The ability to tightly focus, i.e., over tens of microns, dense (> 10^{10} particles), short (with duration ~ps) bunches of positively charged particles is far beyond the possibility of present particle accelerators. The increase of the particle density of these beams would significantly improve the efficiency and prospects of a number of important applications. High-energy density proton beams would allow, for example, igniting preassembled inertial confinement fusion (ICF) targets, also known as proton fast ignition (PFI) [1], or enable ultrafast heating, above keV, of dense materials to explore their properties [2]. High-energy density positron beams would allow enhancing the rate of antimatter creation in the laboratory [3], opening up investigations of many fundamental laws of nature.

These positively charged beams, broadband or monenergetic, can nowadays be produced with a high particle number and over a short duration using ultraintense, short pulse lasers interacting with solids targets [4,5]. Proton beams are electrostatically accelerated by MeV hot electrons. These electrons are generated at the laser-solid interaction surface. After crossing the target, they induce a Debye sheath on the target rear surface. The quasielectrostatic fields in the sheath then accelerate surface ions [6,7]. Acceleration of positrons, which are produced in the bulk through nuclear processes, when they exit the solid target have also been reported [5]. When using flat targets as sources, the ion beam is divergent, 0°–25° depending on proton energy [8–10], since the expanding sheath field front on the target rear side is Gaussian in shape [11,12]. Such divergence can, however, be compensated by curving the back surface of the target, so that the accelerated proton beam will converge [4,13–15]. This points to the necessity of understanding and optimizing the dynamics of the focusing sheath in order to achieve tight focusing, as necessary for the above-mentioned applications.

In this Letter, we study the ion beam focusing dynamics through temporally and spatially resolved measurements, with picosecond and micrometer resolution, of the shape of the sheath field from a curved target, irradiated by a high-intensity short pulse laser. These are coupled to numerical simulations performed using the 2D particle-in-cell (PIC) codes CALDER [16] and PICLS [17], and a particle transport code, CMC [18]. The main results are as follows: (i) a convergence of the ion beam accelerated from the inner surface of a 800 μm diameter cylinder is observed to ~30 μm diameter, (ii) significant filamentation, however, occurs in the converging plasma, (iii) the location of the focus is a function of proton energy, although most of the protons focus at the geometric target center, and (iv) the exact location of laser illumination on the curved target does not adversely affect the ability to focus the sheath-accelerated ion beam, although it modifies the directionality of the ion beam.

The experiment was carried out using the 100 TW laser at the Laboratoire pour l’Utilisation des Lasers Intenses (LULI) operating in the chirped pulse amplification (CPA) mode. To diagnose the sheath field structure, we used the now established technique of transverse proton radiography, which can uniquely resolve, in space and time, quasi-static fields in dense plasmas [19]. Radiography using laser-driven proton beam is unique in that it is able to probe both electric and magnetic fields in dense plasmas with high temporal and spatial resolution, thanks to the low emittance of the beam and the short emission duration [20].
Studying the field structures in a 3D curved target, such as a hemisphere, is very difficult, if not impossible. Therefore, by using a simpler curved geometry, such as a half cylinder, we can study the fields in 2D. The experimental setup is shown in Fig. 1. The wavelength of the laser light was 1.057 μm and the pulse duration was τ = 320 fs, as measured after compression and before focusing. Two short pulse beams were used. The first short pulse beam (B1), with 1 J in energy, 11 μm spot diameter, and intensity of $2.5 \times 10^{18}$ W/cm² on target, was used to irradiate aluminum half cylinders, 670 μm long, having 50 μm thick walls and 800 μm diameter, producing protons with energy up to 1 MeV. The second independently compressed short pulse beam (B2), with 7 J in energy, 7 μm spot diameter, and intensity of $4.4 \times 10^{19}$ W/cm², irradiated a 10 μm thick gold foil to produce protons with energy up to 15 MeV, which were used for proton radiography. This technique inherently takes advantage of proton time-of-flight [21] such that the highest energy protons will probe the cylinder at the beginning of the interaction and the slower protons will probe later in time. Therefore, multi-frame snapshots of the fields’ evolution can be captured on a single shot.

The detector was a stack of radiochromic film (RCF) where the deflected protons will deposit most of their energy at a depth within the stack according to their Bragg curve. The stack was composed of four pieces of Gafchromic HD-810 film followed by MD-55 films with a 13 μm Al foil filter at the very front to block unwanted radiation. The distance from the Au foil to the B1 irradiation point on the cylinder is 3 mm and from the cylinder to the RCF is 25 mm. On some shots, a copper mesh was placed 2 mm from the Au foil, i.e., before the half-cylinder target, to imprint a grid pattern onto the proton probe beam to explicitly show the magnitude and direction of the fields [20].

Side-on experimental radiographs of the inner surface of the half-cylinder target are shown in Figs. 2(a)–2(d) and all times are normalized to $t_{\text{arrival}}$ at which the highest energy protons arrive at the focus point. The dark regions, indicative of proton pileup, outline the expanding sheath field created by the hot electrons [11]. The first radiograph of the series is taken at 2 ps after irradiation of the cylinder, a time at which the cloud of hot electrons produced during the laser interaction has already surrounded the entire half cylinder uniformly (not shown). In Fig. 2(a), at $t = 4$ ps, we can see that in addition to this general sheath front, at the center of the half cylinder, there is another spherically shaped front which is expanding faster. As observed in previous experiments, this front is produced by the ~MeV hot electrons that accelerate the highest energy ions [7,11], with the lower energy protons being accelerated behind the front by lower amplitude fields [4,6]. At $t = 11$ ps, the spherical expansion front disappears and short filaments appear inside the expanding plasma, which is consistent with what has been simulated by PIC codes [22]. This can be attributed to either electromagnetic or electrothermal instabilities [23]. As time progresses, the filaments grow and elongate. We have previously observed [8] that such a filamented sheath will give rise to a filamented proton beam. Therefore, this will impair the homogeneity of the final produced beam. However, in our observations, we can also use these filaments as a fiducial which indicates the
direction of plasma flow since the filaments are produced in the direction of the hot electron flow. Thus, despite the filamentation, we can witness that the plasma begins to converge after 10 ps.

At $t = 27$ ps, the filaments reach a crossing point which defines $t_{\text{arrival}}$. The convergence is clearest at $t/t_{\text{arrival}} = 1.77$ and the image is shown in Fig. 2(c). It should be noted that in the radiographs at $t/t_{\text{arrival}} = 1.77$, Figs. 2(c) and 2(d), there appear to be two sets of filaments: a shorter set close to the cylinder wall and a longer set within the expansion region. The shorter set is likely due to filamentation in the general sheath field, which extends over the entire target, but remains close to the target surface. The longer set is only produced close to the laser interaction area and is associated with the progressing proton cloud and its localized focusing. Since the radiographs integrate over the 670 μm length of the target, both sets are captured on the radiograph. Note that filamentation could not be observed in the first experiment reporting proton focusing [13], due to limited spatial resolution and because the focusing was observed indirectly by measuring the heating of a secondary target placed at the ion beam focus. The focus of the central filaments and of the overall beam envelope is 370 μm away from the inner surface of the cylinder, which is consistent with the radius of curvature of the cylinder, and has a spot size of ~30 μm diameter. This gives a $D/r = 0.93$ with $D$ being the location of focus relative to the target back surface and $r$ the radius of curvature of the target. In projecting the shorter filaments, corresponding to lower energy protons accelerated far from the laser irradiation location, they too come to a cross point, but this time at 400 μm from the back surface and the projections make a much larger spot size of 100 μm, which is consistent with previous data showing that lower energy protons have a larger divergence [9,10]. We can estimate the proton current density at focus. For this, we take our laser parameters, a spread of proton energies from 500 keV to 1 MeV, a proton conversion efficiency of 1% of the laser energy [24], and a spot area of $9 \times 10^{-6}$ cm$^2$. The difference in time of arrival at focus is 11 ps which gives a current density of $1 \times 10^8$ A cm$^{-2}$.

The radiographs of the half cylinders shown in Figs. 2(c) and 2(d) are for early times. The radiographs in Figs. 2(e) and 2(f) are shown using curved targets, made from a large foil moulded onto a rod. They show the sheath field structure later in time. Both the filaments and caustic features also come to a crossing point near the radius of curvature and then diverge after the focus point as is predicted in the simulation shown in Fig. 3(c) (detailed below). Note that the structures appearing in Figs. 2(e) and 2(f) are not necessarily in a one-to-one correspondence to the filaments within the converging ion beam since they represent modulations induced on the probing proton beam passing through the plasma and projected far away on the film. Nevertheless, the fact that such structures appear in the probing proton beam implies that the converging proton beam is indeed inhomogeneous.

We used CALDER and CMC codes to simulate, in 2D geometry, laser-cylinder interaction, proton acceleration, and focusing. Here, the CALDER code is used to calculate the laser-target interaction, electromagnetic fields, and

![FIG. 3](color online). CMC simulation results showing proton position in the interior of the half-cylinder target at (a) $t/t_{\text{arrival}} = 0.47$, (b) $t/t_{\text{arrival}} = 1$, (c) $t/t_{\text{arrival}} = 2$. All times are normalized to $t_{\text{arrival}} = 5.7$ ps.

![FIG. 4](Simulation results from CALDER and CMC. (a),(b) Proton beam waist and focusing location as a function of proton energy when laser intensity is $10^{18}$ W cm$^{-2}$. (c),(d) Same, but using laser intensity of $8 \times 10^{18}$ W cm$^{-2}$.)
particle positions up to 1.2 ps after the interaction; then information on protons velocity and direction is used in CMC to trace particle trajectories for longer times than what can reasonably be done in standard PIC codes, until and after the ion beam reaches its focus.

In the simulation, the half cylinder has a radius of curvature of 80 µm (5 times smaller than the experimental target) and the laser intensity is $10^{18}$ W/cm$^2$, accelerating protons to a maximum energy of several MeVs, as we see experimentally. The convergence time is $t_{\text{arrival}} = 5.7$ ps, i.e., 5 times smaller than the experimental $t_{\text{arrival}}$, which is consistent with the experimental results of a reduced scale target. The evolution of the proton beam in the simulation is consistent with the measured data, such that early in time, the protons, accelerated off the back surface of the target, also exhibit a convex shape in the central region [see Fig. 2(b)] and later on transformed into a focused beam [see Fig. 3(a) compared to 3(b)]. Once protons travel beyond the focus point, they tend to diverge again as shown in Fig. 3(c). Furthermore, we found that the focus is chromatic such that the higher energy protons focus farther than the lower energy protons. Hence, the location of the proton focus changes in time and extends over 110 µm as shown in Fig. 4(b). The highest energy protons originate only near the laser interaction region and converge at a distance 110 µm farther than the geometrical focus, giving a ratio $D/r = 2.4$, which is consistent with previous findings [25]. However, the bulk of the protons are lower in energy ($\sim$ 1 MeV) and they originate from the entire surface of the sheath and converge at its geometrical center, giving a ratio $D/r = 1$, which is consistent with the behavior of the short filaments in the experimental images.

Finally, we performed simulations with higher laser intensity in order to produce protons which have higher energy than in the experiments discussed in this Letter, but closer to fast ignition requirements [1]. The proton beam characteristics for laser intensity of $8 \times 10^{18}$ W/cm$^2$ are shown in Figs. 4(c) and 4(d). The higher intensity increased the proton spectrum up to 25 MeV, reduced the beam waist at the focus location for lower energy protons, and reduced the spread of distances that the protons focus to as a function of energy, as is beneficial for fast ignition. It also suggests that with even higher laser intensities, focusing of the proton beam will improve even more.

Beyond determining the dynamics of the focusing, we also tested the effect of unbalanced irradiation onto the half-cylinder target. Indeed, in future large-scale ICF facilities (HiPER [26], NIF-ARC [27]), short pulse beams will use several “beamlets” to construct the overall laser beam that will impinge onto the target. In view of PFI applications, where these beamlets will irradiate a hemispherical shell to produce the igniting proton beam [28], there is a clear interest in testing how ion beam focusability can be affected by an unbalanced distribution of intensity on the shell.

Here we tested this by taking one shot where the short pulse laser $B_1$ was aimed slightly beneath the axis of the half cylinder. In Figs. 5(a) and 5(b), proton radiographs at two different times for the same shot are shown. It is obvious that off-axis irradiation prevents formation of a uniform sheath field, with a larger field observed at the edge of the cylinder closest to where the laser impacted.

We simulated this scenario using a half cylinder with a radius of 42 µm (10 times smaller than the experimental target) and thickness of 5 µm using the code PICLS. The simulation box was $92 \times 92$ µm$^2$, the laser intensity of $3 \times 10^{18}$ W/cm$^2$ with a pulse duration of 175 fs and FWHM of 6 µm. Figures 5(c) and 5(d) show the spatial position of the hot electrons with energy of 100 to 500 keV at different times (normalized to $t_{\text{arrival}} = 1.5$ ps). As expected, the edge closest to where the laser hit the target has a higher concentration of hot electrons than the ends of the target. This asymmetry is maintained even later in time as the sheath expands into vacuum due to the fact that electrons take more time to transit to the far distant edge.

![FIG. 5](image-url)

FIG. 5 (color online). The $B_1$ short pulse laser was aimed off-center on the half cylinder. Deflectograms of the sheath field at $t/t_{\text{arrival}} = 0.08$ (a) and 0.27 (b). PICLS simulation results plotting hot electron positions are shown in (c) and (d). Simulated proton positions are shown in (e) and (f) that also show the location of the focus.
and to come back to their initial location than they do relative to the closer edge. The influence of such transverse electron refluxing dynamics [29] leads to an uneven development of the sheath field. However, when looking at the accelerated protons as shown in Figs. 5(e) and 5(f), this is not detrimental to proton beam focusing, but only changes the directionality of the focused beam itself. It is clear from the contours in the proton beam that they do still converge to a point. In more general terms, balancing of the laser beamlets that would compose the single laser beam on target used for PFI would thus not be important in terms of the ability to focus the ion beam.

In conclusion, we diagnosed converging filaments in the sheath field at the back of a curved, laser-irradiated solid foil. The coupling of experimental data and simulation suggests that protons with intermediate energies, which carry most of the beam energy, consistently focus close to the center of the cylinder, even for off-axis laser impact on the half cylinder. Filamentation in the plasma, however, implies that the proton beam transverse size at focus will be enlarged since filamentation is a manifestation of an emittance degraded beam [30]. All this, resulting here in the observed beam size of 30 μm, is detrimental to the proton fast ignition scheme which would require 10–20 μm beam to minimize the required igniter energy [1]. However, simulations shown in Figs. 4(c) and 4(d) suggest that focusing could improve for conditions closer to fast ignition than tested here. The next step will be to test this in future experiments.

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