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Lens-loaded Cavity Antenna with Detector Diode as a Direction-of-Arrival Estimator

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Abstract—This letter proposes a novel direction-of-arrival (DoA) estimation approach which uses a lens-loaded, coded aperture antenna connected to a detector diode for millimeter-wave (mmWave) frequencies. The presented approach exploits three distinct, but closely related properties of mmWave communication front-end hardware: First, the quasi-random radiation modes created by a lens-loaded cavity antenna; Second, the frequency-diverse impulse response of over-sized metallic cavities; Third, the sensitivity of detector diodes at mmWave frequencies. Critically, we use a combination of the synthesis approach and experimental results to demonstrate that DoA estimation is possible with less complex hardware as compared to conventional methods, where an array of mmWave antennas is typically employed for DoA estimation. Bandwidth-to-accuracy trade-off is thoroughly studied, which is an important commercial matrix. It is demonstrated that the lens-loaded cavity antenna with a detector diode circuit can be an apt choice for DoA estimation. Finally, it is shown that the proposed approach provides fast and accurate DoA estimation, thus inherently suitable for DoA estimation in future mmWave systems.

Index Terms—B5G, channel estimation, detector diode, direction-of-arrival estimation, frequency-diverse antenna, lens antenna, millimetre-wave.

I. INTRODUCTION

ACCURATE direction-of-arrival (DoA) information is a key requisite of mmWave channel sounding. Typically, an array of antennas and associated radio frequency (RF) hardware is employed for DoA estimation, in conjunction with techniques such as the ESPRIT [1], Capon [2], Bartlett [3] and MUSIC [4], [5] algorithms. The development of antenna arrays can be both complex and costly at mmWave frequencies. Notwithstanding the number of antennas required to provide sufficient angular discrimination, high path loss at mmWave frequencies requires a greater number of antennas in an array formation, thereby increasing the complexity of radio hardware. Recently, a number of mmWave antenna hardware simplification approaches have been investigated, which focus on classical beam synthesis [3], [6]–[9]. Highly directive,

Fig. 1: System block diagram showing lens-loaded cavity antenna and estimator module.

frequency-diverse antenna apertures have also been shown to be a promising alternative to a fully connected antenna array. Frequency diverse antenna apertures use microwave computational imaging concepts (e.g. [10]–[14]), where field-of-view (FoV) information is captured. Recently, it has been shown that channel information within a FoV (in terms of far-field radiation) can also be constructed from quasi-random measurement modes using computational techniques [15]. In this context, in [15], a preliminary theoretical investigation of DoA estimation using a mode-mixing cavity was presented. However, this was limited by the use of a hypothetical frequency-diverse antenna with high-Q factor. In [16], a numerical and experimental validation of DoA estimation using a lens-loaded cavity aperture was presented. These works use computational methods for the DoA estimation.

This work proposes a novel DoA estimation approach that requires a lens-loaded frequency-diverse antenna connected to a detector diode circuit as a mmWave receiver. One of the main drawbacks of the aforementioned studied techniques is their reliance on a high bandwidth. In this contribution, we show that DoA estimation is possible using significantly less bandwidth compared to computational techniques proposed in [15] and [16]. This is made possible using the proposed estimation technique which exploits the classical concept of power detection to translate the DoA information at the output of a lens-loaded cavity antenna into a detectable voltage.

II. PROPOSED DOA ESTIMATION TECHNIQUE

The proposed system block diagram is given in Fig. 1, where a *lens-loaded cavity* is connected to a base-band signal processing unit via an *estimator module*. The lens loaded cavity is composed of an over-sized metallic hollow cavity with a curved opening comprising of an array of sub-wavelength holes. The cavity opening is covered with a constant- ϵ_r lens [17] that provides a high antenna gain. Typically, this required lens operation can be achieved when the dielectric constant (ϵ_r) value of the lens material is more than 2.0 and less

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Fig. 2: (a) Lens-loaded cavity antenna far-field gain patterns (color map is scaled from -27.8 to 12.2 dBi). (b) Photograph of fabricated lens-loaded cavity.

than 3.5. The lens structure used in this study has $\epsilon_r = 2.53$ which makes the focal point 3.5 mm. The lens is developed by machining out a sphere from Rexolite material having a loss tangent $\tan \delta = 0.00066$. Choice of lens material with this loss tangent means the wave propagating through the lens structure will suffer significantly less attenuation compared to the gain achieved due to lens operation. The mode mixing cavity has dimensions of approximately $18 \times 18 \times 18 \text{ cm}^3$, while the Rexolite lens has a diameter of 13.3 cm. For a standard base station application, $18 \times 18 \text{ cm}^2$ aperture size is practical. An arbitrarily oriented metallic scatterer of size around $3 \times 5 \text{ cm}^2$ is placed inside the chaotic cavity to introduce and enhance the mode-mixing capabilities by introducing quasi-random disorderly reflections. The metallic scatterer built inside that helps mode-mixing and also breaks the structural symmetry. The randomly oriented scatterer produces enough disorder in the chaotic cavity that for a specific fabricated lens-loaded cavity, the quasi-random radiation modes are very subjective and device specific. A detailed explanation of the construction of the lens-loaded cavity and rationale behind the use of the lens can be found in [16]. The estimator module in Fig. 1 comprises of an impedance matching network, a detector diode circuit, and a comparator system. The detector diode circuit is a two-port microwave device that rectifies a received radio signal. This is similar to the detectors widely used in amplitude modulation based radio receivers.

The primary objective of the detector diode circuit in Fig. 1 is to provide a voltage amplitude that is proportional to the received power at the output of the lens-loaded cavity antenna. Typically, an RF choke is connected in shunt and provides the required DC return necessary for the detector diode to provide the DC voltage to the comparator. The RF choke acts as an open circuit for the signal coming into the detector diode circuit. The shunt capacitance after the detector diode provides ground to the diode, which acts as an open circuit at detector's baseband bandwidth. Detector diode circuits are often packaged into power meters operating as a scalar network analyzers (e.g. Keysight N1922A and N8480). The detector diode block input impedance is generally not a good match to the conjugate of the lens-loaded cavity output, therefore, a matching network operating as an impedance transformer is required between the both. The output voltage (V) is directly proportional to the square root of the input signal power (W). The sensitivity of the detector diode is given in the form of an open-circuit voltage in mV per unit mW.

Fig. 3: Normalized voltage map at the output of detector diode circuit when normalized sum of multiple modes are used (color map scale 0–1 mV where red and blue are maximum and minimum respectively).

Hence, the estimator sensitivity S_{est} is given by

$$S_{est}(P_{av,c}) = \frac{V_d}{P_{av,d}(\theta, \phi)} \text{ (mV/mW)}, \quad (1)$$

where $P_{av,c}$ is the received signal power available at the lens-loaded cavity, θ and ϕ are the angular variation along elevation and azimuth directions within the FoV, V_d is the estimator output voltage, and $P_{av,d}$ is the power available at the input of the detector diode circuit.

The absolute V_d value depends on the load resistance, however, for the sake of simplicity and generality we used V_d values normalized to 1 mV in this study. Generally the detector diodes operate at a 0-bias, hence, a very low input power level at the output of the lens-loaded cavity can lead to estimator sensitivity deviation. One possible way to mitigate this deviation is to bias the detector diode circuit to match the comparator's voltage levels. For a given voltage level of the detector diode circuit, the comparator creates a binary output signal and provides it to the digital signal processing block. In the sequel, we present the hardware construction of the system architecture presented in Fig. 1 that can be used for DoA estimation.

III. MEASUREMENTS, RESULTS AND DISCUSSION

A proof-of-concept mmWave lens-loaded cavity hardware is used to investigate and demonstrate the proposed approach. When a mmWave signal excites the input of the lens loaded cavity, spatially diverse radiation patterns are observed (Fig. 2(a) shows an example of this at a frequency of 28 GHz). Conversely, impinging signals along (θ, ϕ) will experience a frequency-diverse transfer function. We propose to exploit this property of the lens-loaded cavity and differentiate the DoA of an impinging signal based on the direction dependent gain. To test this, we measured the frequency-diverse transfer function and spatially quasi-orthogonal radiation fields of a lens-loaded cavity antenna within the frequency range of 27 – 29 GHz (see

Fig. 4: Detector diode circuit output voltages indexed along azimuth and elevation FoV and sorted in ascending order to generate estimation masks when (a) 1 mode and (b) normalized sum of 11 modes are used (normalized color map scale).

Fig. 2(b)). The fields were recorded using a frequency sweep interval of 50 MHz, hence 41 radiation modes were captured within the 2 GHz bandwidth. It should be noted that there are always measurement discrepancies and fabrication anomalies with complex structures like the one used in this investigation, however, the lens-loaded cavity inherently operates at *quasi-randomness* of the radiation modes, and the fields recorded at the output of the cavity are very hardware specific. Hence, the measurement discrepancies are not considered to be a fundamental limit of the proposed approach. Another point to note here is that the fields at the output of the lens loaded cavity for a vertically polarized impinging signal are different from the fields observed for a horizontally polarized signal. Hence, measurements were performed separately for vertical and horizontal polarization. A vector sum of both polarization components results in defining the level of $P_{av,d}$ at a load impedance of 50Ω , measured using Keysight PNA 8361C. The voltage levels against $P_{av,d}$ at the output of the estimator block

Fig. 5: Comparison between normalized sum of V_d for multiple modes sorted in ascending order versus DoA estimation index.

in Fig. 1 are numerically evaluated in a post-processing step.

Output voltage maps (normalized to 1 mV) are presented in Fig. 3 against the impinging signal's measured $P_{av,d}$. The discrimination between the voltage level for different combinations of azimuthal elevation FoV can be clearly seen. One important point to note is that for a given mode, e.g. mode 1, the same normalized voltage level can be mistaken for more than one DoA which can lead to erroneous estimation. To overcome this, we propose the use of multiple modes to enhance the DoA estimation accuracy. For instance, a high number of distinct V_d values are observed for each DoA when a normalized sum of more than 1 V_d mode masks are used compared to the normalized V_d of 1 mode. For example, in Fig. 3 the normalized sum of V_d for 4, 11 and 41 modes is provided.

To further explain this, let us consider unique V_d values indexed against DoA estimation and sorted in ascending order to generate a DoA *estimation mask*. If we use only 1 mode to generate an estimation mask, the possibility of more than 1 DoA estimation overlaps is higher compared to when 11 modes are used to create a similar estimation mask. This can be visualized in Fig. 4 where the estimation masks for both these cases are illustrated. If the same quantization interval is used to index the DoA for a given normalized V_d , then the DoA estimation using a greater number of modes will naturally be better. However, there is a limit to this enhancement. To demonstrate this, let us observe the total number of DoA estimation indexes based on the measurement results versus normalized V_d in Fig. 4. In theory, half of the DoA estimation indexes should represent V_d values from 0 - 0.5, while the remaining half should represent V_d from 0.5 - 1. If we use 1 mode for DoA estimation, the majority of the DoA estimation indexes will be reserved for low V_d values, and vice versa. This can be solved by using a greater number of modes. Recalling the previous example, if we use 11 modes, 50% of the DoA estimation indexes will represent V_d values below 0.35, compared to below 0.22 when only 1 mode is used. The higher the number of modes used, the lower the number

Fig. 6: Number of DoA estimation overlaps (errors) vs the number of modes used for DoA estimation, compared for multiple values of ΔV_d .

of DoA estimation overlaps. Consulting Fig. 5, it is worth highlighting that although DoA estimation is better for the sum of 41 modes compared to the sum of 11 modes, the benefit is marginal. Based on this observation, there is a clear opportunity to conserve bandwidth, which is the most prominent feature of the proposed approach. The use of 11 modes requires only 0.55 GHz of bandwidth as compared to 2.00 GHz when 41 modes are used.

IV. BANDWIDTH-SENSITIVITY TRADE OFFS

It has been established in the previous section that the proposed approach can provide benefit in terms of bandwidth conservation. This section analyzes the trade-off between bandwidth and estimator sensitivity. Fig. 6 presents the overall number of DoA estimation overlaps (i.e. errors) versus the normalized sum of modes used for the DoA estimation. Here, measured $P_{av,d}$ values are used when the voltage resolution is varied, which depends upon the diode's S_{est} . For a low resolution ΔV_d , e.g. at ± 100 mV, there are 4412 errors, which decreases to 534 when 14 modes are used. The number of errors are observed to go as low as 113 when 41 modes are used. The same trend can be observed for higher ΔV_d resolution. This trend highlights that by using a better resolution for V_d , where V_d is directly proportional to the sensitivity, we can decrease the number of errors while operating at the same number of modes. For example, setting the number of modes to be 6, as the ΔV_d is varied from ± 100 mV to ± 0.1 mV, the number of errors decreases from 1789 to 1.

The choice of detector diode circuit is dependent upon the operational $P_{av,c}$ and $P_{av,d}$. Consider, for example, at $P_{av,d} = -30$ dBm, the Anritsu 70KA50 detector provides $V_d = 0.1$ mV with a load resistance is 1 k Ω , hence the operational S_{est} will be 100 mV/mW. It is worth mentioning that detectors with low tangential signal sensitivity (TSS) and high S_{est} should also be considered to achieve better DoA estimation accuracy within a given bandwidth (e.g. Pasternak PE8009-P with TSS = -52 dBm at 26 GHz). For detectors requiring higher input power, an additional RF amplification stage can be included before the matching network in Fig. 1, however, this should be implemented with caution as it may impact the overall linearity of the system. Note that the assumption that the spectrum of the incident plane-wave remains constant is valid as shown in

[16] since we are operating at a much higher frequency i.e. 28 GHz, with respect to the the variation across center frequency i.e. less than 1 GHz.

V. LIMITATIONS OF THE PROPOSED APPROACH

While the proposed approach marks a significant step towards achieving accurate DoA estimation using low complexity hardware, it does require some considerations. Firstly, the proposed approach requires the lens-loaded cavity to act only as a receiver, while an additional port will be required if the same cavity hardware is to be used as a transmitter. Secondly, calibration of the system in a controlled radio environment is required, especially when high-sensitivity and low bandwidth DoA estimation is to be achieved. A co-located antenna with uniform gain within the FoV is required for referencing $P_{av,c}$ to accurately develop the DoA estimation mask at a given S_{est} . Thirdly, to achieve high sensitivity over smaller bandwidth, the estimator module requires precision radio hardware. This is especially true for the detector diode and the transition between the lens-loaded cavity and estimator module. Lastly, high linearity of detector diode circuit is essential to facilitate accurate DoA estimation within the dynamic range $P_{av,d}$.

VI. CONCLUSIONS

This letter has proposed a novel DoA estimation technique that utilizes a frequency-diverse lens-loaded cavity antenna and a mmWave receiver. The new approach makes use of a detector diode circuit with frequency-diverse antenna, to translate the DoA of an impinging signal into a detectable voltage level. The major contribution is the estimation technique that uses two distinct modules combined in a simplified fashion. A bandwidth conservation of $\sim 70\%$ is achieved compared to computational DoA based estimation technique, at the cost of additional (sensitive) radio hardware. The trade-off between bandwidth and detector diode circuit sensitivity highlights the impact of sensitivity on the DoA estimation accuracy. As a result of its low complexity, the proposed system will find application in mmWave channel estimation, localization, and radio source positioning.

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