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On the importance of nesting considerations for accurate computational damage modelling in 2D woven composite materials

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Abstract

The mechanical behaviour and progressive damage of two-dimensional plain woven carbon-epoxy fabrics is modelled at different length scales, taking into account the geometric and material variability of the weave, by subjecting the dry preforms to compaction simulations. Micromechanical analyses are performed using a fibre distribution algorithm, in order to obtain the mechanical properties of the tows for any given fibre volume fraction. Different Representative Unit Cells are generated, compacted, and subjected to Periodic Boundary Conditions in order to compare their mechanical performance, under different loading scenarios. Additional analyses are undertaken to evaluate the effect of nesting under different stress states. Through computational homogenisation, it is possible to study damage evolution and corresponding stiffness degradation of the material. The numerical predictions are compared with experimental observations, and show that, to model damage: i) a single ply with three-dimensional Periodic Boundary Conditions or four plies with two-dimensional Periodic Boundary Conditions may not be the most accurate approach to model damage; ii) it is important to consider the effect of nesting in such computational models, since they play a key role in the mechanical response of the material.

Keywords: Textile composites, Fibre volume fraction variability, Computational mechanics, Multiscale analysis, Damage modelling

Nomenclature

2D, 3D	Two- and three-dimensional
BK	Benzeggagh-Kenane
BC	Boundary Condition
CT	Computed Tomography
FE	Finite Element

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	MESI	Measurement Enhanced Shape Identification
	PBC	Periodic Boundary Condition
	RUC	Representative Unit Cell
10	RVE	Representative Volume Element
	UD	Unidirectional
	a, b	Major and minor ellipse axis
	d_m	Matrix damage variable
	d_f	Fibres damage variable
15	d_{11}^t, d_{11}^c	Longitudinal tensile and compressive damage variable of the tows
	d_{11}	Combined longitudinal damage variable of the tows
	d_{mat}	Damage variable of the matrix inside the tows
	d_i	Damage variable of the cohesive interfaces
	g_0	Quadratic interpolation of the matrix-dominated volumetric strain energies
20	h_i, h_{med}	Local and average height of a tow
	k	Integration point
	l_{mat}, l_{fib}	Characteristic element length in the matrix and fibre direction
	n	Exponent of the power ellipse equation
	n_f	Number of fibres inside each tow
25	r_m, r_f	Internal variable related to the matrix and fibres damage model
	$\mathbf{s}$	Deviatoric stress tensor
	t	Total time of the compaction simulation
	t_i	Frame of the compaction simulation
	A_i	Local cross-sectional area of a tow
30	A_{med}	Average cross-sectional area of a tow
	A_m, A_f	Internal parameter related to the elements of the matrix and fibres
	A^e	Fracture surface area of the element
	E_{11}^{DT}, E_{22}^{DT}	Longitudinal and transverse Young's modulus of the dry tows
	E_m	Young's modulus of the matrix
35	E_{11}^f, E_{22}^f	Longitudinal and transverse Young's modulus of the fibres
	E_{11}, E_{22}	Longitudinal and transverse Young's modulus of the tows
	E_{11}^0, E_{11}^T	Laminate level undamaged and tangent longitudinal Young's modulus
	$\mathbf{F}$	Deformation gradient
	F_m^d	Damage activation function for the matrix
40	F_f^d	Damage activation function for the fibres
	F_{11}^t, F_{11}^c	Longitudinal failure index of the tows for tension and compression

	F_{mat}	Failure index of the matrix inside the tows
	G_1, G_2	Gap between parallel and overlapping tows
	G_{12}^{DT}	In-plane and out-of-plane shear modulus of the dry tows
45	G_{12}^f	In-plane and out-of-plane shear modulus of the fibres
	G_{12}, G_{23}	In-plane and out-of-plane shear modulus of the tows
	G_{12}^0, G_{12}^T	Laminate level undamaged and tangent in-plane shear modulus
	$\mathcal{G}_{Ic}^m, \mathcal{G}_{Ic}^f$	Mode I fracture toughness of the matrix and fibres
	$\mathcal{G}_{Ic}^{11}, \mathcal{G}_{Cc}^{11}$	Mode I and compressive longitudinal fracture toughness of the tows
50	$\mathcal{G}_{Ic}^{22}, \mathcal{G}_{Cc}^{22}$	Mode I and compressive transverse fracture toughness of the tows
	$\mathcal{G}_{IIc}^{12}, \mathcal{G}_{IIc}^{13}, \mathcal{G}_{IIc}^{23}$	In-plane and out-of-plane matrix shear dominated fracture toughness of the tows
	$\mathcal{G}_{rc}^{22}$	Quadratic interpolation of the matrix-dominated fracture toughnesses
	$\mathcal{G}_{Ic}^i, \mathcal{G}_{IIc}^i, \mathcal{G}_{IIIc}^i$	Interface fracture toughness
	$\mathcal{G}_c^i$	Mixed-mode interface fracture toughness evaluated with the BK law
55	H_i, H	Local and total length of a tow
	I_1	First stress invariant of the applied stress tensor
	$\tilde{I}_1$	First stress invariant of the effective stress tensor
	J_2	Second invariant of the deviatoric stress tensor
	$\tilde{J}_2$	Second invariant of the effective deviatoric stress tensor
60	K_i	Penalty/Interface stiffness
	L_0, L	Reference and gauge length
	N_p	Total number of integration points in the specific domain
	S_{12}, S_{12}^{is}	In-plane shear strength of the tows, and corresponding in-situ strength
	S_{23}, S_{23}^{is}	Out-of-plane shear strength of the tows, and corresponding in-situ strength
65	V_0^e, V^e	Undeformed and deformed volume of an element
	V^k	Associated volume of the integration point
	V^{mat}, V^{tows}	Total volume of the matrix and tows inside the RUC
	V^{RUC}	Total volume of the RUC
	W	Width of a tow
70	X^t, X^c	Longitudinal tensile and compressive strength of the tows
	X_m^t, X_m^c	Absolute value of the tensile and compressive strength of the matrix
	X_f^t	Tensile strength of an element of the FE mesh of the fibres
	$Y^t, Y^{t,is}$	Transverse strength of the tows and corresponding in-situ strength
	$Y^c, Y^{c,is}$	Compressive strength of the tows and corresponding in-situ strength
75	δ_m^0, δ_m^f	Displacement of the interface at damage initiation and failure
	δ_m^{max}	Maximum value of the effective displacement of the interface attained during the

loading history

ε Strain tensor

ε_e^p Equivalent plastic strain

80 $\varepsilon_{11}^{0t}, \varepsilon_{11}^{0c}$ Tensile and compressive fibre failure initiation strain in the tows

$\varepsilon_{11}^{ft}, \varepsilon_{11}^{fc}$ Tensile and compressive fibre failure strain in the tows

$\varepsilon_r, \varepsilon_{r,in}^0, \varepsilon_r^0, \varepsilon_r^f$ Norm of the total, inelastic, initiation and failure strains acting in the tows fracture plane

η_{BK} Mixed-mode interaction parameter

85 κ, λ Parameters for the matrix failure criteria of the tows

μ_τ Coefficient of friction between tows

μ_{NL}, μ_{NT} Transverse friction coefficients

ν_{12}^{DT} In-plane Poisson's coefficient of the dry tows

ν_{12} In-plane Poisson's ratio of the tows

90 ν_m Poisson's ratio of the matrix

ν_p Plastic Poisson's ratio of the matrix

ν_{12}^f In-plane Poisson's ratio of the fibres

ρ, ρ_m, ρ_f Density of the tows, matrix and fibres

σ Stress tensor

95 $\sigma_{Y_t}, \sigma_{Y_c}$ Absolute value of the tensile and compressive yield strength of the matrix

σ_0, m, l_0 Weibull parameters

$\sigma_{NN}, \sigma_{NL}, \sigma_{NT}$ Stresses on the fracture surface of the tows

σ_r Norm of the stresses in the fracture plane

$\sigma_{ij}^0, \sigma_{ij}^{0c}$ Homogenised far-field stress component and its critical value

100 σ_{ij}^k Stress component determined at the integration point, k

ϕ_m^d, ϕ_f^d Loading function of the matrix and fibres

τ_{eff}^0 Interfacial effective traction at damage initiation

τ_0, τ_1, τ_2 Interface strengths

ω_f^i Local intra-tow fibre volume fraction

105 ω_f^{towmed} Average fibre volume fraction of the tows

$\omega_f^{\text{RVE}}, \omega_f^{\text{RUC}}$ Fibre volume fraction of the RVE and RUC

1. Introduction

Textile composites are preferred over unidirectional (UD) laminated composites when higher production rates and drapability are significant design drivers [1]. They are attractive due to yarn interlacing, which improves structural stability and damage tolerance [2], and can accommodate a wide variety of textile architectures, encompassing braids, weaves, knitted, and nonwoven fabrics. Since two-dimensional (2D) plain weave fabrics are one of the most widely used textiles for structural components, the ability to evaluate and predict damage initiation and propagation in this type of material system is critical. Despite the numerous investigations conducted by several authors, it is still not completely clear how damage evolves in textile composites, since different internal geometries of the material [3] may lead to different stress concentration areas, crack propagation patterns and final failure scenarios.

The meso-discretisation of these materials is usually based on a Representative Unit Cell (RUC), which is composed of homogenised fibre bundles (or tows), in resin. The ability to predict the mechanical behaviour of the material is dependent on the ability of the RUC, to capture: i) the complex and non-uniform distribution of the cross-sectional area of the tows [3, 4, 5] and, consequently, the variability of the fibre volume fraction along their length [4, 6, 7]; ii) the crimp angles of the tows [8]; iii) the overall fibre volume fraction of the material (which is still nowadays a challenge to model a RUC with an empiric overall fibre volume fraction of the composite without virtually increasing the fibre volume fraction of the tows [9]); iv) the number of plies in the RUC, and v) the nesting between plies [10, 11, 12, 13, 14].

Modelling-wise, the aforementioned features are not easy to obtain. Therefore, simplistic RUCs (generated using the Finite Element Method (FEM) or shape functions, which use a constant cross-sectional area along their length, and an idealised sinusoidal path) have been used to predict homogenised stiffness [5, 9, 15, 16, 17] and assess damage initiation and/or propagation of damage [11, 18, 19, 20, 21, 22]. These models are often generated with open source software packages such as *TexGen* [23] and *WiseTex* [24]. However, since the aforementioned models are not able to replicate the fibre volume fraction of the composite, i.e. their exact inner structure, a higher artificial fibre volume fraction needs to be assigned to each tow, impeding accurate and realistic localised stress-strain predictions. Voxel FE models [25, 26, 27] are easy to deal with. However, due to the staircase-like shape of the voxels, artificial contact between yarns may occur, and the local stress states fluctuate with mesh refinement rather than reaching a converged value [28].

Several contributions have been made towards developing a more realistic geometry of textile woven composite materials in a computational environment [7, 29, 30, 31]. Namely, Doitrand et al. [29, 30] made use of compaction simulations to generate fabrics with non-idealised cross-sectional areas and

sweep paths of the tows, preserving the overall fibre volume fraction of the composite. Sevenois et al. [7] proposed the Measurement Enhanced Shape Identification (MESI) method, which generates the RUC geometry by using more complex shape functions together with observations conducted using micro-Computed Tomographic (μ -CT) scans of the material.

In this work, the progressive damage of a 2D plain weave carbon-epoxy fabric is analysed, through the development of an one-way multiscale approach, by generating statistical Representative Volume Elements (RVEs) at the microscale, and RUCs at the mesoscale, which take into account the aforementioned features. Multiscale strategies, which involve homogenisation techniques from the microscale, may induce errors due to several factors, e.g. different mechanical properties of the neat resin coupons compared to the in-situ resin [32], uncertainty in the behaviour of the fibre-matrix interfacial regions, and, after damage localisation, the homogenisation procedure may become ill-posed due to the application of Periodic Boundary Conditions (PBCs) [33]. Therefore, by normalising the numerical and experimental results, proper quantitative and qualitative comparisons can thus be made.

The main aims of this paper are to: i) analyse the importance of considering a compaction step for the generation of a mesoscale framework; ii) evaluate the material variability that arises due to the compaction step, which material properties were previously calibrated at the microscale; iii) analyse the influence of the number of plies within an RUC in predicting the mechanical performance under different loading scenarios, and iv) explore the importance of nesting in mesomechanical simulations.

The structure of the paper is organised as follows. The compaction simulations are described in Section 2, the constitutive models for each part of the computational framework are described in Section 3, followed by the micromechanical FE modelling strategy in Section 4. The numerical results are presented in Section 5 and, finally, the conclusions are drawn in Section 6.

2. Dry fabric compaction simulations

A similar methodology previously used by Doitrand et al. [29, 30] is used in order to obtain an accurate representation of the plain weave RUCs with the desired features. Initially, the geometry of the tows has a sinusoidal sweep path and a cross-sectional shape of a special form of the super-ellipse, the power ellipse [34], which is defined as:

$$\left| \frac{x}{a} \right| + \left| \frac{y}{b} \right|^{2/n} = 1, \quad (1)$$

with the major and minor ellipse axis given by a and b , respectively. The exponent of the power ellipse was chosen to be $n = 1.4$, guaranteeing that there is no initial contact and/or overclosures between tows in the initial geometry of the weave. The geometric parameters of a tow are illustrated in Figure 1 and described in Table 1.

Figure 1: Initial geometry of the tows.

Dimensions	[mm]	Description
H	4.7	Tows' length
h_{med}	0.15	Tows' average height
W	2.2	Tows' width
G_1	0.15	Gap between parallel tows
G_2	0.04	Gap between overlapping tows

Table 1: Initial dimensions of the fabrics (see Figure 1).

Several RUCs are generated and compacted with: i) one ply; ii) four aligned stacked plies; iii) eight aligned stacked plies; iv) eight plies stacked with maximum offsets in both in-plane directions (x and y directions); and v) eight plies stacked randomly. The eight-ply RUC with randomised offsets is generated by placing each of its plies randomly, through the multiplication of the initial in-plane coordinates of each layer, by a uniformly distributed scalar on the open interval $[0, 1]$.

The preforming compaction step was simulated using Abaqus[®]/Explicit [35], with the aim of obtaining RUCs with an overall fibre volume fraction similar to a real composite, a qualitative reproduction of nesting between the layers, and more realistic cross-sectional shape and size of the yarns along their length. At this stage, the homogenised tows are assumed to have a transversely isotropic linear-elastic behaviour. The longitudinal elastic modulus, is assumed to be $E_{11}^{\text{DT}} = 135$ GPa, the transverse and shear moduli equal to $E_{22}^{\text{DT}} = G_{12}^{\text{DT}} = G_{23}^{\text{DT}} = 8 \times 10^{-2}$ GPa, and the Poisson's ratio in the longitudinal direction is assumed to be close to zero ($\nu_{12}^{\text{DT}} = 0.01$), leading to negligible contraction along the length of the yarns [29]. The models are subjected to 2D PBCs [19, 36, 37], in order to force periodicity on the outer shape of the RUCs. A general contact explicit formulation, using a penalty friction approach was used to avoid interpenetration between yarns during the step. Values for the coefficient of friction of the fibre-matrix interface and/or tow-on-tow contact have been reported to be in the range $0.25 \leq \mu_{\tau} \leq 0.6$ [32, 38, 39, 40]. Since the characterisation of this value has been reported to depend on the orientation of the tows and on the material system, a coefficient of friction

(a) Preform before compression step.

(b) Compacted preform.

Figure 2: Compaction step.

of $\mu_\tau = 0.5$ was used for the compaction simulations. Figure 2 shows the compaction procedure of the preforms.

By considering the same overall fibre volume fraction of the composite throughout the analyses ($\omega_f^{\text{RUC}} = 50\%$), different fibre volume fractions of the tows inside the RUC, ω_f^{towmed} , are derived. The fibre volume fraction of the tows for each RUC is reported in Table 2.

RUC	$V^{\text{tows}} [\text{mm}^3]$	$V^{\text{mat}} [\text{mm}^3]$	n_f	$\omega_f^{\text{towmed}} [\%]$
No offsets, one ply	3.19	1.32	3117	70.70
No offsets, four plies	13.70	4.08	3072	62.40
No offsets, eight plies	27.39	7.61	3023	63.89
Maximum offsets, eight plies	26.10	4.40	2634	58.42
Random offsets, eight plies (1)	25.24	5.17	2626	60.24
Random offsets, eight plies (2)	26.13	5.11	2698	59.78
Random offsets, eight plies (3)	25.85	5.07	2671	59.81

Table 2: Fibre volume fraction of the tows for each RUC.

It is known from experimental observations [3, 7] that this compaction step changes the cross-sectional area of the tows, and consequently the intra-tow fibre volume fraction, causing a change on the local material properties of the material. Sevenois et al. [7], through the use of a μ -CT scan, were able to identify the shape and path of the tows of a 2D plain woven carbon-epoxy fabric, and observed that the variation of the cross-sectional area was predominantly dependent on the change of the height

Figure 3: Variation of the height of the tows along their length for different steps of the compaction simulations.

of the tows. Figure 3 shows the normalised local height of the tows, h_i , with respect to their average height, h_{med} , along their length for different frames of the compaction simulation, where t_i and t are the incremental and total time of the simulation, respectively.

It can be seen that during the compaction simulation, the local height of the tows increases locally relative to their average height, h_{med} . Comparing the numerical results with the μ -CT measurements conducted by Sevenois et al. [7] (see Figure 4), it can be concluded that the compacted RUC shows a better representation of experimental observations than an idealised RUC, where the cross-sectional area is considered constant along the tows' length.

If the meso-level models of the RUCs are not generated through compaction simulations, the variation in cross-sectional area may be assumed as sinusoidal [7]. Figure 5 shows the variation in the height of the tows along their length, for different gaps between parallel tows, G_1 .

Increasing G_1 leads to an unrealistic distribution, where certain parts of the tows were not even compacted (flat parts in the plots). This implies that accurate measurements of the preform geometry need to be conducted, using, for example, μ -CT measurements, in order to accurately model the behaviour of such textile composites.

With what was previously described, the local intra-tow fibre volume fraction is affected, and consequently, the local mechanical properties of the tow itself, affecting the performance of the material. Figure 6 shows an example of the intra-tow fibre volume fraction variability along the length of the tows due to the change on the local cross-sectional area.

Figure 4: Comparison of the numerical predicted variation of the cross-sectional area of the tows along their length, with experimental observations conducted by Ref. [7].

Figure 5: Predicted variation of the height of the tows along their length, for different gaps between parallel tows, G_1 .

Figure 6: a) Quantitative and b) qualitative example of intra-yarn fibre volume fraction variability along the length of the tows.

3. Constitutive modelling

The multiscale approach used here represents a direct link between the micro and the mesoscale framework, and consists, at the microscale, of an RVE, composed of the fibres, matrix, and their interface, and at the mesoscale, by the epoxy matrix (same as the one used in the micromechanical framework) and homogenised tows (see Figure 7). The objective of the microscale model is to mechanically characterise the tows along their length. This information is used to build the mesoscale model, which is used to predict the homogenised mechanical performance at the laminate level (macroscale). For the sake of completeness, the highlights of the constitutive models for each of these materials are briefly described in the following sub-sections.

3.1. Epoxy matrix

The epoxy matrix presented in both micro and mesoscale is modelled using the coupled elastoplastic damage model proposed by Melro et al. [41], and is here implemented as a VUMAT user subroutine [35]. Before plasticity, the behaviour of the epoxy is assumed to be linear-elastic. A non-associative flow rule, to prevent positive volumetric plastic strain under a hydrostatic pressure is used, together with the paraboloidal yield criterion proposed by Tschoegl [42]:

$$f(\boldsymbol{\sigma}, \sigma_{Y_c}, \sigma_{Y_t}) = 6J_2 + 2(\sigma_{Y_c} - \sigma_{Y_t})I_1 - 2\sigma_{Y_c}\sigma_{Y_t}, \quad (2)$$

where σ_{Y_c} and σ_{Y_t} are the absolute values of the compressive and tensile yield strengths, $I_1 = \text{tr}(\boldsymbol{\sigma})$ is the first stress invariant, and $J_2 = \frac{1}{2} \boldsymbol{s} : \boldsymbol{s}$ is the second invariant of the deviatoric stress tensor, $\boldsymbol{s}$.

Figure 7: Representation of the multiscale approach.

The yield surface defined by the yield criterion solely depends on the tensile and compressive yield strengths that are both affected by hardening, depending on the equivalent plastic strain, ε_e^p , which is defined as:

$$\varepsilon_e^p = \sqrt{\frac{1}{1 + 2\nu_p^2} \varepsilon^p : \varepsilon^p}, \quad (3)$$

The thermodynamically-consistent isotropic damage model only uses one damage variable, d_m , which affects the stiffness of the epoxy resin. The damage onset is defined by the following damage activation function:

$$F_m^d = \phi_m^d - r_m, \quad (4)$$

where r_m is an internal variable related to d_m , and ϕ_m^d represents the loading function, which is defined by:

$$\phi_m^d = \frac{3\tilde{J}_2}{X_m^c X_m^t} + \frac{\tilde{I}_1(X_m^c - X_m^t)}{X_m^c X_m^t}, \quad (5)$$

where X_m^c and X_m^t represent the compressive and tensile strengths of the material, while invariants $\tilde{J}_2$ and $\tilde{I}_1$ are determined using the effective stress tensor. Mesh size dependency is avoided in the model through the usage of the Bazant and Oh's crack band model [43].

Finally, the matrix damage variable, d_m is defined as:

$$d_m = 1 - \frac{e^{A_m(3-\sqrt{7+2r_m^2})}}{\sqrt{7+2r_m^2}-2}, \quad (6)$$

where A_m is a parameter that must be computed for each element of the mesh.

For more details, the reader is referred to [41, 44].

3.2. Fibrous reinforcements

The reinforcing material is considered to be linear elastic up to failure and to have a transversely isotropic behaviour. A thermodynamically-consistent isotropic damage model is also used, which is only activated by the longitudinal stress component. Therefore, only one damage variable is used to affect the different stiffnesses of the material. The damage activation function is defined as:

$$F_f^d = \phi_f^d - r_f, \quad (7)$$

where ϕ_f^d is the loading function:

$$\phi_f^d = \frac{\tilde{\sigma}_{11}}{X_f^t}, \quad (8)$$

and r_f is an internal variable related to d_f . The loading function is a function of the fibre tensile strength, X_f^t , which has a stochastic value and will vary from element to element [45]. A random value for the tensile strength of the fibres is assigned to each element of their mesh using the following Weibull distribution:

$$X_f^t = \sigma_0 \left[-\frac{L_0}{L} \ln(1-X) \right]^{1/m_0}, \quad (9)$$

where σ_0 is the Weibull strength, m_0 is the Weibull parameter, L_0 is the reference length, L is the gauge length, i.e. the length of the RVE, and X is a random scalar generated in the open interval $[0,1]$. To avoid mesh size dependency problems and to control the energy dissipated in the fracture process, Bažant and Oh's crack band model [43] was also implemented.

Finally, the damage evolution law defined for the fibres is given by:

$$d_f = 1 - \frac{e^{A_f(1-r_f)}}{r_f}, \quad (10)$$

where A_f is a parameter that must be computed for each element of the mesh.

For more details on the damage model, the reader is referred to [45].

3.3. Homogenised tows

The tows presented at the mesoscale framework are modelled using an intralaminar damage model developed by the Advanced Composites Research Group (ACRG) at Queen's University Belfast [46, 47, 48, 49, 50]. The damage response is assumed to be linear elastic up to failure in the longitudinal and transverse directions, and inelastic in shear. A quadratic strain based failure criterion is employed to model tensile and compressive damage initiation in the longitudinal direction:

$$F_{11}^{t(c)} = \left(\frac{\varepsilon_{11}}{\varepsilon_{11}^{0t(c)}} \right)^2, \quad (11)$$

where F_{11}^t and F_{11}^c are the failure indices for tension and compression, respectively. Damage initiates when $F_{11}^{t(c)} \geq 1$. The tensile and compressive fibre failure initiation strains are represented by ε_{11}^{0t} and ε_{11}^{0c} , respectively.

The failure criterion used to capture the transverse and through-thickness matrix-dominated damage initiation was the one proposed by Catalanotti et al. [51]:

$$F_{mat} = \left(\frac{\sigma_{NN}}{S_{23}^{is}} \right)^2 + \left(\frac{\sigma_{NT}}{S_{23}^{is}} \right)^2 + \left(\frac{\sigma_{NL}}{S_{12}^{is}} \right)^2 + \lambda \left(\frac{\sigma_{NN}}{S_{23}^{is}} \right) \left(\frac{\sigma_{NL}}{S_{12}^{is}} \right)^2 + \kappa \left(\frac{\sigma_{NN}}{S_{23}^{is}} \right), \text{ for } \sigma_{NN} > 0, \quad (12)$$

$$F_{mat} = \left(\frac{\sigma_{NT}}{S_{23}^{is} - \mu_{NT}\sigma_{NN}} \right)^2 + \left(\frac{\sigma_{NL}}{S_{12}^{is} - \mu_{NL}\sigma_{NN}} \right)^2, \text{ for } \sigma_{NN} \leq 0, \quad (13)$$

where F_{mat} is the failure index for matrix tensile and compressive failure, and σ_{ij} ($i, j = N, T, L$) are the stresses acting on the fracture surface of an UD lamina, as shown in Figure 8. Parameters κ and λ are defined by $\lambda = 2\mu_{NL}S_{23}^{is}/S_{12}^{is} - \kappa$, and $\kappa = ((S_{12}^{is})^2 - (Y^{t,is})^2)/(S_{23}^{is}Y^{t,is})$, where S_{12}^{is} and S_{23}^{is} are the in-situ in-plane and out-of-plane shear strengths, respectively. The transverse friction coefficients, μ_{NT} and μ_{NL} , are defined based on Mohr-Coulomb's theory, where $\mu_{NT} = -1/\tan(2\theta_f)$, $S_{23}^{is} = Y^{c,is}/(2\tan(\theta_f))$, and $\mu_{NL} = \mu_{NT}S_{12}^{is}/S_{23}^{is}$. $Y^{t,is}$ and $Y^{c,is}$ are the in-situ transverse tensile and compressive strength, respectively.

Different damage variables are used to affect the stiffness of the material, and each one is related to a specific failure mode. Damage variables, d_{11}^t and d_{11}^c , refer to fibre-dominated tensile and compressive damage, respectively. d_{mat} indicates the evolution of matrix damage due to a combination of transverse tension/compression and shear loading,

$$d_{11}^{t(c)} = \frac{\varepsilon_{11}^{ft(c)}}{\varepsilon_{11}^{ft(c)} - \varepsilon_{11}^{0t(c)}} \left(1 - \frac{\varepsilon_{11}^{0t(c)}}{\varepsilon_{11}^{t(c)}} \right), \quad (14)$$

Figure 8: Schematic representation of the fracture plane and corresponding coordinate system.

$$d_{mat} = \left(\frac{\varepsilon_r^f - \varepsilon_{r,in}^0}{\varepsilon_r^f - \varepsilon_r^0} \right) \left(\frac{\varepsilon_r - \varepsilon_r^0}{\varepsilon_r - \varepsilon_{r,in}^0} \right). \quad (15)$$

The longitudinal modulus is reduced according to the damage parameter, d_{11} :

$$d_{11} = \max\{d_{11}^t, d_{11}^c\}. \quad (16)$$

The failure initiation strains, $\varepsilon_{11}^{0t(c)}$, are determined by the stiffness of the material and longitudinal strength, $X^{t(c)}$. The failure strains, $\varepsilon_{11}^{ft(c)}$, are determined by the longitudinal fracture toughness, $\mathcal{G}_{I(C)c}^{11}$, characteristic length, l_{fib} , and $X^{t(c)}$:

$$\varepsilon_{11}^{ft(c)} = \frac{2\mathcal{G}_{I(C)c}^{11}}{X^{t(c)}l_{fib}}, \quad (17)$$

where l_{fib} is determined by $l_{fib} = V_0^e/A^e$. V_0^e is the undeformed volume of the element, and A^e is the fracture surface area calculated using an approach proposed by Tan et al. [47]. In equation (15), ε_r is the l^2 -norm of strains acting on the fracture plane. $\varepsilon_{r,in}^0$ is the l^2 -norm of inelastic strains at damage initiation. ε_r^0 and ε_r^f are the l^2 -norms of strains corresponding to initial and final damage, respectively. The failure strain is defined by:

$$\varepsilon_r^f = \left(\frac{2\mathcal{G}_{rc}^{22}}{\sigma_r^0 l_{mat}} - g_0 \right) + \varepsilon_r^0, \quad (18)$$

where σ_r^0 is the stress at damage initiation. Using a quadratic interpolation function [47], the different matrix-dominated fracture toughnesses and volumetric strain energies are combined into single

Figure 9: Example of an RVE generated using a modification of [54].

parameters, $\mathcal{G}_{rc}^{22}$, and g_0 , respectively.

For more details about the theoretical foundations of the intralaminar damage model, the reader is referred to [46, 47, 48, 49, 50].

3.4. Cohesive interfaces

Fibre-matrix and tow-matrix interfaces are modelled using zero-thickness cohesive elements available within the FE software Abaqus[®] [35]. A bilinear traction separation behaviour is assumed. Damage initiation is predicted using a stress-based quadratic failure criterion [52]. Propagation of damage is evaluated according to the Benzeggagh-Kenane (BK) law [53] under mode I, mode II and mixed-mode. The interfacial damage variable, d_i is defined as:

$$d_i = \frac{\delta_m^f (\delta_m^{\max} - \delta_m^0)}{\delta_m^{\max} (\delta_m^f - \delta_m^0)}, \quad (19)$$

where, $\delta_m^f = 2\mathcal{G}_c^i / \tau_{\text{eff}}^0$ with, $\mathcal{G}_c^i$, as the mixed mode fracture toughness, and τ_{eff}^0 as the effective traction at damage initiation. $\delta_m^{\max}$ refers to the maximum value of the effective displacement attained during the loading history, and δ_m^0 is the displacement at damage initiation [35].

4. FE models: geometry, material properties and boundary conditions

4.1. At the microscale

The RVEs are generated using an already developed fibre distribution algorithm developed by Catalanotti [54], which is able to create random distributions of uniform spherical or circular particles for any given fibre volume fraction. Figure 9 shows an example of an RVE with a random distribution of fibres.

The mechanical properties of the constituents and fibre-matrix interface considered here are shown in Tables 3, 4, and 5, respectively. The authors recognise that the mechanical characterisation of the fibre-matrix interface is still problematic, especially the associated critical energy release rate. Nevertheless, the parameters used in this work are based on the available experimental data [55, 56, 57] and also on previous micromechanical simulations [36, 37, 44, 58, 59, 60, 61]. The interface between tows and matrix is assumed to have the same strength as the fibre-matrix interface. However, tougher values are used, i.e. the same toughness as the epoxy, $\mathcal{G}_{Ic}^i = \mathcal{G}_{IIc}^i = \mathcal{G}_{IIIc}^i = 0.09$ N/mm.

Material property	Value
Young's modulus	
E_m [MPa]	3760
Poisson's ratio	
ν_m	0.39
Plastic Poisson's ratio	
ν_p	0.3
Tensile strength	
X_m^t [MPa]	93
Compressive strength	
X_m^c [MPa]	180
Mode I fracture toughness	
$\mathcal{G}_{Ic}^m$ [N/mm]	0.09
Density	
ρ_m [kg/mm ³]	1.3×10^{-6}

Table 3: Matrix material properties [44, 62].

RVEs with in-plane dimensions of $15r$ and with a longitudinal dimension of $4r$ are used [44]. However, the RVEs submitted to a longitudinal tensile loading case, have a longitudinal dimension of thirty times the fibre radius ($30r$). The transverse and longitudinal dimensions of the RVEs play a role on the homogenised mechanical response, namely under longitudinal tension, where sufficiently

Material property	Value
Fibre diameter	
$2r$ [mm]	0.007
Young's moduli	
E_{11}^f [MPa]	234000
E_{22}^f [MPa]	15000
Poisson's ratio	
ν_{12}^f	0.2
Shear moduli	
G_{12}^f [MPa]	15000
G_{23}^f [MPa]	7000
Mode I fracture toughness	
$\mathcal{G}_{Ic}^f$ [N/mm]	0.004
Weibull parameters	
σ_0 [MPa]	4275
m	10.7
l_0 [mm]	12.7
Density	
ρ_f [kg/mm ³]	1.78×10^{-6}

Table 4: AS4 carbon fibre material properties [45, 63].

big dimensions are needed, in order to capture the ineffective length of the fibres and the clustering process leading to the ultimate failure of the material [64]. However, the appropriate definition of the dimensions of the RVEs, under longitudinal tension, is outside the scope of the present work, and therefore the aforementioned dimensions were deemed sufficient. Both fibres and matrix are modelled by means of C3D8R, three-dimensional, reduced integration linear hexahedral elements, with an average size of $0.7 \mu\text{m}$.

Material property	Value
Interface stiffness	
K [N/mm ³]	10 ⁶
Interface strengths	
τ_1^0 [MPa]	75
τ_2^0 [MPa]	75
τ_3^0 [MPa]	50
Interface critical energy release rates	
$\mathcal{G}_{Ic}^i$ [N/mm]	0.002
$\mathcal{G}_{IIc}^i$ [N/mm]	0.006
$\mathcal{G}_{IIIc}^i$ [N/mm]	0.006
Mixed-mode interaction parameter (BK law [53])	
η_{BK}	1.45

Table 5: Interfacial properties [36, 37, 44].

4.2. At the mesoscale

Through an efficient modelling strategy, mesh conforming between tows and matrix is obtained, and it is possible to model the compacted tows by means of C3D8R, three-dimensional, reduced integration linear brick elements. This represents an advantage when comparing with the methodology used by Doitrand et al. [29, 30], since they were only able to model tows with a free meshing algorithm, with tetrahedral elements, which may not be the most adequate way to model damage, since it is well known that for highly orthotropic materials, mesh alignment is a must to avoid mesh-induced direction bias [65]. All necessary sets and surfaces were previously defined in the compaction simulation, enabling a correct definition of the material orientation of each tow inside the compacted RUC. The epoxy matrix at the mesoscale, since it represents a complex geometrical part, is modelled by means of C3D4, three-dimensional tetrahedral continuum solid elements. Both tows and matrix are modelled with elements with an average size of 0.03 mm. This mesomechanical framework has already been used to numerically analyse the effect of the notch tip radius on the mode I intralaminar fracture toughness of this type of material [66].

The elastic and strength mechanical properties of the tows are computed through micromechanical analyses that are conducted in Section 5.1. However, the model further requires as an input, seven

other material properties which are far more complicated to obtain using micromechanical simulations (for more information, the reader is referred to, e.g. [67, 68]), which are the values of the fracture toughnesses: the longitudinal mode I and compressive intralaminar fracture toughness, $\mathcal{G}_{Ic}^{11}$ and $\mathcal{G}_{Cc}^{11}$, respectively, the transverse mode I and compressive intralaminar fracture toughness, $\mathcal{G}_{Ic}^{22}$ and $\mathcal{G}_{Cc}^{22}$, respectively, and the shear matrix dominated intralaminar fracture toughness, $\mathcal{G}_{IIc}^{12}$, $\mathcal{G}_{IIc}^{13}$, and $\mathcal{G}_{IIc}^{23}$. The values of $\mathcal{G}_{Ic}^{11}$ and $\mathcal{G}_{Cc}^{11}$ considered here are the ones obtained by Catalanotti et al. [69, 70], which are $\mathcal{G}_{Ic}^{11} = 101.5 \text{ kJ/m}^2$ and $\mathcal{G}_{Cc}^{11} = 61 \text{ kJ/m}^2$. The values used for the transverse damage progression are reported to be similar to the corresponding interlaminar fracture toughness values [71]. Since the interlaminar properties of the material system IM7/8552 are well documented [72], they are used throughout the analyses: $\mathcal{G}_{Ic}^{22} = 0.277 \text{ kJ/m}^2$, and $\mathcal{G}_{Cc}^{22} = \mathcal{G}_{IIc}^{12} = \mathcal{G}_{IIc}^{13} = \mathcal{G}_{IIc}^{23} = 0.788 \text{ kJ/m}^2$.

5. Numerical predictions

The numerical simulations were conducted using the FE solver Abaqus[®]/Explicit [35]. The objective of these simulations was to mechanically characterise the tows along their length through micromechanical simulations, and to evaluate the different mechanical response that distinct modelling approaches of RUCs present, and the effect of nesting considerations when modelling this type of material. In order to avoid numerical errors due to excessive element distortion, damaged elements have been removed throughout the simulations according to the following strategy:

$$\text{Delete element if} = \left\{ \begin{array}{l} d_m > 0.99 \\ d_f > 0.99 \\ d_{11} > 0.99 \\ \det \mathbf{F} \leq 0.1 \vee \det \mathbf{F} \geq 3.0 \end{array} \right\}, \quad (20)$$

where $\det \mathbf{F}$ yields the ratio of the deformed volume, V^e , to the undeformed, V_0^e , volume of an element $\det \mathbf{F} = V^e/V_0^e$.

5.1. At the microscale

At the microscale, the intention is to homogenise the mechanical properties of the tows through volumetric homogenisation:

$$\sigma_{ij}^0 = \frac{1}{V^{\text{RUC}}} \int_V \sigma_{ij} \, dV = \frac{1}{V^{\text{RUC}}} \sum_{k=1}^{N_p} \sigma_{ij}^k V^k, \quad (21)$$

where σ_{ij}^0 represents the homogenised far-field stress tensor, σ_{ij}^k and V^k are the stress component determined at the integration point, k , and associated volume, and N_p is the total number of integration points in the RVE/RUC, and V^{RUC} is the volume of the RUC.

After assigning the appropriate constitutive material models to each of the constituents and the fibre-matrix interface, it is possible to address the mechanical performance of the RVEs. The strength and elastic properties of the tows were determined by submitting different RVEs to 3D PBCs and different loading conditions, following Melro et al. [44]. The micromechanical simulations included pure longitudinal tension, transverse tension and compression, and in-plane and out-of-plane shear stress states. The RVEs have three different fibre volume fractions, i.e. $\omega_f^{\text{RVE}} = 35\%$, $\omega_f^{\text{RVE}} = 55\%$, and $\omega_f^{\text{RVE}} = 75\%$. Per fibre volume fraction, five RVEs having distinct fibre distributions are generated to assess microstructural randomness. The purpose of choosing three RVEs having different fibre volume fractions was to: i) analyse the mechanical behaviour of the composite having a more non-linear matrix-dependent behaviour, i.e. ductile and weak ($\omega_f = 0.35$) and a more linear, fibre-dependent behaviour, i.e. brittle and strong ($\omega_f = 0.75$), capturing a wider spectrum of the behaviour of the material; and ii) obtain three different representative points, from which second order polynomial curve fitting expressions are generated, enabling the evaluation of the mechanical properties along the length of the tows. Figure 10 and 11 show, respectively, the quantitative and qualitative numerical predictions for all the aforementioned loading conditions. The contour plots shown are related to the equivalent plastic strain (equation (3)) of a deformed RVE with a fibre volume fraction of $\omega_f^{\text{RVE}} = 55\%$. The highlighted points on the homogenised stress-strain curves represent the peak homogenised stresses.

For all loading scenarios, it is shown that stiffer and more brittle behaviour results with increasing fibre volume fraction. The RVEs submitted to longitudinal tension showed that the first fibre failure occurred in the middle, leading to other fibre failures in the vicinity, in different sections of their lengths through stress concentrations, followed by final damage of the RVE [45]. Damage propagated perpendicularly to the load, in the RVEs submitted to transverse tension, along the fibre matrix-interfaces. The RVEs submitted to transverse compression failed at an angle which is comparable with previously conducted experimental observations [73, 74], i.e. approximately 53° to the vertical. The RVEs subjected to longitudinal shear failed with an horizontal damage band. And finally, for the case of transverse shear, due to the fibre-matrix interfacial behaviour, the failure tends to occur in a diagonal manner, where the matrix failure occurs in a plane roughly perpendicular to the maximum principal macro-stress [44]. The longitudinal compressive strengths of the tows should not influence the numerical predictions at the mesoscale. Therefore, a constant value of $X^c = 1000$ MPa was used throughout the simulations.

Table 6 summarises the results of the mean, minimum, and maximum values of the homogenised mechanical properties for the three different fibre volume fractions. The value of the homogenised density was obtained following Chamis' rule of mixtures.

Figure 10: Contour plots of the equivalent plastic strain (equation (3)) in deformed RVEs having a fibre volume fraction of $\omega_f^{\text{RVE}} = 55\%$ when submitted to: (a) longitudinal tension; (b) transverse tension; (c) transverse compression; (d) in-plane shear; and (e) out-of-plane shear.

Figure 11: Numerical predictions of the stress-strain curves when submitting different fibre volume fraction RVEs to different loading scenarios: (a) longitudinal tension; (b) transverse tension; (c) transverse compression; (d) in-plane shear; and (e) out-of-plane shear. The plots shown are for RVEs which have the same fibre distribution.

	$\omega_f^{\text{RVE}} = 35\%$			$\omega_f^{\text{RVE}} = 55\%$			$\omega_f^{\text{RVE}} = 75\%$		
M. property	Mean	Min	Max	Mean	Min	Max	Mean	Min	Max
E_{11} [MPa]	83791	82145	84568	127311	12704	127400	170751	170011	170956
E_{22} [MPa]	7701	7604	7856	9054	9024	9065	10793	10785	10865
ν_{12} [-]	0.332	0.323	0.341	0.293	0.292	0.295	0.242	0.240	0.242
G_{12} [MPa]	3448	3341	3544	4880	4865	4899	7204	6875	7555
G_{23} [MPa]	2549	2423	2605	3156	3141	3162	4312	4302	4400
$10^6 \rho$ [kg/mm ³]	1.47	—	—	1.56	—	—	1.66	—	—
X^t [MPa]	1653	1523	1804	2445	2305	2502	2744	2680	2845
X^c [MPa]	1000	—	—	1000	—	—	1000	—	—
Y^t [MPa]	41	37	44	48	45	49	53	51	57
Y^c [MPa]	102	93	119	131	120	142	151	143	159
S_{12} [MPa]	41	39	43	53	49	55	63	59	67
S_{23} [MPa]	37	35	38	40	38	43	44	42	50
$\mathcal{G}_{Ic}^{11}$ [N/mm] [69]	101.5	—	—	101.5	—	—	101.5	—	—
$\mathcal{G}_{Cc}^{11}$ [N/mm] [70]	61	—	—	61	—	—	61	—	—
$\mathcal{G}_{Ic}^{22}$ [N/mm] [72]	0.277	—	—	0.277	—	—	0.277	—	—
$\mathcal{G}_{Cc}^{22}$ [N/mm] [72]	0.788	—	—	0.788	—	—	0.788	—	—

Table 6: Properties of the homogenised tows.

5.2. At the mesoscale

5.2.1. Comparison of modelling approaches

A computational comparison of different approaches to model a plain weave carbon fibre RUC was made by evaluating the mechanical behaviour and progressive damage of different perfectly stacked RUCs, when subjected to a uniaxial longitudinal tensile load and to pure in-plane shear. The three different RUCs' geometries were: i) one ply submitted to 3D PBCs, simulating an infinite laminate in all three directions; ii) four plies; and iii) eight plies. The latter two are subjected to in-plane PBCs [19, 36, 37].

By using volumetric homogenisation (equation (21)), Figure 12 shows the quantitative (Figure 12a) and qualitative (Figure 12b) numerical predictions of the normalised homogenised stress-strain curves, where σ_{11}^{0C} is the peak homogenised stress of the one ply RUC submitted to 3D PBCs. Different points are indicated and associated with different stages of the damage process: A) initiation of observed non-linear behaviour mostly due to matrix plasticity along the contact between the edges of the tows and the matrix; B) total rupture of the transverse outer plies, leading to a greater decrease in stress

for the RUCs subjected to 2D PBCs; C) laminate failure along the matrix rich regions.

The qualitative predictions were fairly similar between all three RUCs. The contour plots presented in Figure 12b validate the present framework, since they fully agree with the observations carried out by Daggumati et al. [75, 76], indicating that, under longitudinal tension, an inner layer will first trigger transverse damage at the edges of the crimped weft tows, while an outer layer will have transverse damage concentrated at the crimp regions of the weft tows. Looking to the quantitative predictions, it can be seen that the homogenised stress-strain curves were different. The most conservative mechanical performance was the one ply RUC submitted to 3D PBCs. This RUC represents an inner ply which is embedded in an infinite laminate in all three directions, and with that being said, it does not model the behaviour of the outer plies, which are free to deform in the out-of-plane direction (z-direction), leading to higher stresses in the outer plies [76]. Thus, homogenising this behaviour would give more conservative results in terms of stress-strain distribution and peak stress. Figure 13 shows the contour plots of the matrix damage inside the tows, and the corresponding transverse stress distributions along their centreline, for an outer ply tow (Figure 13a), and inner ply tow (Figure 13b).

The outer ply weft tow shows a non-uniform transverse stress distribution along its length, where damage starts earlier at its crimp regions, leading to an earlier damage initiation. However, the inner weft tow presents a uniform distribution of the transverse stress along its length, delaying damage initiation. Another important remark is the fact that the four plies RUC submitted to in-plane PBCs showed the poorest mechanical performance. This is due to the fact that not enough plies were modelled, creating a laminate which is more free to deform in the out-of-plane direction, and thus, damage starts earlier in the outer plies, leading to an earlier damage propagation along the RUC.

When submitting the RUCs to pure in-plane shear, the same trends of the uniaxial longitudinal case are obtained, i.e. the infinite laminate showed a more conservative response than the other two, and the four plies a poorer response. However, here the difference is not as great as for the one of the longitudinal uniaxial loading condition. Figure 14 shows the quantitative (Figure 14a) and qualitative (Figure 14b) numerical predictions of the normalised homogenised shear stress-shear strain curves using different approaches to model the plain weave, where τ_{12}^{0C} is the peak homogenised shear stress of one ply RUC submitted to 3D PBCs. Different points are indicated and associated with different stages of the damage process: A) the RUC is no longer in the elastic domain, where plasticity mainly concentrates in the resin rich pockets; B) severe matrix plasticity and matrix damage in the tows; C) laminate failure along the edges of the tows.

Analysing the distribution of matrix damage inside an inner and an outer longitudinal tow (see Figure 15), it can be seen that the differences for this loading condition are almost negligible, indicating that for in-plane shear, the out-of-plane deformation caused to an inner and an outer ply is very similar [76].

(a) Numerical predictions of the homogenised stress-strain curves for different modelling approaches. The red points indicate the normalised failure stress.

(b) Contour plots of: A) equivalent plastic strain ("Eq. P. Str.") in the matrix and Von Mises stress ("S. Mises") in the tows; B) matrix damage variable ("Matrix damage") and matrix damage in the tows ("Tows matrix damage"); C) matrix damage variable ("Matrix damage") and fibre tensile damage in the tows ("Tows fibre damage"). The contour plots shown are related to the one ply submitted to 3D PBCs.

Figure 12: Numerical predictions of three different perfectly stacked RUCs submitted to a uniaxial longitudinal loading condition.

(a) Outer ply weft tow.

(b) Inner ply weft tow.

Figure 13: Numerical predictions of the distribution of the transverse stress (global x -direction) along a centreline of the weft tows, with corresponding contour plots of the matrix damage variable inside the tows (equation (15)).

(a) Numerical predictions of the homogenised shear stress-shear strain curves for different modelling approaches. The red points indicate the normalised failure stress.

(b) Contour plots of: A) Von Mises stress ("S. Mises"); B) equivalent plastic strain ("Eq. P. Str.") in the matrix and matrix damage in the tows ("Tows matrix damage"); C) matrix damage variable ("Matrix damage") and matrix damage in the tows ("Tows matrix damage"). The contour plots shown are related to the one ply submitted to 3D PBCs.

Figure 14: Numerical predictions of three different perfectly stacked RUCs submitted to a pure in-plane shear loading condition.

Figure 15: Contour plots of the matrix damage variable inside the tows (equation (15)).

Figure 16: Tows (dark blue - warp; light blue - weft) after compression step: A) perfectly stacked; B) maximum offsets and C) random offsets.

5.2.2. Effect of nesting

The role of nesting is addressed through the numerical comparison of the longitudinal tension and in-plane shear mechanical performance of three different eight-ply stacked nested RUCs: i) no offset between plies; ii) maximum offset between plies; and iii) random offsets between plies. Three different random RUCs are generated. Figure 16 shows the three different pos-compressed fabrics.

Figure 17 shows the numerical predictions (Figure 17a), involving the stress-strain curves and the modulus degradation (E_{11}^0 , and E_{11}^T are the undamaged and tangent longitudinal Young's modulus, respectively), as well as the corresponding qualitative results (Figure 17b), for the three different nested configurations. The experimental data reported in the plots was taken from Ito and Chou [12]. Since fibre tensile damage of the warp tows is what dictates laminate failure, the contour plots shown are related to the fibre tensile damage reported in equation (14).

The initial slope of the perfectly stacked RUC is smaller when comparing to the others. Based on the classical lamination theory, Ito and Chou [12] have shown that, under a uniaxial longitudinal tensile load, a plain weave composite exhibits a tension/out-of-plane shear coupling effect on the elastic behaviour, depending on ply shifting. When lamina shifting increases, this coupling effect tends to be less pronounced, leading to greater values of the longitudinal Young's modulus. This effect is captured using the present numerical framework. For more information regarding this effect following an analytical perspective, the reader is referred to [12]. The highest peak load was obtained for the maximum shifted RUC. This is due to the restraining out-of-plane movement caused by the presence

(a) Quantitative numerical predictions: 1) stress-strain curves and 2) longitudinal Young's modulus degradation curves.

(b) Qualitative numerical predictions involving the contour plots of the fibre tensile damage variable in the tows (equation (14)) at final failure, for: 1) no offsets; 2) maximum offsets; and 3) random offsets.

Figure 17: Numerical predictions of three different nested RUCs submitted to a uniaxial longitudinal loading condition.

of the maximum internal yarn shifting, leading to a greater fibre damage accumulation in the warp tows and less damage in the matrix material, causing the material to exhibit a non-linear behaviour at larger applied strains. On the other hand, in-phase stacking of all plies in the tows crimp regions led to early damage propagation, and to a lower peak load [76, 77]. Both maximum and random shifted plies showed a more linear behaviour, and consequently a slower damage propagation, as per comparison with the experimental results [12]. The non-linear behaviour captured by the perfectly stacked RUC is mostly due to the concentration of plasticity along the edges of the tows, which the constitutive material model for the matrix is able to capture [41], leading to a faster degradation of the Young's modulus, and a poorer mechanical performance. Despite the initial linear behaviour, the randomly stacked RUCs presented a more brittle behaviour in comparison with the other RUCs, reaching the corresponding peak load for lower applied strains.

Figure 18 shows the numerically predicted shear stress-shear strain curves, and corresponding shear modulus degradation (G_{12}^0 , and G_{12}^T are the undamaged and tangent in-plane shear modulus, respectively), as well as the contour plots of the matrix damage variable inside the tows (equation (15)), for the three different stacking sequences. The experimental data reported in the plots is retrieved from Medina et al. [14].

For this type of loading, the quantitative predictions were fairly similar between all three nested configurations. Comparing with the uniaxial case mentioned above, the RUCs are subjected to higher strain levels, and consequently the shear modulus becomes almost null before complete failure. Even though damage seems to propagate faster for the perfectly aligned RUC, all stacking sequences presented similar rates of damage propagation, which is notably comparable with the experimental observations [14]. As it has been previously reported in Section 5.2.1, for this type of BC, the mechanical response does not depend on the interaction between plies, thus layer shifting has a minimum influence on the overall macroscopic response.

With Figures 17 and 18, it can be seen that, when modelling damage, nesting needs to be taken into account when modelling woven composite materials, since they induce different damage initiation mechanisms, and consequently, final failure scenarios, namely under in-plane longitudinal tensile loading conditions. Thus, care must be taken when using a 3D infinite RUC to model this type of material. Remarkably, both constitutive material models [41, 47, 48] were able to capture the rate of damage progression of the different RUCs, as shown in Figures 17a and 18a.

6. Conclusions

A multiscale modelling strategy, incorporating thermodynamically consistent damage models [41, 47, 48] in an efficient micro-meso multiscale framework, was developed to evaluate the mechanical

(a) Quantitative numerical predictions: 1) shear stress-shear strain curves and 2) in-plane shear modulus degradation curves.

(b) Qualitative numerical predictions involving the contour plots of the matrix damage variable (equation (15)), in the tows at laminate failure, for: 1) no offsets; 2) maximum offsets; and 3) random offsets.

Figure 18: Numerical predictions of three different nested RUCs submitted to an in-plane shear loading condition.

behaviour of 2D woven textile composite materials, overcoming several computational limitations previously reported.

The homogenised tows at the mesoscale were first compacted in a prior simulation, where their mechanical properties were assumed to be the ones of a dry preform. Woven layers with different stacking sequences were submitted to 2D PBCs and compressed, making use of two compression plates. Realistic cross-sectional shapes of the tows are generated, causing an intra-tow fibre volume fraction variability along their length [3, 7]. Therefore, different mechanical properties were assigned to the mesh of the tows. These mechanical properties were previously obtained by homogenising the behaviour of 3D periodic RVEs, which describe the micromechanical behaviour of the composite. The compaction simulations showed that, depending on the considered gap between plies, the assumption regarding that the variation of the cross-sectional area along the length of the tows is periodic, may not be accurate. This suggests that, to accurately model the behaviour of the material, proper measurements of the geometrical features of the weaves need to be conducted (e.g. through μ -CT scanning).

Having the mesoscale completely defined, and by assigning the appropriate constitutive material models [41, 47, 48], a study was undertaken to further understand the limitations of modelling damage in this type of material with a small amount of plies. Perfectly stacked RUCs having a different number of plies were compared under in-plane loading conditions. A 3D infinite laminate (one ply submitted to 3D PBCs) exhibited the most conservative response, since it does not model outer plies, which are the ones having a higher out-of-plane deformation [75, 76], and a more uniform centred stress distribution along their length. However, modelling a 2D infinite RUC with insufficient plies may cause an earlier damage initiation mechanism and a final failure scenario, induced by the early breakage of the outer plies.

The effect of ply shifting on the mechanical response was also a topic of analysis. Under a uniaxial tensile load, the numerical predictions showed that perfectly stacked laminates along the crimp regions of the tows show a more non-linear behaviour, which is caused by the amount of matrix plasticity along their edges. Therefore, a perfectly stacked RUC shows a faster progression of damage than the other RUCs. The RUC having the maximum ply shifts showed that it better restrains damage. Under in-plane shear, all responses were fairly similar, since under this type of load, the mechanical response does not depend on the interaction between plies. Similar trends were obtained when comparing the numerical predictions with previously conducted experimental observations for both loading conditions [12, 14].

Concluding, with the numerical simulations conducted here, it is evident that simplified geometries or single ply RUCs cannot properly model damage. Normalised comparisons were made, since the experimental data retrieved from the available literature uses a different material system than the one studied here. Nevertheless, both damage models for the resin [41], and for the tows [47, 48] were

able to remarkably replicate the rate of damage progression in different RUCs under in-plane loading conditions.

Declarations of interest

None.

Data availability

Datasets related to this article can be found at <http://dx.doi.org/10.17632/sr5hsxxhb3.1>, an open-source online data repository hosted at Mendeley Data.

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