design, no power is being dissipated within the switch as nonzero voltage and current do not occur simultaneously (Fig. 3). However, in practice, this is something that design engineers must keep an eye on, especially when a slow switching device is used.

For an idealized amplifier, the dc power  $P_0 = I_0 V_{DD}$  is equal to the fundamental-frequency output power delivered to the load  $P_{out} = V_R^2/2R$ , resulting in unity drain efficiency ( $DE$ ). Hence, the optimum load resistance  $R$  can be calculated as

$$R = \frac{1}{2} \frac{V_R^2}{P_{out}} = \frac{1}{2} \left( \frac{V_R}{V_{DD}} \right)^2 \frac{V_{DD}^2}{P_{out}}. \quad (7)$$

The optimum load-network parameter  $\omega L$  is derived using [12, eqs. (23), (24)] with  $V_R$  in (24) replaced by  $V_1$ . Subsequently,  $\omega C$  can be derived from (6b)

$$\omega L = \frac{V_{DD}^2}{2\pi P_{out}} \left[ \frac{\pi^2}{2} - \frac{V_1}{V_{DD}} (2 \sin \varphi_1 + \pi \cos \varphi_1) \right] \quad (8)$$

$$\omega C = \frac{1}{q^2 \omega L}. \quad (9)$$

In the presence of a nonzero reactance  $X$  in series with load resistance  $R$ , as shown in Fig. 1(e), the real and imaginary

components of voltage amplitude  $V_1$  need to be defined. In this case, the sinusoidal voltage  $v_1(\omega t)$  in (3) can be expressed as

$$\begin{aligned} v_1(\omega t) &= v_R(\omega t) + v_X(\omega t) \\ &= V_R \sin(\omega t + \varphi) + V_X \cos(\omega t + \varphi) \end{aligned} \quad (10)$$

where  $\varphi$  is the initial phase.

The ratio of the imaginary and real components of  $V_1$ , i.e.,  $V_X$  and  $V_R$ , respectively, can be obtained as follows:

$$q_1 = \frac{V_X}{V_R} = \frac{X}{R} = \tan(\varphi_1 - \varphi) = \tan\psi \quad (11)$$

resulting in

$$V_1 = \sqrt{V_R^2 + V_X^2} = V_R \sqrt{1 + q_1^2} \quad (12)$$

where voltage amplitude  $V_R$  is defined in [12, eq. (12)].

As a result, the remaining unknown parameters  $q_1$ ,  $V_R/V_{DD}$ , and  $\varphi$  can be determined as a function of parameter  $q$  from a system of three equations of [12, eqs. (2), (3), (19)]. For a prescribed supply voltage  $V_{DD}$  and output power  $P_{out}$ , the load-network parameters  $\omega L$ ,  $X$ ,  $R$ , and  $\omega C$ , normalized to  $V_{DD}$  and  $P_{out}$ , can be expressed in terms of  $q$ .

The normalized optimum series inductance  $\omega L P_{out}/V_{DD}^2$ , series reactance  $X P_{out}/V_{DD}^2$ , shunt capacitance  $\omega C V_{DD}^2/P_{out}$ , and load resistance  $R P_{out}/V_{DD}^2$  are plotted versus parameter  $q$  in Fig. 4. From Fig. 4(a), it can be observed that a larger value of  $\omega L$  corresponds to a lower  $q$  value. To compensate for such an increased inductive value, the reactance  $X$  must, therefore, be decreased. The series reactance  $X$  changes from negative to positive values (or from capacitive to inductive) as  $q$  increases. Fig. 4(b) shows that as  $q$  increases, the value of  $\omega C$  increases, and consequently for a specific value of  $C$  representing the device output capacitance ( $C = C_{out}$ ),  $f_{max}$  increases with the increasing  $q$ . Thus,  $f_{max}$  of the generalized Class-E PA with shunt capacitance and shunt filter can be expressed as in the following equation:

$$f_{max} = k \frac{P_{out}}{V_{DD}^2 C_{out}}. \quad (13a)$$

The parameter  $k$  is plotted versus  $q$  in Fig. 4(b), from which it follows that  $q = 1.3$  results in  $k = 0.0728$  and  $q = 1.6$  results in  $k = 0.097$ , that are in line with [11, Table 3] and [12, eq. (32)], respectively, and are 1.44 and 1.91 times higher than that in [3], respectively. Furthermore,  $q = 2.1$  results in  $k = 0.227$  with the corresponding  $f_{max}$  being 4.5 and 2.7 times higher than that in [3] and [7], respectively. Equation (13a) can be rearranged to calculate the required shunt capacitance  $C$  in Fig. 1(d) for a prescribed supply voltage  $V_{DD}$ , output power  $P_{out}$ , and operating frequency  $f_0$ . Thus, the increase in  $k$  as  $q$  increases can also mean that a larger transistor with higher output capacitance can be used to implement the PA, thus enabling higher output power

$$C = k \frac{P_{out}}{V_{DD}^2 f_0}. \quad (13b)$$

The maximum operating frequency of the PA can also be defined in terms of the transistor output inductance, (13c), using (6b) and (13a). Since  $k$  increases with increasing  $q$ ,  $m$  will decrease with increasing  $q$ . As a result, for a given

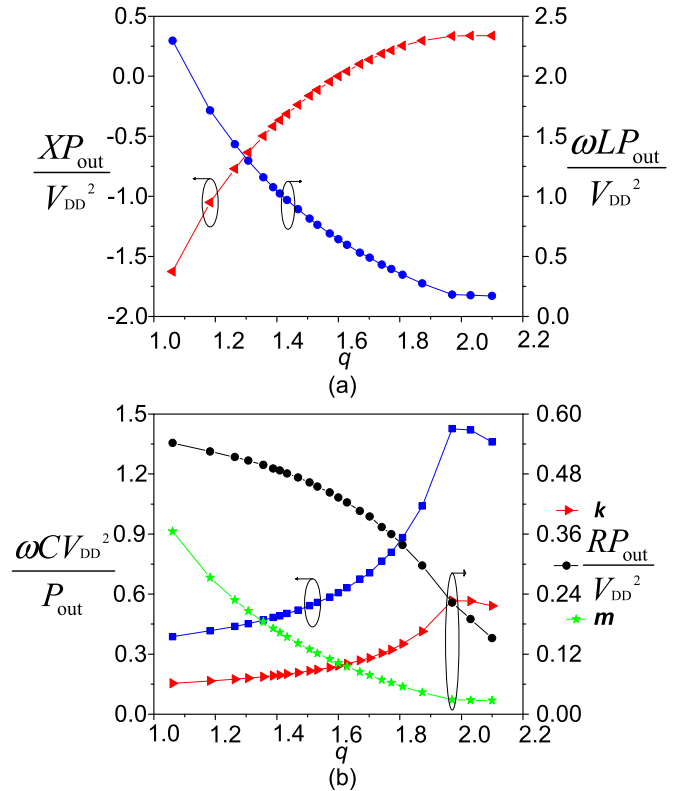


Fig. 4. Normalized optimum load-network parameters for the generalized Class-E with shunt capacitance and shunt filter. (a) Normalized series reactance and inductance. (b) Normalized shunt capacitance and load resistance.

TABLE I  
LOAD-NETWORK PARAMETERS OF [11] AND [12]  
COMPARED TO THIS PAPER

Parameter	Fig. 1(a)		Fig. 1(b)	
	[11]	This work	[12]	This work
$q$	1.3	1.3	1.6	1.6
$k$	0.0728	0.07194	0.097	0.097
$XP_{out}/V_{DD}^2$	-0.65	-0.634	0	0
$\omega L P_{out}/V_{DD}^2$	1.32	1.296	0.6351	0.6351
$\omega C V_{DD}^2/P_{out}$	0.455	0.452	0.6096	0.6096
$R P_{out}/V_{DD}^2$	0.494	0.507	0.4281	0.4281
Switch voltage peak factor	3.63	3.632	3.677	3.677

$V_{DD}$ ,  $P_{out}$ , and  $L_{out}$ ,  $f_{max}$  will also decrease with increasing  $q$ . Parameter  $m$  is plotted in Fig. 4(b)

$$f_{max} = \frac{1}{k(2\pi q)^2} \frac{V_{DD}^2}{P_{out} L_{out}} = m \frac{V_{DD}^2}{P_{out} L_{out}}. \quad (13c)$$

Table I shows that for  $q = 1.3$  and 1.6, the normalized load-network parameters and switch voltage peak factor derived in this paper are in line with the results obtained in [11] for  $q = 1.3$  and in [12] for  $q = 1.6$ ; thus, [11] and [12] are subsets of the work presented in this paper.

### III. EXPLORING THE NEW DESIGN SPACE

To accentuate the significance of the theoretical analysis and insights described in Section II, we designed and simulated three distinctive PAs: the Class E with series filter and ideal

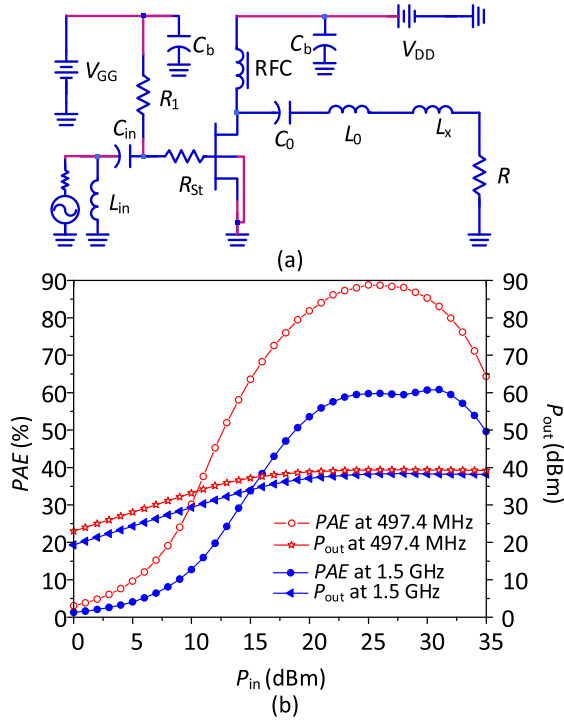


Fig. 5. Class-E PA with series filter and ideal RFC [1]–[3]. (a) Simulated circuit schematic. (b) Simulated PA performance versus  $P_{in}$  at 497.4 MHz and 1.5 GHz with  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

RFC [1]–[3], the Class E with series filter and finite RFC [7], and the proposed Class E with shunt filter and nonzero  $X$  in Fig. 1(c). For fair comparison, the three PAs employ the same transistor, i.e., Cree CGH40010F GaN HEMT with an output capacitance  $C_{out}$  of 1.3 pF and an output inductance  $L_{out}$  of 0.653 nH, and are biased with the same voltages, i.e.,  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V. The PAs were designed to deliver an output power of 10 W at a fixed operating frequency  $f_0 = 1.5$  GHz.

#### A. Class-E PA With Series Filter and Ideal RFC [1]–[3]

The design equations in [3] are used to determine the load-network parameters of the PA shown in Fig. 5(a). It follows that  $R = 45.2 \Omega$ ,  $L_X = 5.53$  nH,  $C = 0.43$  pF,  $L_0 = 48$  nH, and  $C_0 = 0.23$  pF for a loaded quality factor  $Q_L = 10$ . Notice that the required  $C$  is smaller than  $C_{out}$ . The total series inductance used in the simulation is  $L_X + L_0 - L_{out} = 52.9$  nH, i.e., to alleviate the detrimental effect of the parasitic inductance  $L_{out}$  on the PA performance. Fig. 5(b) shows that the PA delivers a peak power added efficiency (PAE) of 60.9% and a peak  $P_{out}$  of 38.4 dBm at 1.5 GHz. Substantially, higher peak PAE of 88.9% and peak  $P_{out}$  of 39.4 dBm are obtained if the PA is designed at its maximum operating frequency  $f_{max} = 497.4$  MHz, calculated using (13a) with  $k = 0.0507$  [3], with the circuit component values as follows:  $R = 45.2 \Omega$ ,  $L_X = 16.7$  nH,  $C = 1.3$  pF ( $= C_{out}$ ),  $L_0 = 145$  nH, and  $C_0 = 0.7$  pF for  $Q_L = 10$ . Thus, to fulfill the optimum Class-E conditions and, consequently, high-efficiency operation, the classical Class-E PA in [1]–[3]

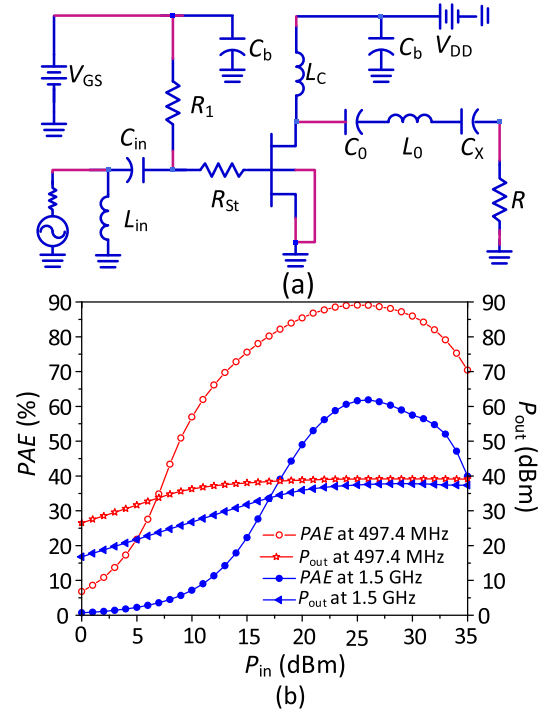


Fig. 6. Class-E PA with series filter and finite RFC [7]. (a) Simulated circuit schematic. (b) Simulated PA performance versus  $P_{in}$  at 497.4 MHz and 1.5 GHz with  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

should be operated at frequencies below or equal to  $f_{max}$  where the relationship  $C_{out} \leq C$  holds.

#### B. Class-E PA With Series Filter and Finite RFC [7].

The design set for maximum operating frequency ( $q = 1.468$ ) in [7, Table VI] is used to determine the load network parameters of the PA in Fig. 6(a). It follows that  $R = 104.4 \Omega$ ,  $L_C = 7.3$  nH,  $C = 0.71$  pF,  $C_X = 6.39$  pF,  $L_0 = 110.8$  nH, and  $C_0 = 0.1$  pF for  $Q_L = 10$ . Notice that the required  $C$  is greater than that of the design in Section III-A but smaller than  $C_{out}$ . Fig. 6(b) shows that the PA achieves a peak PAE of 61.9% and a peak  $P_{out}$  of 37.8 dBm at 1.5 GHz.

Substantially higher peak PAE of 89% and peak  $P_{out}$  of 39.15 dBm are obtained if the PA is designed at  $f_{max}$  of [1]–[3], i.e., 497.4 MHz, given that the same  $q$  value (i.e., 1.468) results in  $C = 2.15$  pF.

#### C. Proposed Class-E PA With Shunt Filter

Fig. 7(a) shows the simulated circuit schematic of the proposed topology in Fig. 1(c). The value of  $q = 1.85$  is selected to give  $C = 1.272$  pF  $\approx C_{out}$  at  $f = 1.5$  GHz, extracted from Fig. 4(b), which results in  $k = 0.1496$ , extending the  $f_{max}$  of the Class E with series filter [1]–[3] by a factor of 2.9. The value of  $L = 2.66$  nH is obtained from Fig. 4(a) for  $q = 1.85$  and  $f = 1.5$  GHz, resulting in an excess inductor  $L_e = L - L_{out} \approx 2$  nH. For the given  $V_{DD}$  and  $P_{out}$ ,  $X = 20.4 \Omega$  and  $R = 25.1 \Omega$  are determined from Fig. 4(a) and (b), respectively. Fig. 7(b) shows that the PA achieves a peak PAE of 84.3% and a peak  $P_{out}$  of 39 dBm at 1.5 GHz.

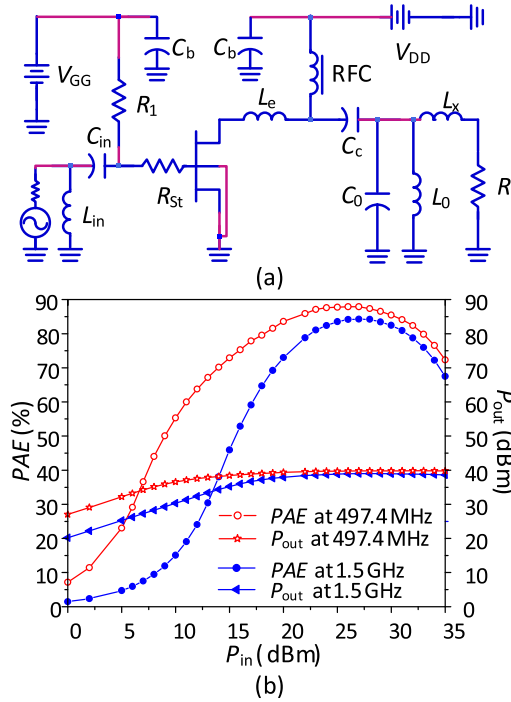


Fig. 7. Proposed Class-E PA with shunt filter. (a) Simulated circuit schematic. (b) Simulated PA performance versus  $P_{in}$  at 497.4 MHz and 1.5 GHz with  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

If designed at  $f_{max}$  of [1]–[3], i.e., 497.4 MHz, the same  $q$  value (i.e., 1.85) results in  $C = 3.84$  pF. Fig. 7(b) shows that the PA achieves a peak PAE of 87.9% and a peak  $P_{out}$  of 39.9 dBm. This result also shows that at a fixed frequency,  $f = 497.4$  MHz, a larger (hence, higher power capability) transistor with a  $C_{out} = 3.84$  pF can be used for this PA design.

The values of  $L_0$  and  $C_0$  in Fig. 7(a) are determined using (14b) and (14c) with the series connected  $L_x$  and  $R$  transformed to its equivalent parallel circuit  $L_P$  and  $R_P$ . For a given  $Q_L$ , the total inductance  $L_T$  that is formed by the parallel combination of  $L_0$  and  $L_P$  can be calculated using the following equation:

$$L_T = \frac{R_P}{\omega_0 Q_L} \quad (14a)$$

$$L_0 = \frac{L_P L_T}{L_P - L_T} \quad (14b)$$

$$C_0 = \frac{1}{\omega_0^2 L_0}. \quad (14c)$$

#### D. Discussion

The optimum circuit component values and performances of the PAs in Section III-A–III-C are summarized and compared in Table II. It has been shown that unlike the classical Class-E PAs in [1]–[3], and [7], the proposed PA can be operated at much higher frequencies while maintaining the high-efficiency characteristics. Critically, the classical PA requires much higher inductance value ( $L_0$ ) for the same loaded quality factor, rendering its implementation challenging as high inductance implies high ESR and low SRF, meaning that substantial power will be dissipated within the series filter.

TABLE II  
PA COMPARISONS

Design Frequency	Class E with Series Filter and Ideal RFC (IIIA)	Class E with Series Filter and Finite RFC (IIIB)	Class E with Shunt Filter (IIIC)
497.4 MHz	$C = 1.3$ pF $L_x = 16.7$ nH $R = 45.2$ $\Omega$ $L_0 = 145$ nH $C_0 = 0.7$ pF	$C = 2.15$ pF $L_c = 22.1$ nH $R = 104.4$ $\Omega$ $C_x = 19.27$ pF $L_0 = 334.1$ nH $C_0 = 0.306$ pF	$C = 3.84$ pF $L = 8$ nH $R = 25.1$ $\Omega$ $L_x = 6.52$ nH $L_c = 7.37$ nH $L_0 = 1.45$ nH $C_0 = 70.6$ pF
	$PAE = 88.9\%$ $P_{out} = 39.4$ dBm	$PAE = 89\%$ $P_{out} = 39.1$ dBm	$PAE = 87.9\%$ $P_{out} = 39.9$ dBm
1.5 GHz	$C = 0.43$ pF $L_x = 5.53$ nH $R = 45.2$ $\Omega$ $L_0 = 48$ nH $C_0 = 0.23$ pF	$C = 0.71$ pF $L_c = 7.3$ nH $R = 104.4$ $\Omega$ $C_x = 6.39$ pF $L_0 = 110.8$ nH $C_0 = 0.1$ pF	$C = 1.3$ pF $L = 2.66$ nH $R = 25.1$ $\Omega$ $L_x = 2.16$ nH $L_c = 2$ nH $L_0 = 0.48$ nH $C_0 = 23.4$ pF
	$PAE = 60.9\%$ $P_{out} = 38.4$ dBm	$PAE = 61.9\%$ $P_{out} = 37.8$ dBm	$PAE = 84.3\%$ $P_{out} = 39$ dBm

TABLE III  
LOAD-NETWORK PARAMETERS OF PA PROTOTYPE I

$q$	$XP_{out}/V_{DD}^2$	$\omega LP_{out}/V_{DD}^2$	$\omega CV_{DD}^2/P_{out}$	$RP_{out}/V_{DD}^2$
1.364	-0.4617	1.1139	0.4835	0.486
1.831	0.2448	0.3485	0.8559	0.34

The Class-E PA with series filter treated in Section III-A employs an ideal RFC that has infinite impedance at all frequencies, and consequently, the series inductors  $L_0 + L_x$  can be used to absorb the transistor output inductance  $L_{out}$ .

However, in practice, the RFC needs to be replaced with a finite dc-feed inductance, and consequently,  $L_{out}$  can no longer be absorbed by  $L_0 + L_x$ , as  $L_{out}$  is no longer in series with  $L_0 + L_x$ . Similarly, in the Class-E PA with series filter and finite RFC treated in Section III-B,  $L_{out}$  cannot be absorbed by  $L_0$ . On the contrary, the Class-E PA with shunt filter proposed in this paper has a mechanism in place to absorb  $L_{out}$ , i.e., through the series inductor  $L$  [Fig. 1(c)].

#### IV. IMPLEMENTATION AND MEASUREMENT

To validate the theory and simulation results described in Sections II and III-C, we built two PA prototypes: one implemented with an IRF630 MOSFET and lumped elements at 1 MHz while the other implemented with a Cree CGH40010F GaN HEMT and TLs at 1.5 GHz.

##### A. Low-Frequency Implementation With Lumped Elements

A power MOSFET IRF630 with an intrinsic output capacitance of 200 pF is used in this design. The PA was designed at 1 MHz based on the topology in Fig. 1(c). Table III presents the load-network parameters extracted from Fig. 4 for two

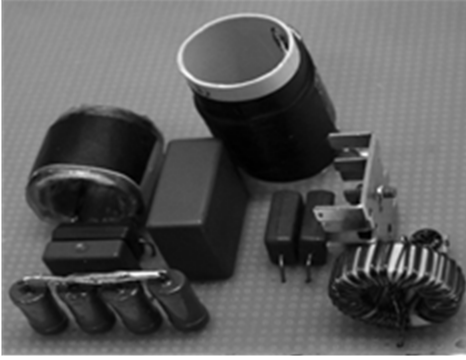
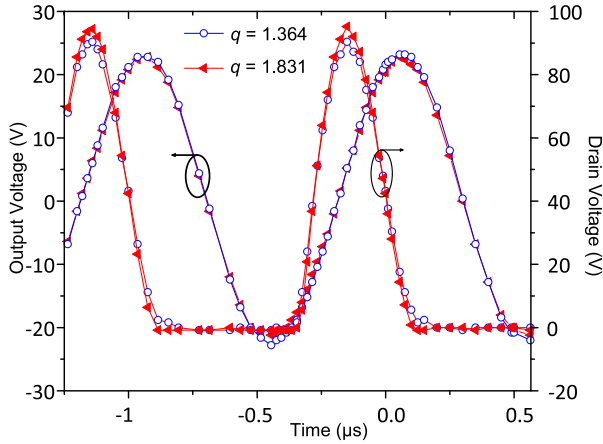


Fig. 8. Constructed PA prototype 1.

Fig. 9. Measured drain and output voltage waveforms of PA prototype 1.  $q = 1.364$ .  $q = 1.831$ .

arbitrary  $q$  values, i.e., 1.364 and 1.831 that results in a capacitive and inductive reactance  $X$ , respectively.

For a specified  $V_{DD} = 24$  V and  $P_{out} = 5$  W, the circuit component values were determined as:  $C_x = 2.99$  nF,  $L = 20.42$   $\mu$ H,  $C = 667.98$  pF, and  $R = 55.99$   $\Omega$  for  $q = 1.364$ , and  $L_x = 4.488$   $\mu$ H,  $L = 6.39$   $\mu$ H,  $C = 1.182$  nF, and  $R = 39.168$   $\Omega$  for  $q = 1.831$ . The shunt filter was implemented for  $Q_L = 5$ , resulting in  $L_0 = 1.57$   $\mu$ H and  $C_0 = 16.14$  nF.

The component values were slightly tuned to take into account the nonlinearity effect of the transistor output capacitance and parasitic ESR of the reactive components while preserving the nominal Class-E conditions.

Fig. 8 shows the photograph of the PA prototype 1, where the load is realized using four parallel connected 2-W resistors. Fig. 9 shows the measured drain and output voltage waveforms, with the former satisfying the ZVS and ZVDS conditions required for soft-switching and high-efficiency operation.

The measured PA performance in Fig. 10 shows that at 1 MHz, the PA delivered a  $DE$  of 93.3%, an output power ( $P_{out}$ ) of 5 W for  $q = 1.364$  and a  $DE$  of 88.6%, a  $P_{out}$  of 4.3 W for  $q = 1.831$ . The lower than-specified output power for  $q = 1.831$  is mainly due to the parasitic ESR of the shunt  $L_0C_0$  resonator [14].

### B. High-Frequency Implementation With Transmission Lines

The second PA prototype was designed at 1.5 GHz as in Section III-C. The basic circuit schematic of the PA prototype

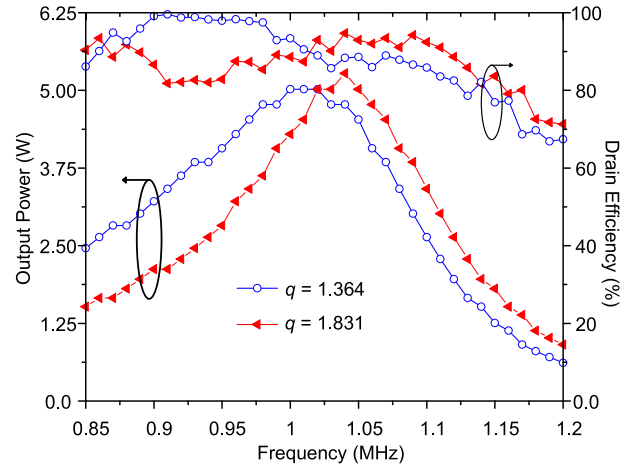
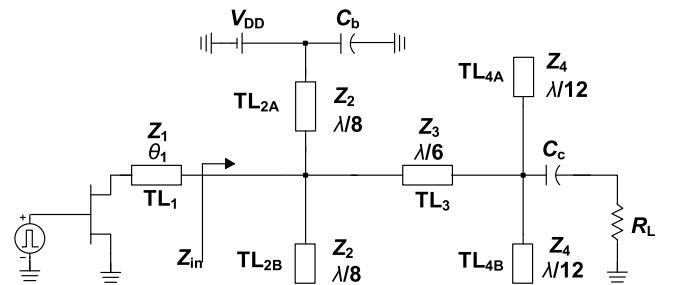
Fig. 10. Measured  $DE$  and output power of PA prototype 1.  $q = 1.364$ .  $q = 1.831$ .

Fig. 11. Basic circuit schematic of PA prototype 2 using TMs.

2 with a TL load-network is shown in Fig. 11, where  $C_c$  is a dc blocking capacitor and  $C_b$  is a bypass capacitor. The excess inductor  $L_e$  is realized using a series  $TL_1$  with a characteristic impedance of  $Z_1$  and electrical length of  $\theta_1$ , whose value is determined using the following equation:

$$\theta_1 = \tan^{-1} \left( \frac{\omega_0 L_e}{Z_1} \right). \quad (15)$$

For  $\theta_1$  in (15) to be considered sufficiently short at  $f_0$ , the value of  $Z_1$  should be selected to satisfy the relationship in the following equation:

$$Z_1 > \frac{4\omega_0 L_e}{\pi}. \quad (16)$$

A shorted  $\lambda/8$  stub ( $TL_{2A}$ ) together with an open-circuited  $\lambda/8$  stub ( $TL_{2B}$ ) with  $Z_2$  set to a high value enforce a short-circuit termination at even harmonic frequencies and an open-circuit termination at fundamental and odd harmonic frequencies [15]. A series  $\lambda/6$   $TL_3$  in conjunction with two open-circuited  $\lambda/12$  stubs ( $TL_{4A}$  and  $TL_{4B}$ ) enforce a short-circuit termination at  $3f_0$ . Hence,  $Z_{in} = 0$   $\Omega$  at  $2nf_0$  and  $3f_0$ , satisfying the load impedance requirement in Fig. 1(f). The characteristic impedances of  $TL_3$  and  $TL_{4A}/TL_{4B}$ , i.e.,  $Z_3$  and  $Z_4$ , respectively, are calculated to match  $Z_{opt} = (R + jX)$   $\Omega = (25.1 + j20.4)$   $\Omega$  to the standard 50  $\Omega$  load resistance ( $R_L$ ), thus satisfying the load impedance requirement in Fig. 1(e). At



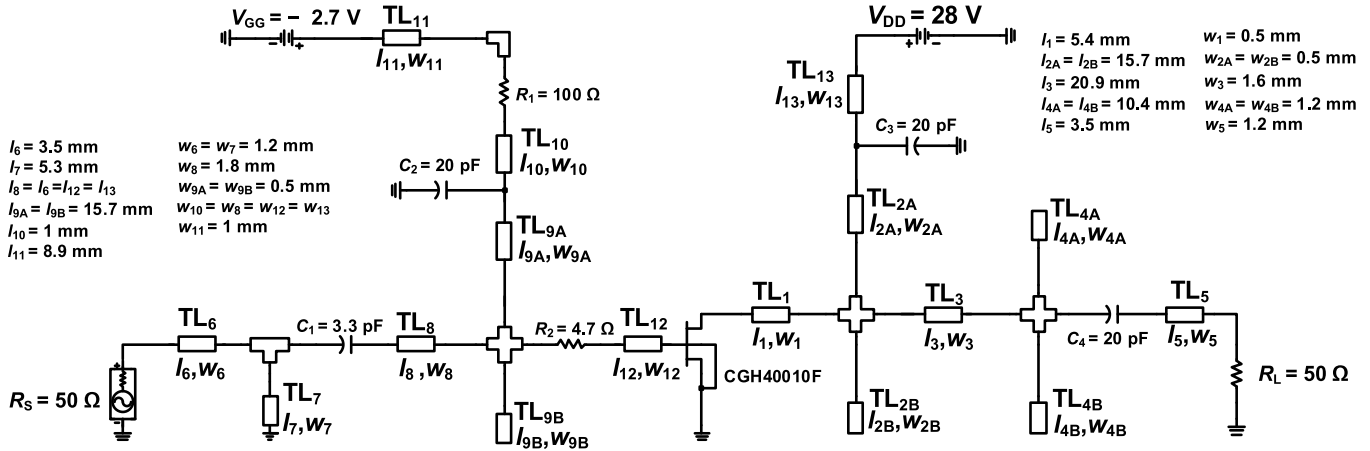


Fig. 12. Simulated circuit schematic of PA prototype 2.

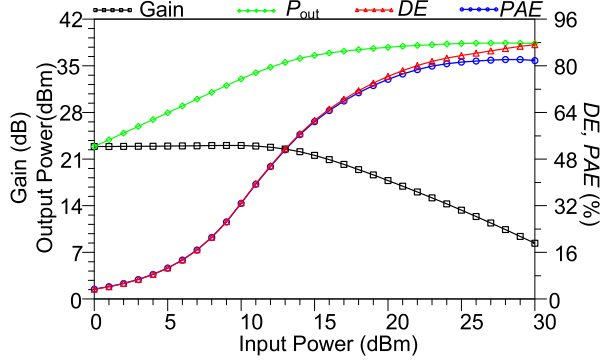
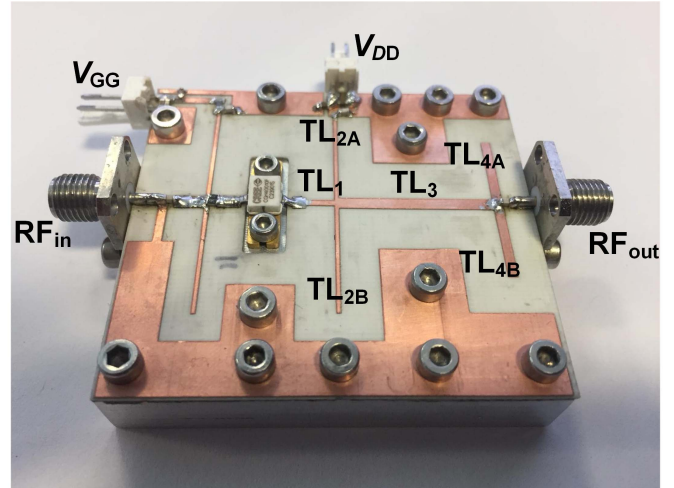
Fig. 13. Simulated PA performance versus input power at 1.5 GHz with  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

Fig. 14. Constructed PA prototype 2.

$f_0$ , the input impedance  $Z_{in}$  is given by the following equation:

$$Z_{in} = Z_3 \left[ \frac{3Z_3Z_4 + j\sqrt{3}(2Z_3 - Z_4)R_L}{(2Z_3 + 3Z_4)R_L - j\sqrt{3}Z_3Z_4} \right] \quad (17)$$

For  $R_L$  to be matched to  $Z_{opt}$  at  $f_0$ ,  $\text{Re}\{Z_{in}\} = R$  and  $\text{Im}\{Z_{in}\} = X$ , resulting in a system of two equations with two unknowns parameters described in (18) and (19), from which  $Z_3$  and  $Z_4$  are obtained as 50 and 63.5  $\Omega$ , respectively

$$3Z_3^2Z_4^2(4R_L - R) - R_L^2R(2Z_3 + 3Z_4)^2 = 0 \quad (18)$$

$$3Z_3^2Z_4^2(\sqrt{3}Z_3 - X) + R_L^2(2Z_3 + 3Z_4) \times [\sqrt{3}Z_3(2Z_3 - Z_4) - X(2Z_3 + 3Z_4)] = 0 \quad (19)$$

Harmonic-balance simulations were performed on the PA circuit depicted in Fig. 12 within the Keysight's Advanced Design System (ADS) environment. The simulation results in Fig. 13 show that the PA delivers a peak  $DE$  of 89.2%, a peak  $PAE$  of 83.7%, a peak  $P_{out}$  of 38.6 dBm, and a small-signal gain of 22.9 dB at 1.5 GHz.

The PA prototype 2 was constructed on a 0.51-mm-thick Rogers RO4003C substrate with a dielectric constant of 3.55 and a loss tangent of 0.0027, as shown in Fig. 14. A continuous-wave signal was applied to the PA using a Rohde & Schwarz SMR20 signal generator while the output power

was measured by a Keysight's N9320A spectrum analyzer. A 40-dB attenuator was connected between the PA and the spectrum analyzer. The gate and drain biasing voltages were provided by a Thurlby 32-V dc power supply.

The measured PA performance in Fig. 15 shows that when biased with  $V_{GG} = -2.7$  V and  $V_{DD} = 28$  V, the PA delivers a peak  $DE$  of 90.2%, a peak  $PAE$  of 82.6%, a peak  $P_{out}$  of 39.8 dBm, and a linear gain of 14 dB at an operating frequency of 1.37 GHz. The values of  $P_{out}$  and power gain at the peak  $PAE$  are 39.6 dBm and 11.5 dB, respectively. The deviation between results in Figs. 13 and 15 is likely due to the fabrication tolerance and the inaccuracy of the transistor's large-signal model, for instance, in capturing the effect of the package parasitics.

Fig. 16 shows the measured output power, gain,  $DE$ , and  $PAE$  with the frequency swept from 1.32 to 1.5 GHz at an input power level of 28.3 dBm.

The PA delivers  $DE$  and  $PAE > 60\%$ ,  $P_{out} = 38.6 \pm 1$  dBm, and power gain  $> 9.9$  dB over the 180-MHz frequency range.

Fig. 17 shows the measured output power, gain,  $DE$ , and  $PAE$  with the drain supply voltage swept from 14 to 32 V at

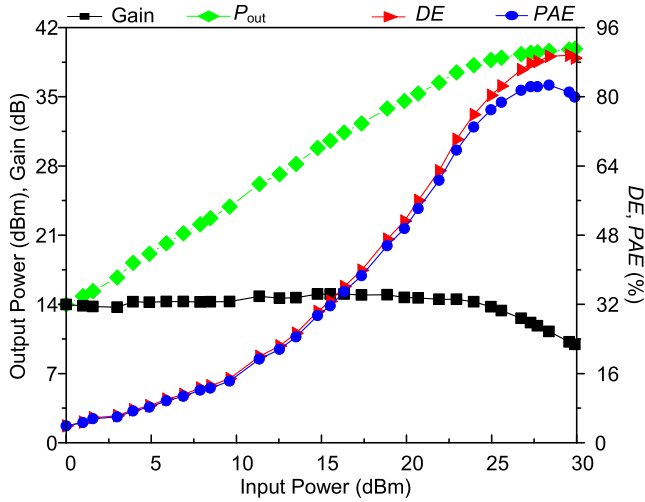


Fig. 15. Measured PA performance versus input power at 1.37 GHz with  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

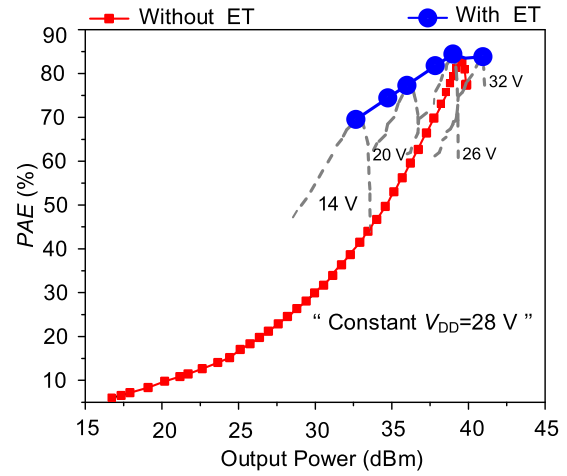


Fig. 18. Measured instantaneous  $PAE$  versus output power with quasi-static ET.

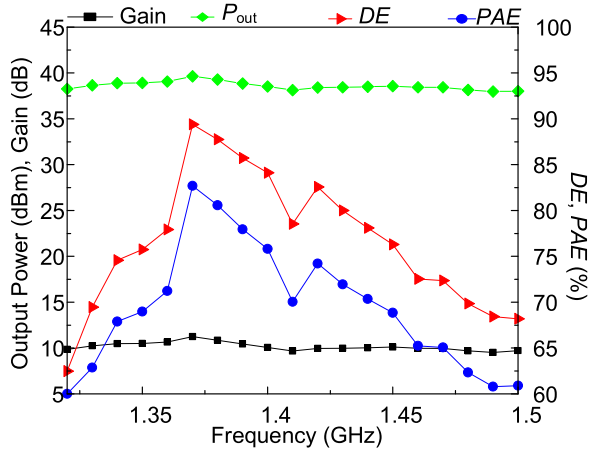


Fig. 16. Measured PA performance versus frequency at  $P_{in} = 28.3$  dBm with  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

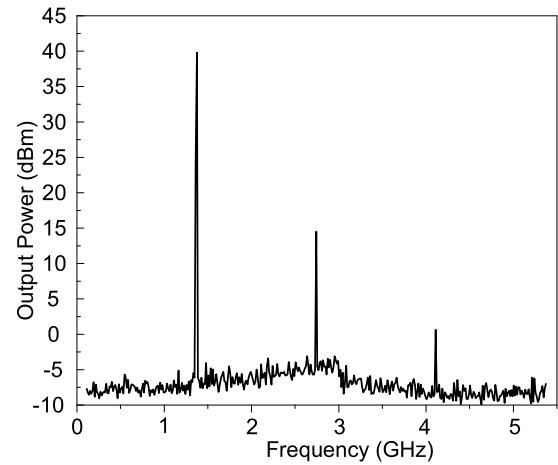


Fig. 19. Measured output power spectrum at  $V_{DD} = 28$  V and  $V_{GG} = -2.7$  V.

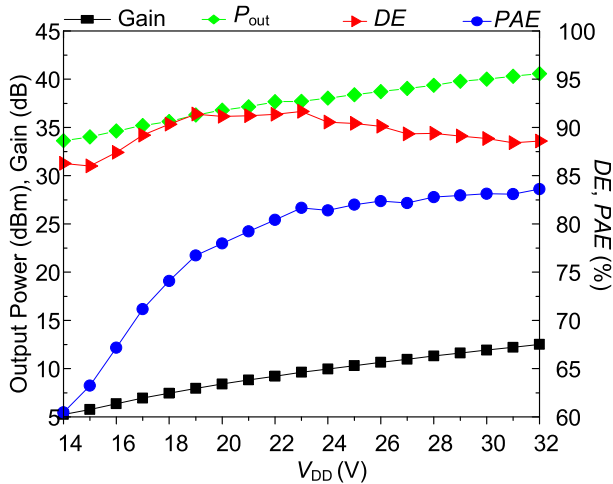


Fig. 17. Measured PA performance versus drain supply voltage at 1.37 GHz with  $P_{in} = 28.3$  dBm and  $V_{GG} = -2.7$  V.

an operating frequency of 1.37 GHz and an input power level of 28.3 dBm. The PA delivers a  $DE > 85\%$  and a  $PAE > 60\%$  over the specified range of  $V_{DD}$ , showing the potential

of operating the PA efficiently at lower drain supply voltages for deployment in polar transmitters or envelope elimination and restoration (EER) systems.

Fig. 18 shows the plot of the instantaneous  $PAE$  of the PA against output power for a constant  $V_{DD} = 28$  V, from which it can be seen that the  $PAE$  degrades substantially as  $P_{out}$  decreases. It can also be seen that by operating the PA with reduced  $V_{DD}$  values at low  $P_{out}$ , the  $PAE$  can be greatly improved. Each dashed line in Fig. 18 is obtained by biasing the PA with a particular  $V_{DD}$  value while sweeping the input power.

The peaks of these lines are then joined and interpolated to establish a quasi-static envelope tracking (ET) curve. For example, the ET curve gives a  $PAE$  of 77.7% at  $P_{out}$  of 36.3 dBm. This is achieved by setting the  $V_{DD}$  and the input power to 20 V and 26.2 dBm. In contrast, to obtain the same level of output power, the constant " $V_{DD} = 28$  V" curve gives a much lower  $PAE$  of 59.5% at an input power of 22.48 dBm.

Fig. 19 shows the measured output power spectrum with the second and third harmonic suppression levels of 25 and 39.7 dBc, respectively, showing the effectiveness of the

TABLE IV  
PERFORMANCE SUMMARY AND COMPARISON WITH OTHER GAN PAs

Ref	Freq (GHz)	$V_{DD}$ (V)	$P_{out}$ (dBm)	$DE$ (%)	$PAE$ (%)	Gain (dB)
[15]	2.22	28	39.5	91	80	9.2
[16]	2.8	28	40.1	77.5	70.8	10.7
[17]	1.5	28	42	85	81	13.1
[18]	2.14	30	40	76	73.1	14
[19]	3.5	26	40.2	75.8	70	12
This work	1.37	28	39.8	90.2	82.7	11.5

proposed TL load network. The PA performance is summarized in Table IV and compared with other pertinent work.

## V. CONCLUSION

The theoretical analysis of a generalized Class-E PA with shunt capacitance and shunt filter with 50% duty ratio, including the explicit derivation of the idealized optimum voltage and current waveforms and load-network parameters has been presented and verified through frequency-domain simulations and experiments. The calculated and simulated switch voltage and current waveforms show good agreement between them while fulfilling the ZVS and ZVDS conditions of the Class-E operation. Two PA prototypes, i.e., one designed with lumped elements at low frequency and the other designed with TLs at high frequency, have been built and measured, with both PAs achieving a peak  $DE$  of around 90% and excellent second and third harmonic suppression levels.

## ACKNOWLEDGMENT

The authors would like to thank Wolfspeed for providing the GaN power device.

## REFERENCES

- [1] G. D. Ewing, "High-efficiency radio-frequency power amplifiers," Ph.D. dissertation, Dept. Elect. Eng., Oregon State Univ., Corvallis, OR, USA, 1964.
- [2] N. O. Sokal and A. D. Sokal, "Class E—A new class of high-efficiency tuned single-ended switching power amplifiers," *IEEE J. Solid-State Circuits*, vol. SSC-10, no. 3, pp. 168–176, Jun. 1975.
- [3] F. Raab, "Idealized operation of the class E tuned power amplifier," *IEEE Trans. Circuits Syst.*, vol. CAS-24, no. 12, pp. 725–735, Dec. 1977.
- [4] V. B. Kozylev, "Single-ended switching-mode generator with filtering contour," (in Russian), *Poluprovodnikovye Pribory Tekhnike Elektrosvyazi*, vol. 8, pp. 152–166, 1971.
- [5] R. Zulinski and J. Steadman, "Class E power amplifiers and frequency multipliers with finite DC-feed inductance," *IEEE Trans. Circuits Syst.*, vol. CAS-34, no. 9, pp. 1074–1087, Sep. 1987.
- [6] A. V. Grebennikov and H. Jaeger, "Class E with parallel circuit—A new challenge for high-efficiency RF and microwave power amplifiers," in *IEEE MTT-S Int. Microw. Symp. Dig.*, Jun. 2002, pp. 1627–1630.
- [7] M. Acar, A. J. Annema, and B. Nauta, "Analytical design equations for class-E power amplifiers," *IEEE Trans. Circuits Syst. I, Reg. Papers*, vol. 54, no. 12, pp. 2706–2717, Dec. 2007.
- [8] J. Cumana, A. Grebennikov, G. Sun, N. Kumar, and R. H. Jansen, "An extended topology of parallel-circuit class-E power amplifier to account for larger output capacitances," *IEEE Trans. Microw. Theory Techn.*, vol. 59, no. 12, pp. 3174–3183, Dec. 2011.
- [9] T. Mury and V. F. Fusco, "Series-L/parallel-tuned comparison with shunt-C/series-tuned class-E power amplifier," *IEE Proc. Circuits, Devices Syst.*, vol. 152, no. 6, pp. 709–717, Dec. 2005.

- [10] T. Mury and V. F. Fusco, "Inverse class-E amplifier with transmission-line harmonic suppression," *IEEE Trans. Circuits Syst. I, Reg. Papers*, vol. 54, no. 7, pp. 1555–1561, Jul. 2007.
- [11] M. Thian and V. Fusco, "Idealised operation of zero-voltage-switching series-L/parallel-tuned class-E power amplifier," *IET Circuits, Devices Syst.*, vol. 2, no. 3, pp. 337–346, Jun. 2008.
- [12] A. Grebennikov, "High-efficiency class-E power amplifier with shunt capacitance and shunt filter," *IEEE Trans. Circuits Syst. I, Reg. Papers*, vol. 63, no. 1, pp. 12–22, Sep. 2016.
- [13] P. Chen, K. Yang, and T. Zhang, "Analysis of a class-E power amplifier with shunt filter for any duty ratio," *IEEE Trans. Circuits Syst., II, Exp. Briefs*, vol. 64, no. 8, pp. 857–861, Aug. 2017.
- [14] D. G. Makarov, J. V. Rassokhina, V. G. Krizhanovski, and G. Andrei, "High-frequency class-E power amplifier with shunt filter," in *Proc. Int. Conf. Radio Electron. Info Commun.*, Sep. 2016, pp. 1–4.
- [15] M. Thian, A. Barakat, and V. Fusco, "High-efficiency harmonic-peaking class-EF power amplifiers with enhanced maximum operating frequency," *IEEE Trans. Microw. Theory Techn.*, vol. 63, no. 2, pp. 659–671, Feb. 2015.
- [16] Y. Leng *et al.*, "An extended topology of parallel-circuit class-E power amplifier using transmission-line compensation," *IEEE Trans. Microw. Theory Techn.*, vol. 61, no. 4, pp. 1628–1638, Apr. 2013.
- [17] M. Thian, A. Barakat, and V. Fusco, "A 1.5 GHz GaN HEMT fifth-harmonic-peaking class-EF power amplifier with 85% drain efficiency and 42 dBm output power," in *Proc. IEEE APMC*, Sendai, Japan, Nov. 2014, pp. 1001–1003.
- [18] A. Grebennikov, "High-efficiency class E/F lumped and transmission-line power amplifiers," *IEEE Trans. Microw. Theory Techn.*, vol. 59, no. 6, pp. 1579–1588, Jun. 2011.
- [19] S. Jee, J. Moon, J. Kim, J. Son, and B. Kim, "Switching behavior of class-E power amplifier and its operation above maximum frequency," *IEEE Trans. Microw. Theory Techn.*, vol. 60, no. 1, pp. 89–98, Jan. 2012.



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