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Towards a More Generalized Doherty Power Amplifier Design for Broadband Operation

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Abstract—The conventional Doherty power amplifier (DPA) theory is limited to single carrier operations, leading to a nongeneric structure. This paper presents a new analysis that generalizes the conventional DPA theory for increased efficiency and bandwidth. We demonstrate that by introducing a theoretical parameter \( \alpha \) at the output combiner we can redefine the relationships among the output combiner elements for a greater level of design flexibility than it was possible in the conventional DPA. We also show that previously published works in this area can be considered as special cases of the proposed general theory. As a demonstrator, a specific design, named Reduced-\( \alpha \) Doherty power amplifier, realized using GaN HEMTs is provided to illustrate the robustness of the approach. This design proves effective for further improving the performance of the previously published 2.14/2.655 GHz dual-band parallel DPA. A maximum drain efficiency of 84\% and 67\% at an average of 43-dBm peak and 6-dB back-off power levels, respectively, were measured with continuous wave signals. To quantify the linearity performance, the proposed DPA was tested using wideband CDMA and long-term evolution (LTE) signals where the adjacent channel leakage ratio was recorded at –25 dBc with an average output power of 38.7 and 36.5 dBm at 2.14 and 2.655 GHz, respectively.

Index Terms—Broadband, combiner, Doherty, efficiency, GaN, HEMT, load modulation, power amplifier, transmission line.

I. INTRODUCTION

The evolution of modern wireless communication standards from global system for mobile communications (GSM) through third-generation (3G) wideband CDMA to fourth-generation (4G) long-term evolution advanced (LTE-A) requires highly efficient RF power amplifiers (PAs) that can handle multiple frequency bands simultaneously. One of the promising candidates for this is the Doherty power amplifier (DPA) [1]–[2], which is widely favored due to its simple structure and mature implementation at GHz-frequencies.

While the conventional DPA (CDPA) [3] is effective for single frequency-band operations, it exhibits power and efficiency degradations when the operating frequency deviates from the center frequency of the output combiner. These degradations are caused by the effect of the frequency-selective quarter-wave lines (TL\(_1\) and the output impedance transforming network (ITN) shown in Fig. 1(a)) at peak and back-off power (BOP) levels [4]–[5]. Therefore, extensive amount of research has been dedicated towards enabling the DPA for multiband operation. To achieve this goal, some publications have focused on enhancing the frequency response of the individual passive network elements using either \( \pi \)-networks, T-networks, single- or two-stepped ITNs [6]–[21] or microelectromechanical switches [22]–[23]. For instance, the DPA proposed in [24] has used an output matching network at the Main PA to compensate the effect of TL\(_1\) and the output ITN. Unfortunately, such techniques result in increased complexity, larger overall physical size, and increased mismatch losses.

Other publications have recently focused on developing the output combiner of the DPA. In [4] and [25] the bandwidth of the conventional DPA is enhanced at 6-dB BOP level by reducing the transformation ratio (TR) of TL\(_1\). However, the bandwidth was limited by the output ITN, whereas the load modulation seen by the Auxiliary PA’s input impedance \( Z_A \) was not carried out properly. These drawbacks have been addressed in the 2.14/2.655 GHz dual-band parallel DPA (PDPA) [26] wherein the output ITN was omitted, and two quarter-wave lines, TL\(_2\) and TL\(_3\) in Fig. 1(b), were imposed to achieve proper load modulation seen by the Auxiliary PA. Consequently, the bandwidths of the output combiner at low and 6-dB BOP were improved by reducing the TR of TL\(_1\) by a factor of two compared to that of the conventional DPA. However, two extra 35-\( \Omega \) quarter-wave transmission lines, one at the Main path and one at the Auxiliary path, were required to match the 50-\( \Omega \) resistance seen at the combiner’s input (\( Z_{\text{in}} \) and \( Z_A \) in Fig. 1) at peak power (PP) to the nominal Class-E load resistance, \( R_{\text{opt}} \), e.g. 25 \( \Omega \) in [26]. Furthermore, the theoretical analysis presented in [26] cannot be directly used in the practical implementation as some tuning of the output combiner transmission line (TL) parameters are necessary, without which the high efficiency, as predicted in the theory, will not be obtained.

The same output combiner structure was adopted in [27] and [28] but with no theoretical analysis adequately provided. In
an approach to find the exact values of this combiner parameters was presented, however, the approach provided sophisticated formulae that permitted negative characteristic impedances for TL2 and TL3. Moreover, other techniques have been proposed to design wideband DPAs such as digital DPA [5], three-way sequential DPA [30], and DPA with an output combiner comprised of a branch-line coupler [31].

In this paper, we propose a new analysis to provide generalized DPA theory of operation with respect to the combiner parameters. This analysis introduces, through parameter \(\alpha\) (positive real number), simple formulae to define the relationships between the combiner parameters for a load modulation process over wide bandwidth. The new formulae provide an additional degree of design freedom through which the output ITN is no longer required. This ITN, first proposed by McMorrow [3], is typically required in the conventional DPA to transform the standard load \((R_L = 50 \, \Omega)\) into the combined load \(R'_L = R_{opt}/2\) [4], [7]–[23], [32]–[37]. However, it occupies both Main and Auxiliary paths, leading to a reduced bandwidth and larger circuit size.

Based on this approach, a new DPA variant, named Reduced-\(\alpha\) Doherty power amplifier (RDPA), is proposed to improve the performance of the parallel DPA and demonstrate the effectiveness of the analysis. In this design, when \(\alpha\) is calculated, it directly reduces the structure complexity by obviating the need for the output ITN, and also by eliminating the parallel DPA’s extra 35-\(\Omega\) quarter-wave lines, as a result of matching \(Z_M\) and \(Z_A\) directly to \(R_{opt}\) at PP. The new design outperforms both conventional and parallel DPAs in terms of bandwidth capability at low and 6-dB BOP levels (i.e. where the Auxiliary PA is switched off). An infinite fractional bandwidth (FBW) can theoretically be achieved as a result of reducing the TR of TL1 at 6-dB BOP by a factor of four compared to the conventional DPA.

The technical work included in this paper was partially reported in [38], whereas a complete analysis and measurements are given in this paper. This paper is organized as follows. Section II presents the derivation of the new analysis along with the resulting design formulae and operational conditions. Section III explains the design procedures of the proposed Reduced-\(\alpha\) DPA combiner, followed by a comparison of its simulated performance with that of the parallel DPA in Section IV. Section V describes implementation and measurement of the Reduced-\(\alpha\) DPA with continuous wave (CW) signals. In Section VI, the linearity performance of the realized DPA is examined through modulated signal measurements. Finally, the conclusions of this paper are given in Section VII.

II. BASIC OPERATION AND ANALYSIS OF THE GENERALIZED DOHERTY POWER AMPLIFIER

The basic structures of the conventional and generalized DPAs are illustrated in Fig. 1. In the conventional DPA, an output ITN is required to transform \(R_{opt}/2\) to the standard 50-\(\Omega\) load impedance whereas in the generalized DPA two transmission lines TL2 and TL3 are inserted at the Auxiliary PA output. The three lines TL1, TL2 and TL3 are quarter-wave lines at the center angular frequency \((\omega_0)\). Therefore, to ensure the phase of the signal in the Main PA path match the phase of the signal in the Auxiliary PA path prior to them being combined, a 90° delay transmission line, not shown in Fig. 1, needs to be added at the input of the Auxiliary PA (for the case of the conventional DPA) or at the input of the Main PA (for the case of the generalized DPA). The analysis of the generalized DPA presented below is based upon assumptions that both Main and Auxiliary PAs are operated in Class-B mode, and that their output currents and voltages follow the ideal characteristics shown in Fig. 2.

Phasors of the fundamental output currents of the Main and Auxiliary PAs, denoted here respectively as \(I_M\) and \(I_A\), can be described as follows [2]:

\[
I_M = \frac{I_{max}}{4} (1 + \xi) e^{j(\omega t + \phi_M)},
\]

\[
I_A = \frac{I_{max}}{2} \xi e^{j(\omega t + \phi_A)} = \frac{I_{max}}{2} \xi e^{j(\omega t + \phi_M + \pi/2)},
\]

where parameter \(\xi\) varies from 0 to 1 as the input drive voltage \((V_{in})\) increases from \(V_{max}/2\) to \(V_{max}\). \(I_{max}\) is the maximum amplitude of the output RF current, \(\phi_M\) and \(\phi_A\) are the phase shift angles of \(I_M\) and \(I_A\) respectively. Let us consider now Fig. 1(b), the impedances seen by TL1, i.e. \(Z_{M1}\) and by TL2, i.e. \(Z_{A1}\) are:
From (11) and (12) we can express \( I_{A1} \) as follows:

\[
I_{A1} = \frac{-Z_3 I_A}{Z_2^2}.
\]  

(13)

By substituting (8) and (13) into (3), \( Z_M \) can be obtained from the quarter-wave impedance transformation formula as follows:

\[
Z_M = \frac{Z_2^2}{Z_{M1}} = \frac{Z_2^2}{R_L\left(1 - j \frac{Z_1 Z_3 I_d}{Z_2 V_M}\right)}.
\]  

(14)

Hence, the fundamental output voltage of the Main PA is

\[
\bar{V}_M = \frac{I_m Z_I}{R_L\left(1 - j \frac{Z_1 Z_3 I_d}{Z_2 V_M}\right)}.
\]  

(15)

Next we substitute \( I_M \) and \( I_A \) described in (1) and (2) into (15) to obtain the following relation:

\[
\bar{V}_M = \frac{I_m Z_1^2}{R_L\left(1 - j \frac{Z_1 Z_3 I_d}{Z_2 V_M}\right)} e^{j(\omega t + \theta + \pi/2)} \frac{V_M}{Z_2^2}.
\]  

(16)

After re-arranging (16), \( \bar{V}_M \) can be expressed as:

\[
\bar{V}_M = \frac{Z_1}{Z_2} \left(\frac{Z_2}{2R_L} \right) V_M e^{-j(\omega t + \theta + \pi/2)}.
\]  

(17)

From Fig. 2, it can be observed that the voltage amplitude \( V_M \) is constant (i.e. equal to \( V_{dc} \)) for input drive ranging from \( V_{max}/2 \) to \( V_{max} \). To accomplish this, \( \bar{V}_M \) in (17) must be set independent of \( \xi \), resulting in (18) and (19). For the convenience of subsequent analysis, a new parameter \( \alpha \) is introduced.

\[
\frac{Z_1}{Z_2} \alpha = \frac{Z_1}{Z_2} \frac{Z_2}{2R_L}.
\]

(18)

\[
V_M = \left(\frac{I_{max}}{2}\right) \left(\frac{Z_2}{2R_L}\right) = V_{dc}
\]

(19)

To achieve maximum output voltage swing of \( V_{dc} \) in Class-B mode, the fundamental impedance seen by the PA must be equal to

\[
R_{opt} = V_{dc} \left(\frac{2}{I_{max}}\right).
\]

(20)

Given (20) and from the inspection of Fig. 2, we can calculate \( Z_M \) at 6-dB BOP level, i.e., at \( v_{in} = V_{max}/2 \) and at PP level, i.e., at \( v_{in} = V_{max} \) as given below:

\[
Z_{M_{BOP}} = \frac{V_M}{I_M} = \frac{V_{dc}}{I_{max}} = 2R_{opt}.
\]  

(21)

\[
Z_{M_{PP}} = \frac{V_M}{I_M} = \frac{V_{dc}}{I_{max}} = R_{opt}.
\]  

(22)

Further from (19) and (20), we obtain
\[
\frac{Z_1^2}{2R_L} = \frac{R_{\text{opt}}}{\alpha}. 
\]  
(23)

Subsequently, the characteristic impedance of TL₁ \((Z_1)\) and the load impedance \((R_L)\) can be calculated from (18) and (23) as follows:

\[
Z_1 = \frac{R_{\text{opt}}}{\alpha}, 
\]  
(24)

\[
R_L = \frac{R_{\text{opt}}}{2\alpha^2}. 
\]  
(25)

In the conventional DPA, an output ITN is typically needed to transform \(R'_L = R_{\text{opt}}/2\) into \(R_L = 50\ \Omega\). For single band operation, a single-stepped ITN is often sufficient whereas for broadband operation a more sophisticated two- or three-stepped ITN needs to be employed, resulting in increased circuit complexity and large physical size. In the generalized DPA, the degree of design freedom is increased by one through the introduction of parameter \(\alpha\), which might dispense with the need for the output ITN.

The impedance \(Z_0\) described in (21) – (22) is transformed by TL₁ into the following impedance:

\[
Z_{M1BOP} = \frac{Z_1^2}{Z_{M,BOP}} = \left(\frac{R_{\text{opt}}}{\alpha}\right)^2 = \frac{R_{\text{opt}}}{2\alpha^2} = R_U, 
\]  
(26)

\[
Z_{M1PP} = \frac{Z_1^2}{Z_{M,PP}} = \left(\frac{R_{\text{opt}}}{\alpha}\right)^2 = \frac{R_{\text{opt}}}{\alpha^2} = 2R_U. 
\]  
(27)

As can be seen from Fig. 1, the only bandwidth-limiting element in the Main PA branch is TL₁. Using (21), (22), (26), and (27) we can describe the FBW of TL₁ at PP and BOP as follows [39]:

\[
\text{FBW}_{\text{TL1}} = 2 - \frac{4}{\pi} \cos^{-1}\left(\frac{\Gamma_m}{\sqrt{1-\Gamma_m^2}}\gamma(\alpha)\right), 
\]  
(28)

where \(\Gamma_m\) is the maximum reflection coefficient magnitude can be tolerated at the combiner input within the bandwidth of interest (assuming \(\Gamma(\omega_0) = 0\) at both PP and 6-dB BOP), and \(\gamma(\alpha)\) is a parameter that depends on \(\alpha\) and the power level which can be expressed as

\[
\gamma(\alpha) = \begin{cases} 
\frac{2\alpha}{|1-\alpha|^2} & \text{at peak power,} \\
\frac{4\alpha}{|1-4\alpha|^2} & \text{at 6 - dB BOP.}
\end{cases} 
\]  
(29)

For instance, if the minimum tolerable input return loss of TL₁ is assumed to be 10 dB then using (28) we can plot FBW_{\text{TL1}} as a function of \(\alpha\) as shown in Fig. 3. This figure implies the bandwidth capabilities of the generalized DPA at PP and 6-dB BOP levels. Clearly, for \(\alpha = 0.5\), termed here as Reduced-\(\alpha\) DPA, FBW_{\text{TL1}} is infinity at BOP which means the combiner response is independent of frequency, and \(Z_{M,BOP} = 2R_{\text{opt}}\) over the entire spectrum. Notice that this feature of the Reduced-\(\alpha\) DPA combiner would not change even if the threshold \(\Gamma_m\) is reduced to zero. The figure also shows the bandwidth capabilities at \(\alpha = 1\), which corresponds to the conventional DPA [1], and at \(\alpha = 1/\sqrt{2}\), which corresponds to the ideal case of the parallel DPA (i.e., without the extra 35-\(\Omega\) lines).

B. Auxiliary PA branch

At 6-dB BOP level, the Main PA is ON while the Auxiliary PA is OFF. Since the output current of the Auxiliary PA is zero, the impedance \(Z_A\) is infinity, (30). Subsequently, TL₂ and TL₃ will transform this impedance into an open circuit at the center frequency, and provide good isolation over a wide bandwidth.

\[
Z_{A,BOP} = Z_{A,\text{BOP}} = \infty. 
\]  
(30)

At PP level, both Main and Auxiliary PAs are ON. From the inspection of Fig. 2, we can calculate

\[
Z_{\text{App}} = \frac{V_A}{I_A} = \frac{V_{dc}}{I_{\text{max}}} = R_{\text{opt}}, 
\]  
(31)

where \(R_{\text{opt}}\) is defined in (20). Further, the impedance \(Z_{A1}\) can be determined as follows:

\[
Z_{A1,\text{PP}} = \frac{Z_{2}}{Z_{A2,\text{PP}}} = \frac{Z_{2}}{Z_{3}} = \frac{R_{\text{opt}} (Z_{2}^2)}{\alpha^2} = 2R_U. 
\]  
(32)

The foregoing analysis assumes that the electrical lengths of TL₂ and TL₃ (i.e., \(\theta_2\) and \(\theta_3\)) are fixed, i.e., 90°, and the corresponding basic circuit schematic is depicted in Fig. 4 with component values given in terms of \(\alpha\) and \(R_{\text{opt}}\) based upon the calculations in (21) – (22), (26) – (27), and (30) – (32). In the following analysis, the frequency behavior of the proposed generalized DPA is examined, i.e., this is the case when the carrier frequency \(f_c\) is varied apart from the center frequency \(f_0\). Since the physical lengths of TL₂ and TL₃ are constant, then \(\theta_2\) and \(\theta_3\) will also vary as follows:

\[
\theta_2 = \theta_3 = \theta = \frac{\pi f_c}{2 f_0} = \frac{\pi}{\alpha} k. 
\]  
(33)
where $k$ is the normalized frequency. The values of $Z_{A2}$ and $Z_A$ at PP level can be computed using lossless transmission line formula as follows:

$$Z_{A2PP} = Z_A^2 \frac{Z_{A1PP} + jZ_2 \tan \theta}{Z_2 + jZ_{A1PP} \tan \theta},$$  

$$Z_{App} = Z_A \frac{Z_{A2PP} + jZ_2 \tan \theta}{Z_2 + jZ_{A2PP} \tan \theta},$$

(34)

(35)

where $Z_{A1PP}$ is given in (32) and the relationship between $Z_2$ and $Z_3$ is described in (18). Substituting (34) into (35) yields:

$$Z_{App} = \frac{Z_2^2 (1 - a \tan^2 \theta) + jZ_2(1 + a) \tan \theta}{Z_2^2 (a - \tan^2 \theta) + j2R_1(1 + a) \tan \theta},$$

(36)

The magnitude of $Z_{App}$ and its normalized magnitude are expressed as follows:

$$|Z_{App}| = aZ_2 \frac{\sqrt{4R_1^2(1 - \tan^2 \theta)^2 + 4Z_2^2(1 + a)^2 \tan^2 \theta}}{Z_2^2 (a - \tan^2 \theta)^2 + 4R_1^2(1 + a)^2 \tan^2 \theta},$$

$$\frac{|Z_{App}|}{R_{opt}} = \sqrt{\frac{2R_1}{Z_2^2} \left(1 - \tan^2 \frac{Z_2}{2Z_2} \right)^2 + (1 + a)^2 \tan^2 \frac{Z_2}{2Z_2}},$$

(37)

(38)

where $R_{opt}$ is given in (25). Notice from (36) that for $\theta = 90^\circ$, $Z_{App}$ will no longer depend on $Z_2$. Illustrated in Fig. 5 is the frequency response of $Z_{App}$ for different values of $Z_2$ where $a$ and $R_L$ are fixed, i.e., $a = 0.5$ and $R_L = 50$ $\Omega$. Here $Z_2$ controls the bandwidth of the Auxiliary branch.

### C. Power and efficiency of the generalized DPA versus bandwidth

The generalized DPA output power at 6-dB BOP level can be derived as follows:

$$P_{outpp} = \frac{1}{2}I_d M \cos \varphi_{MPP} + \frac{1}{2}I_d V_d \cos \varphi_{App}$$

$$= \frac{1}{2} P_{out_{max}} (\cos \varphi_{MPP} + \cos \varphi_{App}),$$

(43)

where

$$\cos \varphi_{MPP} = \frac{\text{real} \left(Z_{MPP}(\theta) \right)}{|Z_{MPP}(\theta)|},$$

$$\cos \varphi_{App} = \frac{\text{real} \left(Z_{App}(\theta) \right)}{|Z_{App}(\theta)|},$$

(44)

(45)
and $Z_{Mpp}(\theta)$ is obtained by substituting (24) and (27) in the lossless transmission line equation of $TL_1$ at PP resulting in

$$Z_{Mpp}(\theta) = \frac{R_{opt}}{\alpha} \frac{1 + j \alpha \tan \theta}{\alpha + j \tan \theta}$$

(46)

By substituting (25), and $Z_2 = \frac{R_{opt}}{\alpha^{3/2}}$ in (36), $Z_{App}$ can be described as

$$Z_{App}(\theta) = \frac{R_{opt}}{\sqrt{\alpha}} \left[ \frac{1 - \alpha \tan^2 \theta}{\sqrt{\alpha}} + j(1 + \alpha) \tan \theta \right]$$

(47)

For a maximum dc power equals to $2(I_{max}/\pi)V_{dc}$, the DE at PP can be written as

$$\eta_{pp} = \frac{\pi}{4} \frac{1}{2} (\cos \varphi_{Mpp} + \cos \varphi_{App})$$

(48)

Note that $Z_2$ in (36) can be selected arbitrarily, but here we have chosen its optimum definition, i.e., (49), over 25% FBW as will be demonstrated in Section III.

The output power and efficiency of the generalized DPA are plotted against $k$ for different values of $\alpha$ as depicted in Figs. 6 and 7. From these figures we observe that the generalized DPA provides an ideal Performance at $f_c$ regardless of the value of $\alpha$. As $f_c$ deviates from $f_0$ the parameter $\alpha$ takes control of the power and efficiency degradations. The effect of $\alpha$ here confirms the results observed in Fig. 3 where best performance at BOP and PP corresponds to $\alpha = 0.5$ and $\alpha = 1$, respectively. For instance, with $\alpha = 0.5$ the back-off efficiency is 1.25 times higher than that of the conventional DPA [1] at $k = 0.5$.

To conclude, the Reduced-$\alpha$ DPA is analytically able to eliminate any bandwidth limitations caused by the combiner at low and 6-dB BOP operation. Whereas its relatively moderate performance at PP might be enhanced, for example, by means of enabling the Auxiliary PA to provide higher power and efficiency at PP through unsymmetrical DPA designs [4]. Note that the conventional DPA [3] has proven power and efficiency degradations with respect to the FBW not only at BOP but also at PP, as reported in [4], due to the imposed output ITN.

III. REDUCED-$\alpha$ DPA DESIGN PROCEDURE

An example with step-by-step design procedures is given below to elucidate the basic operation and theory of the proposed generalized DPA described in Section II. The generalized DPA is designed to operate within 2.1–2.7 GHz frequency range, i.e., 25% FBW. The broadband Class-E PA [40]–[42] employing reactance compensation technique with a nominal resistance ($R_{opt}$) of 25 $\Omega$ reported in [26] is used as Main and Auxiliary PAs. The generalized DPA is terminated with standard 50 $\Omega$ load resistance ($R_L$).

Step 1: Calculate $\alpha$ using (25)

$$\alpha = \sqrt{\frac{R_{opt}}{2R_L}} = \sqrt{25/100} = 0.5$$

This step avoids imposing either an output ITN or any extra quarter-wave lines. Furthermore, this value of $\alpha$ flattens the frequency response of the combiner, over the entire spectrum, at 6-dB BOP level and below. Note that if $R_{opt}$ was not predetermined, then (25) would be used to calculate $R_{opt}$ required for the PA cell based on the desired value of $\alpha$.

Step 2: Calculate $Z_1$ using (24)

$$Z_1 = \frac{R_{opt}}{\alpha} = 50 \Omega$$

Step 3: Determine $Z_2$ and $Z_3$

Given $R_L$ and $\alpha$, the optimum value of $Z_2$ can be obtained graphically as follows:

(i) Using (36) and (38) respectively, plot the phase and the normalized amplitude of $Z_{App}$ for different values of $Z_2$.

(ii) From these two plots, determine $Z_2$ that gives minimal amplitude and phase variation over the required FBW.

From Fig. 5, the optimum $Z_2$ is 70 $\Omega$ since this value gives minimal phase variation $<0.9^\circ$ and minimal amplitude variation $<5.4\%$ across 25% FBW. Alternatively, by assuming $Z_{App} = R_{opt}/\alpha$, the optimum $Z_2$ can be calculated from (49) which gives a more accurate result than the one obtained from the graphical representation, which relies on the resolution of the sweeping intervals (10 $\Omega$).
\[ Z_2 = \frac{R_{\text{opt}}}{\alpha^{3/2}} = 70.71 \, \Omega \] (49)

Subsequently, the value of \( Z_3 \) can be calculated using (18) as follows:
\[
Z_3 = \alpha \, Z_2 = \frac{R_{\text{opt}}}{\alpha^{1/2}} = 35.36 \, \Omega.
\]

As can be seen from Fig. 8, \( Z_4 \) has now been optimally matched to the PA cell nominal resistance \( (R_{\text{opt}} = 25 \, \Omega) \) at PP level over the required bandwidth, and compared with the parallel DPA, the proposed Reduced-\( \alpha \) DPA offers better matching within 25% FBW. The final circuit schematic of the proposed Reduced-\( \alpha \) DPA is illustrated in Fig. 9. Table I shows a comparison between different DPA topologies, from which it can be seen that for \( \alpha = 1/\sqrt{2} \) the generalized DPA is reduced to the parallel DPA and for \( \alpha = 1 \) the generalized DPA is reduced to the conventional DPA, implying that parallel DPA and conventional DPA are essentially a subset of the generalized DPA. In addition, it is observed that the DPA designs reported in [27], [29] and [28] have \( \alpha = 0.6, 0.6 \) and 0.4, respectively. Hence, the method presented in this paper helps classifying various DPA topologies.

The frequency response of the impedances \( Z_{\text{MBOP}}, Z_{\text{MPP}}, \) and \( Z_{\text{APP}} \) is examined for the conventional, parallel, and Reduced-\( \alpha \) DPAs. For the conventional DPA, a two-stepped output ITN is inserted to provide a dual-band behavior. At 6-dBm BOP the Reduced-\( \alpha \) DPA outperforms the other DPAs and achieves an ideal behavior over the entire indicated frequency range as shown in Figs. 10(a) and (b). At PP level, the impedance \( Z_{\text{APP}} \) has almost the same behavior for the conventional and Reduced-\( \alpha \) DPAs as depicted in Fig. 10(c) and (d). Meanwhile, at the Main side, \( Z_{\text{MPP}} \) for the conventional DPA has the best response for up to 40% FBW, while all topologies exhibit poor response at higher FBW as shown in Figs. 10(e) and (f).

### IV. Circuit Simulation

The circuit schematic of the Reduced-\( \alpha \) DPA used in the simulations is depicted in Fig. 11. The substrate used was Rogers RO4350B model with 0.508-mm thickness, a dielectric constant of 3.66, and a loss tangent of 0.0037. Two 10-W GaN HEMTs CGH40010F from Cree were used to deliver a total PP of 43 dBm. A 90° hybrid coupler 11306-3S from Amaren was used to split the input power equally and provide 90° phase shift at the input of the Main PA. The Class-E circuit reported in [26] was used as the Main and Auxiliary PAs. The structure of the output combiner is based on Fig. 9 with \( \alpha = 0.5 \). The electrical lengths of the 25-\( \Omega \) offset lines were optimized for better isolation and efficiency. Table II shows theoretical and actual values of the output combiner parameters. No tuning was performed in the Reduced-\( \alpha \) DPA simulation as opposed to the parallel DPA, leading to a consistency between theory and realization. The gate bias voltages of the Main and Auxiliary PAs were set to \( V_{\text{GM}} = -3.15 \, \text{V} \) and \( V_{\text{GA}} = -7 \, \text{V} \), respectively, and the drain voltage of both cells was kept at \( V_{\text{dc}} = 28 \, \text{V} \).

#### A. Small signal performance

Fig. 12 shows a comparison of the simulated \( |S_{11}| \) and \( |S_{21}| \) of the Reduced-\( \alpha \) DPA with the parallel DPA. Input return loss and small-signal gain were better than 11.5 dB and 10.5 dB, respectively, across a frequency range from 2.1 to 2.7 GHz (25% FBW).

#### B. Large signal performance

Fig. 13 shows the simulated output power and DE versus frequency at 36-dBm input power (corresponding to the PP

![Fig. 8. Theoretical magnitude (solid lines) and phase (dashed lines) of \( Z_{\text{APP}} \) for the parallel and proposed Reduced-\( \alpha \) DPA.](image)

![Fig. 9. Circuit schematic of the 2.1–2.7 GHz Reduced-\( \alpha \) DPA.](image)
level). A significant DE improvement, up to 9.1 points (from 67.2% to 76.3% at 2.65 GHz), is observed over a FBW of 25%, with a maximum value of 81.6% achieved at 2.18 GHz. The output power is maintained at around 43 dBm over the intended bandwidth.

Fig. 14 shows the simulated output power and DE versus frequency at 27.5-dBm input power (corresponding to the BOP level). Similarly, the DE has improved up to 14 points (from 51.5% to 65.5% at 2.4 GHz) over the 2.1–2.7 GHz frequency range where the output power was hovering around 37.5 dBm. The maximum DE observed was 66.4% at 2.28 GHz.

Figs. 15 and 16 show the simulated gain and DE versus output power at 2.14 GHz (center frequency of the lower band 2.11–2.17 GHz) and at 2.655 GHz (center frequency of the upper band 2.62–2.69 GHz), respectively, with input power swept from 0 to 36 dBm. For the lower band, the DE reached a maximum of 81.4% at 42.8 dBm and 54.4% at 6-dB output BOP level. For the upper band, the DE reached a maximum of 76.6% at 43.3 dBm and 62.1% at 6-dB output BOP. The fundamental drain currents of the Main and Auxiliary PAs at 2.14 and 2.655 GHz are shown in Figs. 17 and 18. A current ratio 1:1 is obtained at PP level, conforming to the theory in Section II.

V. IMPLEMENTATION AND CW MEASUREMENTS

The Reduced-α DPA was realized on Rogers RO4350B substrate which was used in the simulations. Fig. 19 shows the fabricated DPA prototype with a total size of 10 cm × 6.2 cm. CW measurements were carried out using Rohde & Schwarz SMW200A signal generator and FSUP spectrum analyzer. A driver amplifier RUP15020-11 from RFHIC was used to boost the input power fed to the DPA up to 36 dBm. A 30-dB attenuator was inserted at the output of the DPA to protect the spectrum analyzer. Three 32V/10A dc power supplies were used to supply the required gate and drain bias voltages for both the driver and the DPA.

Fig. 20 shows the measured S-parameters, obtained with gate bias voltages optimized to $V_{GM} = -2.7$ V and $V_{GD} = -4.75$ V while the drain voltage is maintained at 28 V. Input return loss was better than 8 dB from 2 to 2.9 GHz, and better than 10 dB at the lower and upper band frequencies. The small-signal gain in the lower frequency band was higher than that in the upper frequency band. This is consistent with the fact that the output return loss is better in the lower frequency band. Measured output power, gain and DE at PP level are plotted in Fig. 21 against frequency. A maximum DE of 83.7% is obtained at 2.34 GHz. The PA exhibits DE $\geq 65\%$ within 500-MHz frequency range from 2.1 to 2.6 GHz. The PA delivered 43 ± 2 dBm saturated output power within the required bandwidth. Shown in Fig. 22 is the PA performance at 6 dB BOP level. A maximum DE of 66.8% was recorded at 2.2 GHz. The DE was $\geq 50\%$ within 420-MHz bandwidth from 2.1 to 2.52 GHz.

Fig. 23 shows the measured gain and DE against output

![Fig. 10 Simulated Main and Auxiliary impedances against frequency for the output combiner of the conventional, parallel and Reduced-α DPAs: (a) Normalized magnitude of Main impedance at 6-dB BOP. (b) Phase of Main impedance at 6-dB BOP. (c) Normalized magnitude of Auxiliary impedance at PP. (d) Phase of Auxiliary impedance at PP. (e) Normalized magnitude of Main impedance at PP. (f) Phase of Main impedance at PP.](image-url)
power at the center frequencies of the lower and upper frequency bands. For the lower band, a maximum DE of 70% and 63% was achieved at PP and 6-dB BOP levels, respectively. For the upper band, the maximum DE was 63% at 40.5-dB output power. This performance could potentially be enhanced by improving the output matching and providing a better termination for the second harmonic. In Fig. 24, gain and DE were measured against output power at several frequencies across the bandwidth where we observe that lower frequencies (2.2–2.4 GHz) have better DE than the upper ones.

VI. MEASUREMENTS WITH MODULATED SIGNALS

A. Robust PA linearity testing platform

In order to properly evaluate performance of the Reduced-α DPA, we have created a flexible testing platform as shown in

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Fig. 11. Simulated circuit schematic of the proposed 2.1–2.7 GHz Reduced-α DPA.

Fig. 12. Simulated input reflection coefficient ($S_{11}$) and small-signal gain ($S_{21}$) with $V_{gM} = -3.15$ V, $V_{gA} = -7$ V and $V_{dc} = 28$ V.

Fig. 13. Simulated output power and DE at PP with $V_{gM} = -3.15$ V, $V_{gA} = -7$ V and $V_{dc} = 28$ V.

Fig. 14. Simulated output power and DE at BOP with $V_{gM} = -3.15$ V, $V_{gA} = -7$ V and $V_{dc} = 28$ V.
Fig. 15. Simulated gain and DE versus output power at 2.14 GHz with input power swept from 0 to 36 dBm with $V_{gm} = -3.15\, V$, $V_{gd} = -7\, V$ and $V_{dc} = 28\, V$.

Fig. 16. Simulated gain and DE versus output power at 2.655 GHz with input power swept from 0 to 36 dBm with $V_{gm} = -3.15\, V$, $V_{gd} = -7\, V$ and $V_{dc} = 28\, V$.

Fig. 17. Simulated Main and Auxiliary PAs drain currents (fundamental amplitudes) versus output power at 2.14 GHz with input power swept from 0 to 36 dBm with $V_{gm} = -3.15\, V$, $V_{gd} = -7\, V$ and $V_{dc} = 28\, V$.

Fig. 18. Simulated Main and Auxiliary PAs drain currents (fundamental amplitudes) versus output power at 2.655 GHz with input power swept from 0 to 36 dBm with $V_{gm} = -3.15\, V$, $V_{gd} = -7\, V$ and $V_{dc} = 28\, V$.

Fig. 19. Fabricated circuit prototype of the proposed Reduced-$\sigma$ DPA, measures 10 cm $\times$ 6.2 cm.

Fig. 20. Measured S-parameters with $V_{gm} = -2.7\, V$, $V_{gd} = -4.75\, V$ and $V_{dc} = 28\, V$.

especially LTE signals based on orthogonal frequency-division multiplexing (OFDM) technique, usually have a high peak-to-average power ratio (PAPR) value, which causes a lower efficiency of the PA in the back-off operation mode.

To remove the high peaks, we employed a crest factor reduction (CFR) function in the system, which has been largely accepted as one of the fundamental functions in 4G and fifth-generation (5G) wireless transceivers. Then, the processed modulated digital signals with 122.88 MSPS sampling rate were up-converted to the required RF frequencies to stimulate the DUT (the DPA), and are finally captured by the spectrum analyzer.
B. DPA performance stimulated by modulated signals

For the purpose of evaluating the proposed DPA regarding linearity in the broadband and multiband applications, we created three different testing scenarios, i.e., the Reduced-\( \alpha \) DPA was stimulated by three different types of modulated signals specified as shown in Table III. Specifically, scenario 1 depicts a traditional PA test using a single-carrier wideband CDMA (W-CDMA) signal (5-MHz bandwidth) as stimulation of the DPA. After the CFR function, the testing signal has a 6.5-dB PAPR value and is up-converted to Band 1, i.e., 2.14 GHz. Scenario 2 utilizes a 20-MHz LTE signal with a 7.5-dB PAPR value to excite the DPA at 2.655 GHz. Those two tests are used to illustrate the DPA performance regarding wideband signals applications. Furthermore, we provided another type of test to illustrate the DPA linearity performance regarding concurrent multiband wireless applications. For example, scenario 3 uses an intraband carrier aggregated signal [43] with an 8-dB PAPR value containing two LTE signals (10-MHz bandwidth each) and a 30-MHz gap in between (center RF frequency at 2.655 GHz).

Figs. 26 and 27 show the measured adjacent channel leakage ratios (ACLRs) and DE for scenario 1, where a maximum DE of 48% with ACLR\(_1\) = –25 dBc and ACLR\(_2\) = –44.5 dBc is obtained at average output power of 38.7 dBm. In the other
Fig. 26. Measured ACLRs against the average output power with single carrier 5-MHz W-CDMA signal at 2.14 GHz with 6.5-dB PAPR. ACLR₁ and ACLR₂ are at 5- and 10-MHz offsets from the carrier frequency, respectively.

Fig. 27. Measured DE against the average output power with single carrier 5-MHz W-CDMA signal at 2.14 GHz with 6.5-dB PAPR.

Fig. 28. Measured ACLRs against the average output power with single carrier 20-MHz LTE signal at 2.655 GHz with 7.5-dB PAPR. ACLR₁ and ACLR₂ are at 20- and 40-MHz offsets from the carrier frequency, respectively.

band (2.655 GHz) the DPA shows an ACLR₁ = −24.5 dBc and ACLR₂ = −48.1 dBc at an average output power of 36.5 dBm as depicted in Fig. 28. For the carrier aggregated signal scenario, ACLR₁ and ACLR₂ were found to be around −25.9 dBc and −48.6 dBc respectively as shown in Fig. 29.

Without any linearization approaches, the designed DPA delivered a reasonably good linearity performance over a wide bandwidth. In order to achieve a better linearity performance in the high efficiency saturated region, the linearization of the DPA will be required for wireless applications. Due to its simple architecture and satisfactory performance, digital predistortion (DPD) [37] has been largely accepted as one of the fundamental blocks of wireless RF transceivers. In particular, the accurate PA behavior models proposed in [45]–[46] and effective wideband DPD verification approaches [47]–[48] have been successfully utilized for DPA linearization. However, due to the length restrictions, the linearization of the DPA is beyond the scope of this paper.

In Table IV, the performance of the proposed DPA is summarized and compared with other wideband GaN HEMTs DPA.

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Frequency (GHz)</th>
<th>Peak power</th>
<th>6-dB BOP Max./Min.</th>
<th>Max. ACLR at BOP* (dBc)</th>
</tr>
</thead>
<tbody>
<tr>
<td>[29]</td>
<td>1.0-2.55</td>
<td>43</td>
<td>84/57</td>
<td>500</td>
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<tr>
<td>[25]</td>
<td>1.5-2.5</td>
<td>42</td>
<td>67/52</td>
<td>200</td>
</tr>
<tr>
<td>[24]</td>
<td>1.7-2.25</td>
<td>48.2-49.6</td>
<td>77/65</td>
<td>500</td>
</tr>
<tr>
<td>[32]</td>
<td>1.7-2.3</td>
<td>53</td>
<td>72/58</td>
<td>250</td>
</tr>
<tr>
<td>[31]</td>
<td>1.7-2.4</td>
<td>41</td>
<td>72/53</td>
<td>200</td>
</tr>
<tr>
<td>[4]</td>
<td>1.7-2.6</td>
<td>42.1–45.3</td>
<td>55/50</td>
<td>0</td>
</tr>
<tr>
<td>[30]</td>
<td>1.8-2.45</td>
<td>43</td>
<td>75/59</td>
<td>445</td>
</tr>
<tr>
<td>[5]</td>
<td>1.96-2.46</td>
<td>42.2-44.2</td>
<td>66/52</td>
<td>80</td>
</tr>
<tr>
<td>[33]</td>
<td>2.2-3.0</td>
<td>40.2-41.2</td>
<td>68/52</td>
<td>200</td>
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<td>3.0-3.6</td>
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<td>65/56</td>
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<td>This work</td>
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<td>43</td>
<td>84/57</td>
<td>500</td>
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</tbody>
</table>

* BOP is around 5-7 dB with different modulated signals used. Maximum value across the bandwidth is reported here.

DPA will be required for wireless applications. Due to its simple architecture and satisfactory performance, digital predistortion (DPD) [37] has been largely accepted as one of the fundamental blocks of wireless RF transceivers. In particular, the accurate PA behavior models proposed in [45]–[46] and effective wideband DPD verification approaches [47]–[48] have been successfully utilized for DPA linearization. However, due to the length restrictions, the linearization of the DPA is beyond the scope of this paper.

In Table IV, the performance of the proposed DPA is summarized and compared with other wideband DPAs in the literature. Given two DE thresholds across the bandwidth (65% at PP and 50% at BOP) the Reduced-a DPA offers the highest maximum efficiencies at both PP and BOP levels, along with a balanced wideband performance where the DE is maintained above these thresholds for most of the intended bandwidth.
VII. CONCLUSION

A new theoretical approach that generalizes the conventional DPA theory is introduced in this paper. The approach introduces a theoretical parameter at the output combiner side which relates the combiner parameters through closed form formulae, and relaxes the Doherty operational conditions, thereby providing greater design flexibility. Based on the analysis, a new DPA design is proposed to enhance the performance of the parallel DPA published previously. Simulation results over 25% FBW have shown an improvement in the DE, reaching a maximum of 82% and 66% at peak and 6-dB output BOP levels, respectively. The realized DPA has shown a reasonable linearity performance when measured with different modulated signals, where ACLR was around –25 dBc. This paper supports broadband DPA development for modern wireless communication standards, and provides new concepts for the DPA output combining network design.

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