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Precoder Design for Signal Superposition in MIMO-NOMA Multicell Networks

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Abstract—The throughput of users with poor channel conditions, such as those at a cell edge, is a bottleneck in wireless systems. A major part of the power budget must be allocated to serve these users in guaranteeing their quality-of-service (QoS) requirement, hampering QoS for other users and thus compromising the system reliability. In nonorthogonal multiple access (NOMA), the message intended for a user with a poor channel condition is decoded by itself and by another user with a better channel condition. The message intended for the latter is then successively decoded by itself after canceling the interference of the former. The overall information throughput is thus improved by this particular successive decoding and interference cancellation. This paper aims to design linear precoders/beamformers for signal superposition at the base stations of NOMA multi-input multi-output multi-cellular systems to maximize the overall sum throughput subject to the users’ QoS requirements, which are imposed independently on the users’ channel condition. This design problem is formulated as the maximization of a highly nonlinear and nonsmooth function subject to nonconvex constraints, which is very computationally challenging. Path-following algorithms for its solution, which invoke only a simple convex problem of moderate dimension at each iteration are developed. Generating a sequence of improved points, these algorithms converge at least to a local optimum. Extensive numerical simulations are then provided to demonstrate their merit.

Index Terms—Multi-user interference system, multi-input multi-output (MIMO), nonorthogonal multiple access (NOMA), nonconvex optimization, quality-of-service (QoS), successive interference cancellation (SIC), signal superposition.

I. INTRODUCTION

The explosive growth of mobile traffic demand is the driving force behind the development of signal processing and communication technologies to significantly upgrade the high-end experiences of communication such as high throughput, high reliability, and ubiquitous access. It is widely believed that interference-limited techniques such as coordinated multipoint transmission (CoMP) [1], [2], which treat interference as noise cannot meet the edge throughput requirements for 5G [3]. Dirty-paper coding (DPC) [4], under which the interference is successively mitigated, can improve both the edge and sum throughput but is difficult to implement in practice and remains only as a theoretical concept due to its high computational complexity. Nonorthogonal multiple access (NOMA) has been recently recognized as an essential enabling technology for 5G systems [5] due to its potential to improve the edge throughput [6].

In NOMA, a base station (BS) transmits a signal superposition to all users. The users are paired so that in each pair there is one with a better channel condition and another with a poorer channel condition [7]. The messages intended for each pair of users are sequentially decoded as follows. First, the message for the user with the poorer channel condition is decoded by both users. The message for the user with the better channel condition is then successively decoded by this user after canceling the interference from the other user [8]. Thus, while the throughput at the users with poorer channel condition remains the same as that in interference-limited techniques, the throughput at the users with better channel condition is clearly improved, leading to a higher system throughput.

Multi-input multi-output (MIMO) is widely known for its enormous potential in improving the capacity of wireless communication systems without requiring extra bandwidth or power. NOMA for MIMO communication (MIMO-NOMA) in single-cell systems for achieving higher throughput has been investigated in [9], [10], and an extension to multi-cell cases has been considered in [11]. In multi-cell systems, the effects of inter-cell interference are acute and unpredictable, limiting the quality-of-service...
(QoS) for cell-edge users. It is therefore challenging to realize the benefit that NOMA may bring to multi-cell systems.

A. Related Works

In this subsection we discuss the state-of-the-art of signal processing techniques for NOMA downlink transmission. NOMA was mostly studied for single-cell multi-input single-output (MISO) systems known as MISO-NOMA, where the multiple-antenna BS broadcasts signal superpositions to single-antenna users. Under the assumption on low QoS requirement for the near user (with a good channel condition) and high QoS requirement for the far user (with a poor channel condition) in a two-user MISO-NOMA, [12] proposed a heuristic computational procedure with neither convergence nor optimality guaranteed for the beamforming power minimization. Under similar users’ QoS requirements in a 2K-user MISO-NOMA, it used a particular zero-forcing beamformer to cancel the inter-pair interference, so the problem of 2K-user MISO-NOMA beamforming is decomposed into K independent subproblems of two-user MISO-NOMA beamforming. A closed-form solution for minimization of beamforming power in two-user MISO-NOMA subject to natural users’ QoS requirements was obtained in [13]–[15]. In [16], users performed successive interference cancellation (SIC) based on the channel gain differences. Its proposed algorithm for beamforming is of high computational complexity.

Regarding MIMO-NOMA, [9] and [10] derived the outage probability experienced by users in zero-forcing post-coding or signal alignment. Power allocation for achieving the ergodic capacity of two-user MIMO NOMA was considered in [17] and [18]. User-pairing to enhance the throughput of users of poor channel condition was proposed in [19], [11] proposed two interference alignment based coordinated beamforming for a two-cell MIMO-NOMA, where the interference at all cell-center users and edge-center users is canceled.

B. Motivation and Contributions

The paper considers the problem of designing linear precoders/beamformers at the BSs for MIMO-NOMA multi-cell systems to maximize their sum throughput while simultaneously meeting the users’ QoS requirements. In general, such a design problem is very complicated as the objective function is nonlinear and nonsmooth, and the QoS constraints are highly nonconvex, for which even finding a feasible point is already challenging. The main contributions of the paper are three-fold:

- For MIMO-NOMA, two path-following optimization algorithms are proposed for computation, which at least converge to a locally optimal solution. At each iteration, the first algorithm invokes a convex quadratic program while the second algorithm invokes a semi-definite program (SDP). Both these convex programs are of moderate dimension so their computation is very efficient.
- Another path-following algorithm tailored for MISO-NOMA is proposed, which explores much simpler structures of the throughput functions in MISO systems for more efficient computation.
- The provided numerical results show the essential performance improvements of NOMA based systems compared to the conventional systems. The capability of NOMA to improve both edge and sum throughput is revealed.

C. Paper Organization and Notation

The rest of the paper is organized as follows. Section II presents the system model and formulates the problem. A convex quadratic programming based path-following algorithm for the MIMO-NOMA problem is developed in Section III, while another SDP based path-following algorithm is developed in Section IV. Section V devotes to computation for MISO-NOMA problem. Numerical results are provided in Section VI, and Section VII concludes the paper.

Notation. Bold-faced upper-case letters are used for matrices, bold-faced lower-case letters are used for vectors, and lower-case letters are used for for scalars. I_n is the identity matrix of size n × n. X^H, X^T, and X* are the Hermitian transpose, normal transpose, and conjugate of a matrix X, respectively. The inner product ⟨X, Y⟩ of matrices X and Y is defined as trace(X^H Y). Denote by ⟨A⟩ the trace of a matrix A, and by |A| its determinant. ||·|| stands for matrix’s Frobenius norm or vector’s Euclidean norm. For Hermitian symmetric matrices A ≥ 0 (A > 0, resp.) means that A is a positive semidefinite (positive definite, resp.) matrix. Accordingly A ≥ B (A > B, resp.) means A − B ≥ 0 (A − B > 0, resp.). C is the set of all complex numbers, and ∅ is an empty set. ℜ{x} denotes the real part of a complex number x. x ∼ CN(η, Z) means that x is a random vector following a complex circular Gaussian distribution with mean η and covariance matrix Z. ∇_x f(x) is the gradient of function f(·) with respect to its variable x. E{·} denotes the expectation operator.
circular area with radius \( r_0 \) and the BS at its center, and \( K \) far UEs (cell-edge UEs), which are located within the ring area with inner radius \( r_0 \) and outer radius \( r_o \). \( K \) far UEs in each cell are not only in poorer channel conditions than other \( K \) near UEs but also are under more intensified inter-cell interference from adjacent cells.

Upon denoting \( \mathcal{I} \triangleq \{1,2,\cdots,N\} \) and \( \mathcal{J} \triangleq \{1,2,\cdots,2K\} \), the \( j \)-th UE in the \( i \)-th cell is referred to as UE \((i,j)\) \( j \in \mathcal{K}_1 \triangleq \{1,\cdots,K\} \) while the cell-edge UEs are UE \((i,j) \), \( j \in \mathcal{K}_2 \triangleq \{K+1,\cdots,2K\} \). Thus the set of cell-center UEs and the set of cell-edge UEs are \( \mathcal{S}_1 \triangleq \mathcal{I} \times \mathcal{K}_1 \) and \( \mathcal{S}_2 \triangleq \mathcal{I} \times \mathcal{K}_2 \), respectively. In NOMA each cell-center UE \((i,j)\in \mathcal{S}_1\) is randomly paired with cell-edge UE \((i,p(j))\in \mathcal{S}_2\) of the same cell to create a virtual cluster.\(^1\) The signal superpositions are precoded at the BSs prior to being transmitted to the UEs. Specifically, the message intended for UE \((i,j)\) is \( s_{i,j} \in \mathbb{C}^L \) with \( \mathbb{E}\{s_{i,j}\} = I_L \), which is precoded by matrix \( \mathbf{V}_{i,j} \in \mathbb{C}^{N_t\times L} \) where \( L \) is the number of concurrent data streams and \( L \leq \min\{N_t,N_r\} \). For notational convenience, let us define \( \mathbf{V} \triangleq \{\mathbf{V}_{i,j}\}_{(i,j)\in \mathcal{S}} \). The received signals at UE \((i,j)\) and UE \((i,p(j))\) are expressed as

\[
y_{i,j} = \mathbf{H}_{i,j} \mathbf{V}_{i,j} s_{i,j} + \mathbf{H}_{i,j} \mathbf{V}_{i,p(j)} s_{i,p(j)} + \sum_{(s,l)\in \mathcal{S}\setminus \{(i,j),(i,p(j))\}} \mathbf{H}_{s,i,j} \mathbf{V}_{s,l} s_{s,l} + n_{i,j} \tag{1}
\]

and

\[
y_{i,p(j)} = \mathbf{H}_{i,p(j)} \mathbf{V}_{i,p(j)} s_{i,p(j)} + \mathbf{H}_{i,j} \mathbf{V}_{i,j} s_{i,j} + \sum_{(s,l)\in \mathcal{S}\setminus \{(i,j),(i,p(j))\}} \mathbf{H}_{s,i,p(j)} \mathbf{V}_{s,l} s_{s,l} + n_{i,p(j)} \tag{2}
\]

where \( \mathbf{H}_{s,i,j} \in \mathbb{C}^{N_r\times N_t} \) is the MIMO channel from the BS \( s \in \mathcal{I} \) to UE \((i,j)\) \( s \in \mathcal{S} \). The entries of the additive noise \( n_{i,j} \in \mathbb{C}^{N_r} \) are independent and identically distributed (i.i.d.) noise samples with zero mean and variance \( \sigma^2 \). The covariances of \( y_{i,j} \) and \( y_{i,p(j)} \) are thus

\[
\mathbf{M}_{i,j}(\mathbf{V}) = \sum_{(s,l)\in \mathcal{S}} \mathbf{H}_{s,i,j} \mathbf{V}_{s,l} \mathbf{V}_{s,i,j}^H + \sigma^2 \mathbf{I}_{N_r},\tag{3}
\]

and

\[
\mathbf{M}_{i,p(j)}(\mathbf{V}) = \sum_{(s,l)\in \mathcal{S}} \mathbf{H}_{s,i,p(j)} \mathbf{V}_{s,l} \mathbf{V}_{s,i,p(j)}^H + \sigma^2 \mathbf{I}_{N_r}.
\]

The purpose of the paper is to design complex-valued precoding matrices \( \mathbf{V}_{i,j} \) to maximize the overall spectral efficiency under a given pairing for NOMA. The MIMO channel states \( \mathbf{H}_{s,i,j} \) are assumed unchanged during message transmission but may change independently from one message to another and are perfectly known at all nodes [10], [12], [16].

**B. Problem Formulation**

In NOMA, the message \( s_{i,p(j)} \) intended for the cell-edge UE \((i,p(j))\) is decoded by both UE \((i,p(j))\) and UE \((i,j)\). Then message \( s_{i,j} \) intended for the cell-center UE \((i,j)\) is decoded by itself only.

The cell-edge UE \((i,p(j))\) decodes its own message \( s_{i,p(j)} \) with the achievable rate

\[
\mathcal{R}_{i,p(j)}^{(j)}(\mathbf{V}) = \ln |\mathbf{L} + (\mathbf{V}_{i,p(j)}\mathbf{H}_{i,i,p(j)}^{H}\mathbf{M}_{i,p(j)}(\mathbf{V})^{-1}\mathbf{H}_{i,i,p(j)}\mathbf{V}_{i,p(j)})|^2 \tag{5}
\]

where \( \mathbf{M}_{i,p(j)}(\mathbf{V}) \) is defined by

\[
\mathbf{M}_{i,p(j)}(\mathbf{V}) = \mathbf{M}_{i,j}(\mathbf{V}) - \mathbf{H}_{i,i,p(j)} \mathbf{V}_{i,p(j)} \mathbf{V}_{i,p(j)}^{H} \mathbf{H}_{i,i,p(j)}^{H} + \sum_{(s,l)\in \mathcal{S}\setminus \{(i,p(j))\}} \mathbf{H}_{s,i,j} \mathbf{V}_{s,l} \mathbf{V}_{s,i,j}^{H} + \sigma^2 \mathbf{I}_{N_r}.
\]

On the other hand, the cell-center UE \((i,j)\) decodes the message \( s_{i,p(j)} \) with the achievable rate

\[
\mathcal{R}_{i,p(j)}^{(i)}(\mathbf{V}) = \ln |\mathbf{L} + (\mathbf{V}_{i,p(j)}\mathbf{H}_{i,i,p(j)}^{H}\mathbf{M}_{i,p(j)}(\mathbf{V})^{-1}\mathbf{H}_{i,i,p(j)}\mathbf{V}_{i,p(j)})|^2 \tag{7}
\]

where

\[
\mathbf{M}_{i,p(j)}(\mathbf{V}) = \mathbf{M}_{i,j}(\mathbf{V}) - \mathbf{H}_{i,i,j} \mathbf{V}_{i,p(j)} \mathbf{V}_{i,p(j)}^{H} \mathbf{H}_{i,i,j}^{H} + \sum_{(s,l)\in \mathcal{S}\setminus \{(i,p(j))\}} \mathbf{H}_{s,i,j} \mathbf{V}_{s,l} \mathbf{V}_{s,i,j}^{H} + \sigma^2 \mathbf{I}_{N_r}.
\]

Hence, the throughput by decoding the message \( s_{i,p(j)} \) by UEs \((i,p(j))\) and \((i,j)\) is

\[
\mathcal{R}_{i,p(j)} = \min \left\{ \mathcal{R}_{i,p(j)}^{(i)}(\mathbf{V}), \mathcal{R}_{i,p(j)}^{(j)}(\mathbf{V}) \right\} . \tag{9}
\]

---

\(^1\) Using more sophisticated user-pairing strategies may improve the performance of MIMO-NOMA networks (see e.g., [8], [19]) but it is beyond the scope of this paper.
Next, the throughput by decoding the message $s_{i,j}$ by the cell-center UE $(i,j)$ after decoding the message $s_{i,p(j)}$ is

$$R_{i,j}(V) = \ln \left| I_L + (V_{i,j})^H H_{i,j}^H M_{i,j}^p(V)^{-1} H_{i,j} V_{i,j} \right|$$

where

$$M_{i,j}^p(V) \triangleq M_{i,j}^{(j)}(V) - H_{i,j} V_{i,j} (V_{i,j})^H H_{i,j}^H = \sum_{(s,l) \in S \setminus \{ (i,p(j)), (i,j) \}} H_{s,i,j} V_{s,i,j} (V_{s,i,j})^H H_{s,i,j}^H + \sigma^2 I_{N_r}.$$ (11)

Our goal is to maximize the total sum throughput of the system under QoS for each individual UE and power budget at each BS, which is mathematically formulated as

$$\text{maximize } P(V) = \sum_{i=1}^N \sum_{j=1}^K (R_{i,j}(V) + R_{i,p(j)}(V))$$ (12a)

subject to

$$R_{i,j}(V) \geq r_{i,j}, \forall i \in \mathcal{I}, \forall j \in \mathcal{K}_1, \quad (12b)$$

$$R_{i,p(j)}(V) \geq r_{i,p(j)}, \forall i \in \mathcal{I}, \forall j \in \mathcal{K}_2, \quad (12c)$$

$$\sum_{j \in \mathcal{J}} \langle V_{i,j} V_{i,j}^H \rangle \leq P_{i}^{\max}, \forall i \in \mathcal{I}, \quad (12d)$$

where $P_{i}^{\max}$ in (12d) is the transmit power budget of BS $i$. The QoS constraints (12c) and (12d) set a minimum throughput requirement $r_{i,j}$ at the UE $(i,j)$ and $r_{i,p(j)}$ at the UE $(i,p(j))$.

### C. Relations to CoMP and DPC

In CoMP [1, 2], the problem of maximizing the sum throughput under QoS constraints is formulated as [20]

$$\text{maximize } P^{\text{CoMP}}(V) = \sum_{i=1}^N \sum_{j=1}^{2K} R'_{i,j}(V)$$ (13a)

subject to

$$R'_{i,j}(V) \geq r_{i,j}, \forall i \in \mathcal{I}, \forall j \in \mathcal{J}, \quad (13b)$$

$$\sum_{j \in \mathcal{J}} \langle V_{i,j} V_{i,j}^H \rangle \leq P_{i}^{\max}, \forall i \in \mathcal{I}, \quad (13c)$$

where $R'_{i,j}(V)$ is given by

$$R'_{i,j}(V) = \ln \left| I_L + (V_{i,j})^H H_{i,j}^H M_{i,j}^i(V)^{-1} H_{i,j} V_{i,j} \right|$$ (14)

with

$$M_{i,j}^i(V) \triangleq \sum_{(s,l) \in S \setminus \{ (i,j) \}} H_{s,i,j} V_{s,i,j} (V_{s,i,j})^H H_{s,i,j}^H + \sigma^2 I_{N_r}.$$ (15)

Compared $R'_{i,j}(V)$ defined by (14) to $R_{i,p(j)}(V)$ and $R_{i,j}(V)$ defined by (9) and (10) one can see that

$$R'_{i,p(j)}(V) = R_{i,p(j)}^p(V)$$ (16)

$$\sum_{j \in \mathcal{J}} \langle V_{i,j} V_{i,j}^H \rangle \leq P_{i}^{\max}, \forall i \in \mathcal{I}. \quad (22c)$$

Comparing $R'_{i,j}(V)$ defined by (14) to $R_{i,p(j)}(V)$ and $R_{i,j}(V)$ defined by (9) and (10) one can see that

$$R'_{i,p(j)}(V) = \min \left\{ R_{i,p(j)}^p(V), R_{i,j}(V) \right\} \quad (17)$$

$$= R_{i,p(j)}, \forall j \in \mathcal{K}_2, \quad (18)$$

and

$$R'_{i,j}(V) \leq R_{i,j}(V), \forall j \in \mathcal{K}_1, \quad (19)$$

i.e., under the same precoder $V$, the throughput at cell-edge UEs is higher with CoMP while that at cell-center UEs is higher with NOMA. Thus, under the same precoder, NOMA does not need to perform better than CoMP in terms of the total throughput. The preference of NOMA now critically depends on its performance at its optimal precoder, which is sought in the next sections.

On the other hand, DPC at the BS $i$ with encoding order from UE $(i,2K)$ to UE $(i,1)$ enables UE $(i,j)$ view the massages intended for UEs $(i,j'), j' > j$ as non-causally known and thus cancel them from its received signal. Hence, the throughput by decoding the message $s_{i,j}$ for UE $(i,j)$ is defined by

$$R''_{i,j}(V) = \ln \left| I_L + (V_{i,j})^H H_{i,j}^H M_{i,j}^i(V)^{-1} H_{i,j} V_{i,j} \right|$$ (20)

where

$$M_{i,j}^i(V) \triangleq \sum_{s \neq i} \sum_{l=1}^{2K} H_{s,i,j} V_{s,i,j} (V_{s,i,j})^H H_{s,i,j}^H + \sum_{k=1}^{2K} H_{i,k} V_{i,k} (V_{i,k})^H H_{i,k}^H + \sigma^2 I_{N_r}.$$ (21)

The problem of maximizing the sum throughput under QoS constraints is formulated as

$$\text{maximize } P^{\text{DPC}}(V) = \sum_{i=1}^N \sum_{j=1}^{2K} R''_{i,j}(V)$$ (22a)

subject to

$$R''_{i,j}(V) \geq r_{i,j}, \forall i \in \mathcal{I}, \forall j \in \mathcal{J}, \quad (22b)$$

$$\sum_{j \in \mathcal{J}} \langle V_{i,j} V_{i,j}^H \rangle \leq P_{i}^{\max}, \forall i \in \mathcal{I}. \quad (22c)$$

Apparently, under DPC the intra-cell interference from UEs of better channel quality is canceled in decoding the massages intended for UEs of poorer channel quality, resulting in much better edge throughput compared with CoMP. NOMA is advantageous over DPC in terms of ease of implementation. By increasing the QoSs’ requirement in (12b), (13b) and (22b), we will see that the NOMA’s sum throughput is fully superior over CoMP’s one and catches up DPC’s one.

### III. CONVEX QUADRATIC BASED ITERATIONS

Note that the QoS constraints (12b) and (12c) in (12), and (13b) in (13) are set beforehand, which are dependent on the UEs’ throughput requirements but independent on their channel conditions. In maximizing the sum throughput objective (13a), most of CoMP techniques (see e.g. [21]) are unable to address the QoS constraints (13b). Without setting such QoS constraints, the UEs of poor channel condition are easily disconnected from the service because it is well known that almost all of transmit power will be allocated to a very few UEs of the best channel conditions in maximizing the sum throughput, causing almost zero throughput at other UEs. The weighted sum throughput
maximization is only an ad hoc way to balance the UEs’ throughput. Alternatively, the throughput satisfaction can be effectively handled via maximizing the users’ worst throughput but the latter involves optimization of a non-smooth objective function, for which these techniques are powerless. Both QoS constrained sum throughput maximization problem (13) and UEs’ worst throughput maximization problem could be addressed very recently in [20].

Although the optimization problem (12) is different from (13) and (22), all functions appearing in the former have a similar structure to that appearing in the latter. Therefore, a systematic approach to solve the latter is expected to be applicable to the former. In this section, we adopt the approach of [20] to address (12). Unlike [22], which aims at expressing the nonsmooth function \( \mathcal{R}_{i,p}(V) \) in (9) and then the nonsmooth objective function in (12b) as d.c. (difference of two convex functions) by using the universality of d.c. functions [23] and leads to d.c. iterations [24] of high computational complexity, we will see now that each below iteration invokes only a simple convex quadratic program of low computational complexity.

Suppose that \( V^{(\kappa)} \triangleq \{ V_{i,j}^{(\kappa)} \}_{(i,j) \in S} \) is a feasible point found at the \((\kappa - 1)\)-th iteration. Define the following quadratic functions in \( V \):

\[
\mathcal{R}^{j,(\kappa)}_{i,p}(V) \triangleq a^{j,(\kappa)}_{i,p} + 2\Re \left\{ \langle A^{j,(\kappa)}_{i,p}V_{i,p}, V_{i,p} \rangle \right\} - \| M^{p(j)}_{i,j}V^{(\kappa)} - M_{i,j}(V) \|_F^2, \]

\[
\mathcal{R}^{p(j),(\kappa)}_{i,p}(V) \triangleq a^{p(j),(\kappa)}_{i,p} + 2\Re \left\{ \langle A^{p(j),(\kappa)}_{i,p}V_{i,p}, V_{i,p} \rangle \right\} - \| M^{p(j)}_{i,p}V^{(\kappa)} - M_{i,p}(V) \|_F^2, \]

\[
\mathcal{R}^{i,(\kappa)}_{i,j}(V) \triangleq a^{i,(\kappa)}_{i,j} + 2\Re \left\{ \langle A^{i,(\kappa)}_{i,j}V_{i,j}, V_{i,j} \rangle \right\} - \| M^{p(i)}_{i,j}V^{(\kappa)} - M_{i,j}(V) \|_F^2, \]

where \( a^{j,(\kappa)}_{i,p}, a^{p(j),(\kappa)}_{i,p}, a^{i,(\kappa)}_{i,j} \) are given as

\[
a^{j,(\kappa)}_{i,p} \triangleq R^{j}_{i,p}(V^{(\kappa)}) - \left\langle \left( V^{(\kappa)}_{i,p} \right)^H H_{i,j}^{H}, M_{i,j}(V^{(\kappa)}) \right\rangle < 0,
\]

\[
a^{p(j),(\kappa)}_{i,p} \triangleq R^{p(j)}_{i,p}(V^{(\kappa)}) - \left\langle \left( V^{(\kappa)}_{i,p} \right)^H H_{i,j}^{H}, M_{i,p}(V^{(\kappa)}) \right\rangle < 0,
\]

\[
a^{i,(\kappa)}_{i,j} \triangleq R^{i}_{i,j}(V^{(\kappa)}) - \left\langle \left( V^{(\kappa)}_{i,j} \right)^H H_{i,j}^{H}, M_{i,j}(V^{(\kappa)}) \right\rangle < 0,
\]

and \( A^{j,(\kappa)}_{i,p}, A^{p(j),(\kappa)}_{i,p}, A^{i,(\kappa)}_{i,j} \) are given as

\[
A^{j,(\kappa)}_{i,p} \triangleq H^{H}_{i,j}^{H} M_{i,j}(V^{(\kappa)})^{-1} H_{i,j} V^{(\kappa)}_{i,p} - H^{H}_{i,j}^{H} M_{i,j}(V^{(\kappa)})^{-1} H_{i,j} V^{(\kappa)}_{i,p},
\]

\[
A^{p(j),(\kappa)}_{i,p} \triangleq H^{H}_{i,j}^{H} M_{i,p}(V^{(\kappa)})^{-1} H_{i,j} V^{(\kappa)}_{i,p} - H^{H}_{i,j}^{H} M_{i,p}(V^{(\kappa)})^{-1} H_{i,j} V^{(\kappa)}_{i,p},
\]

\[
A^{i,(\kappa)}_{i,j} \triangleq H^{H}_{i,j}^{H} M_{i,j}(V^{(\kappa)})^{-1} H_{i,j} V^{(\kappa)}_{i,j} - H^{H}_{i,j}^{H} M_{i,j}(V^{(\kappa)})^{-1} H_{i,j} V^{(\kappa)}_{i,j}.
\]

Note that all functions in (23) are concave due to (6), (8), and (11):

\[
\mathcal{M}^{p(j)}_{i,p}(V^{(\kappa)})^{-1} - \mathcal{M}_{i,p}(V^{(\kappa)})^{-1} \geq 0,
\]

\[
\mathcal{M}^{p(j)}_{i,j}(V^{(\kappa)})^{-1} - \mathcal{M}_{i,j}(V^{(\kappa)})^{-1} \geq 0,
\]

\[
\mathcal{M}^{p(j)}_{i,j}(V^{(\kappa)})^{-1} - \mathcal{M}^{p(j)}_{i,j}(V^{(\kappa)})^{-1} \geq 0.
\]

The following result shows that the complicated function defined by (9) and (10) is lower bounded by concave quadratic functions.

\[ \text{Theorem 1: For } \mathcal{R}^{(\kappa)}_{i,p}(V) \triangleq \min \left\{ \mathcal{R}^{j,(\kappa)}_{i,p}(V), \mathcal{R}^{p(j),(\kappa)}_{i,p}(V) \right\} \text{ it is true that} \]

\[ \mathcal{R}^{(\kappa)}_{i,p}(V) = R^{(\kappa)}_{i,p}(V) \quad \text{and} \quad \mathcal{R}^{(\kappa)}_{i,p}(V) \geq R^{(\kappa)}_{i,p}(V), \forall V, \quad (26) \]

and

\[ \mathcal{R}^{(\kappa)}_{i,j}(V) = R^{(\kappa)}_{i,j}(V) \quad \text{and} \quad \mathcal{R}^{(\kappa)}_{i,j}(V) \geq R^{(\kappa)}_{i,j}(V), \forall V. \quad (27) \]

\[ \text{Proof: See [20, Appendix B].} \]

Based on these results, at the \( \kappa \)-th iteration, the following convex program, which is an inner approximation for the nonconvex optimization problem (12), is solved to generate the next feasible point \( V^{(\kappa+1)} \):

\[
\max_{V} P^{(\kappa)}(V) \triangleq \sum_{i=1}^{N} \sum_{j=1}^{K} \left( \mathcal{R}^{(\kappa)}_{i,j}(V) + \mathcal{R}^{(\kappa)}_{i,j}(V) \right) \quad (28a)
\]

subject to \( \mathcal{R}^{(\kappa)}_{i,j}(V) \geq r_{i,j}, \forall i \in I, \forall j \in K_{1} \), \( R^{(\kappa)}_{i,p}(V) \geq r_{i,p}, \forall i \in I, \forall j \in K_{2} \), \( (28b) \)

\[ (12d). \]

A pseudo-code of this quadratic programing (QP)-based path-following procedure is given by Algorithm 1.

Note that \( V^{(\kappa)} \) is also feasible for (28) with \( P(V^{(\kappa)}) = P(V^{(\kappa)}) \) by the equalities in (26) and (27). It is then true that \( P(V^{(\kappa+1)}) > P(V^{(\kappa)}) \) whenever \( V^{(\kappa+1)} \neq V^{(\kappa)} \). Together with \( P(V^{(\kappa+1)}) \geq P(V^{(\kappa)}) \) and according to the inequalities in (26) and (27), we have \( P(V^{(\kappa+1)}) > P(V^{(\kappa)}) \), i.e., the optimal solution \( V^{(\kappa+1)} \) of the convex quadratic problem (28) is a better point for the nonconvex nonsmooth optimization problem (12) than \( V^{(\kappa)} \). Therefore, once initialized from an feasible point \( V^{(0)} \), the sequence \( \{ V^{(\kappa)} \} \) obtained by solving (28) is of improved feasible points for (12). By following the same arguments as those in [20, Proposition 1], we can prove that Algorithm 1 converges to a Karush-Kuh-Tucker (KKT) point of (12).

\[ \text{Generation of the initial points: A feasible point for constraints (12b)-(12d) for initializing Algorithm 1 is found} \]
Applying (31) yields

\[ \text{(12a)-(12d).} \]

Complexity is

\[ 1 \]

SDP-based path-following algorithm for (12). To this end,

\[ \text{KN} \]

constraint (12d), the following iterations are invoked

\[ \text{Initialized from a feasible point} \]

\[ \text{till reaching a value more than or equal to 1 in satisfying} \]

(12b)-(12d).

**Complexity Analysis:** Problem (28) is convex quadratic with \( m_{QP} = N(1 + 3K) \) quadratic constraints and \( n = KN(2N_{2L} + 1) \) real decision variables. Its computational complexity is \( O(n^2m_{QP}^2 + m_{QP}^3) \).

**IV. Semi-Definite Programming Based Iterations**

To further improve the convergence speed of solving (12), we need explore more parallel convex structures of functions (9) and (10). In this section, we propose a novel SDP-based path-following algorithm for (12). To this end, we will use the following matrix inequalities:

\[ V^H X^{-1} V \geq V^H X^{-1} V + V^H \bar{X}^{-1} \bar{V}, \quad \forall V, \bar{V}, X > 0, \bar{X} > 0, \]

(31)

and

\[ \ln |X| \geq \ln |X| - \langle X, X^{-1} - \bar{X}^{-1} \rangle, \quad \forall X > 0, \bar{X} > 0, \]

(32)

whose proofs are given by Appendix A and Appendix B.

Let us treat the rate function \( \mathcal{R}^{(i)}(V) \) from (7) first. Applying (31) yields

\[ V^H \bar{H}^{i,j} \mathcal{M}^{(i)}(V)^{-1} \mathcal{H}^{i,j} V_{i,p(j)} \geq \mathcal{Q}^{(i)}(V) \]

(33)

for

\[ \bar{H}^{i,j}(V) \equiv (V_{i,p(j)}^{(i)})^H H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)} + (V_{i,p(j)}^{(i)})^H H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)} - (V_{i,p(j)}^{(i)})^H H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)} \times \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)}^{-1}, \]

(34)

which also satisfies

\[ \bar{Q}^{(i)}(V) = \]

\[ (V_{i,p(j)}^{(i)})^H H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)}, \]

(35)

For \( \mathcal{M}^{(i)}(V) \) defined from (8), applying (31) again yields

\[ \mathcal{M}^{(i)}(V) \geq \mathcal{L}^{(i)}(V) + \sigma^2 \mathcal{I}_{N_r} \]

over the trust region

\[ \mathcal{L}^{(i)}(V) \geq 0, \]

(37)

for the linear mapping

\[ \mathcal{L}^{(i)}(V) \equiv \sum_{(s,l) \in \mathcal{S}_{\{i,p(j)\}}} H_{s,i,j} \mathcal{V}_{s,l}(V_{s,l}) \]

(38)

It follows from (33) that

\[ \mathcal{Q}^{(i)}(V) \leq \mathcal{Q}^{(i)}(V) \]

(39)

for

\[ \mathcal{Q}^{(i)}(V) \equiv V_{i,p(j)}^{H} H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)} \]

(40)

Therefore,

\[ \mathcal{R}^{(i)}(V) \]

\[ = \ln |L| + (V_{i,p(j)}^{(i)})^H H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)} \]

\[ \geq \ln |L| + \mathcal{Q}^{(i)}(V) \]

\[ \geq \mathcal{R}^{(i)}(V) + L \]

\[- \langle I_L + \mathcal{Q}^{(i)}(V), \mathcal{L} + \mathcal{Q}^{(i)}(V)^{-1} \rangle \]

\[ \geq \mathcal{R}^{(i)}(V) \]

(41)

for

\[ \mathcal{R}^{(i)}(V) \]

\[ = \ln |L| + (V_{i,p(j)}^{(i)})^H H_{i,j}^{i,j} \mathcal{M}^{(i)}(V)^{-1} H_{i,j}^i V_{i,p(j)} \]

\[ \mathcal{L} + \mathcal{Q}^{(i)}(V)^{-1} \]

\[ \geq \mathcal{R}^{(i)}(V) \]

(42)

for

\[ \mathcal{R}^{(i)}(V) \]

\[ = \mathcal{R}^{(i)}(V) + L \]

\[- \langle \mathcal{L} + \mathcal{Q}^{(i)}(V), \mathcal{L} + \mathcal{Q}^{(i)}(V)^{-1} \rangle \]

\[ \geq \mathcal{R}^{(i)}(V) \]

(43)
which is a concave function. Inequality (41) follows from (33) and the condition
\[ \ln |I_L + X| \geq \ln |I_L + Y|, \quad \forall X \succeq Y \succeq 0. \]

Inequality (42) follows by applying (32) and using equality
\[ \ln |I_L + \tilde{Q}_2^{(\kappa)}(\mathbf{V}^{(\kappa)})| = R_{i,p}^j(\mathbf{V}^{(\kappa)}). \]

Inequality (43) follows from inequality (33), equality (35), and the condition
\[ \left\langle M, X^{-1} \right\rangle \geq \left\langle M, Y^{-1} \right\rangle, \quad \forall M \succeq 0, \ Y \succeq X \succ 0. \]

Analogously, the rate function \( R^{(\kappa)}_{i,p}(\mathbf{V}) \) and throughput function \( R_{i,j}(\mathbf{V}) \) defined from (5) and (10) are lower bounded by
\begin{equation}
R^{(\kappa)}_{i,p}(\mathbf{V}) \geq \tilde{R}^{(\kappa)}_{i,p}(\mathbf{V}) \geq 0, \tag{45}
\end{equation}
over the trust region
\begin{equation}
L^{(\kappa)}_{i,j}(\mathbf{V}) \geq 0, \tag{46}
\end{equation}
and
\begin{equation}
R_{i,j}(\mathbf{V}) \geq \tilde{R}_{i,j}(\mathbf{V}) \geq 0, \tag{47}
\end{equation}
over the trust region
\begin{equation}
L^{(\kappa)}_{i,j}(\mathbf{V}) \geq 0, \tag{48}
\end{equation}
for linear mappings
\begin{equation}
L^{(\kappa)}_{i,p}(\mathbf{V}) \triangleq \sum_{s,l \in S \setminus \{(i,j)\}}^\mathbf{H}_{s,i,p,j} \left[ \mathbf{V}_{s,l} (\mathbf{V}_{s,l}^H)^H \right] + \mathbf{V}_{s,l}^H - \mathbf{V}_{s,l}^H \mathbf{V}_{s,l}^H H_{s,i,p,j}^H \tag{49}
\end{equation}
and
\begin{equation}
L^{(\kappa)}_{i,i,p}(\mathbf{V}) \triangleq \sum_{s,l \in S \setminus \{(i,p,j), (i,j)\}}^\mathbf{H}_{s,i,p,j} \left[ \mathbf{V}_{s,l} (\mathbf{V}_{s,l}^H)^H \right] + \mathbf{V}_{s,l}^H - \mathbf{V}_{s,l}^H \mathbf{V}_{s,l}^H H_{s,i,p,j}^H, \tag{50}
\end{equation}
and for concave functions
\begin{equation}
\tilde{R}^{(\kappa)}_{i,p}(\mathbf{V}) \triangleq R^{(\kappa)}_{i,p}(\mathbf{V}) + L \tag{51}
\end{equation}
and
\begin{equation}
\tilde{R}^{(\kappa)}_{i,j}(\mathbf{V}) \triangleq R^{(\kappa)}_{i,j}(\mathbf{V}) + L \tag{52}
\end{equation}

\textbf{Algorithm 2} SDP-based path-following algorithm for the STM (12) in MIMO-NOMA

\textbf{Initialization:} Set \( \kappa := 0 \) and solve (57) to generate an initial feasible point \( \mathbf{V}^{(0)} \) for constraints (12b)-(12d).

1: \textbf{repeat}
2: Solve the semi-definite program (56) to obtain the optimal solution: \( \mathbf{V}^\ast. \)
3: Update \( \mathbf{V}^{(\kappa+1)} := \mathbf{V}^\ast. \)
4: Set \( \kappa := \kappa + 1. \)
5: \textbf{until Convergence}

with
\begin{align*}
Q^{(\kappa),k}_{i,p}(\mathbf{V}) & \triangleq (\mathbf{V}_{i,p}^{(\kappa)})^H \mathbf{H}_{i,i,p,j}^H \mathbf{M}_{i,p}^{(\kappa)} (\mathbf{V}_{i,p}^{(\kappa)})^{-1} \mathbf{H}_{i,i,p,j} \mathbf{V}_{i,p}(j) + (\mathbf{V}_{i,p}^{(\kappa)})^H \mathbf{H}_{i,i,p,j}^H \mathbf{M}_{i,p}^{(\kappa)} (\mathbf{V}_{i,p}^{(\kappa)})^{-1} \mathbf{H}_{i,i,p,j} \mathbf{V}_{i,p}(j) \\
& - (\mathbf{V}_{i,p}^{(\kappa)})^H \mathbf{H}_{i,i,p,j}^H \mathbf{M}_{i,p}^{(\kappa)} (\mathbf{V}_{i,p}^{(\kappa)})^{-1} \left[ \mathbf{L}_{i,p}(\mathbf{V}) \right] (\mathbf{V}) + \sigma^2 \mathbf{I}_{N_r} \mathbf{M}_{i,p}^{(\kappa)} (\mathbf{V}_{i,p}^{(\kappa)})^{-1} \mathbf{H}_{i,i,p,j} \mathbf{V}_{i,p}(j) \tag{53}
\end{align*}
and
\begin{align*}
\tilde{R}^{(\kappa)}_{i,p}(\mathbf{V}) & \triangleq \min \left\{ \tilde{R}^{(\kappa)}_{i,j}(\mathbf{V}), \tilde{R}^{(\kappa)}_{i,p}(\mathbf{V}) \right\}. \tag{55}
\end{align*}

In summary, at the \( \kappa \)-th iteration, the following SDP, which is an inner approximation of (12), is solved to generate the next feasible point \( \mathbf{V}^{(\kappa+1)}: \)

\begin{align*}
\max & \quad \tilde{\mathbf{P}}^{(\kappa)}(\mathbf{V}) \triangleq \sum_{k=1}^K \sum_{i=1}^N \left( \tilde{R}^{(\kappa)}_{i,j}(\mathbf{V}) + \tilde{R}^{(\kappa)}_{i,p}(\mathbf{V}) \right) \\
\text{subject to} & \quad \tilde{R}^{(\kappa)}_{i,j}(\mathbf{V}) \geq r_{i,j}, \ \forall i \in \mathcal{I}, \ \forall j \in \mathcal{K}_1, \tag{56a}
\end{align*}

\begin{align*}
\tilde{R}^{(\kappa)}_{i,p}(\mathbf{V}) \geq r_{i,p}, \ \forall i \in \mathcal{I}, \ \forall j \in \mathcal{K}_2. \tag{56b}
\end{align*}

The proposed Algorithm 2 generates a sequence \( \{\mathbf{V}^{(\kappa)}\} \) of improved points of (12), which also converges to a KKT point.

A feasible point \( \mathbf{V}^{(0)} \) for the constraints (12b)-(12d) to initialize Algorithm 2 can be found by invoking the iterations
\begin{align*}
\max & \min \min_{\mathbf{V}^{(\kappa)}} \left\{ \frac{\tilde{R}^{(\kappa)}_{i,j}(\mathbf{V})}{r_{i,j}}, \frac{\tilde{R}^{(\kappa)}_{i,p}(\mathbf{V})}{r_{i,p}} \right\} \tag{57a}
\end{align*}
subject to
\begin{align*}
(12d), (37), (46), (48). \tag{57b}
\end{align*}

to reach a value more than or equal to 1 in satisfying (12b)-(12d).
Complexity analysis: The SDP (56) involves $N(1+3K)$ quadratic constraints, $3NK$ semi-definite constraints with $N_r$ rows and $n = KN(2N_r L + 1)$ real decision variables. For $m_{SDP} \triangleq N(1+3K) + 3NKN_r$, its computational complexity is $O(n^2 m_{SDP} + m_{SDP}^3)$, which is seen higher than that of the convex quadratic problem (28).

V. TAILORED ALGORITHM FOR MISO-NOMA

In this case, all channels are row vectors $(\mathbf{H}_{s,i,j} \in \mathbb{C}^{1 \times N_r})$ and $s_{i,j} \in C \ (L = 1)$.

As observed first time in (25), for

$$\mathbf{V}_{i,j} = e^{-j\arg(\mathbf{H}_{s,i,j} \mathbf{V}_{s,i,j})} \mathbf{V}_{i,j}$$

one has $|\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}| = \mathbf{H}_{s,i,j} \mathbf{V}_{s,i,j} = \Re \{\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}\} \geq 0$ and $|\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}| = |\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}|$ for $(i', j') \neq (i, j)$. Therefore, without loss of generality we can replace

$$\mathbf{H}_{s,i,j} \mathbf{V}_{i,j} \mathbf{V}_{i,j}^H \mathbf{H}_{s,i,j}^H = |\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}|^2, \quad j = 1, \ldots, 2K$$

by

$$\Re \{\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}\}^2, \quad j = 1, \ldots, 2K$$

with

$$\Re \{\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}\} \geq 0, \quad j = 1, \ldots, 2K \quad (59)$$

(including $p(j)$ for $j = K + 1, \ldots, 2K$). Accordingly, write

$$\mathbf{M}_{i,j}(\mathbf{V}) = \sum_{(s,l) \in S_i} |H_{s,i,j} V_{s,l}|^2 + \sigma^2.$$

Then the message $s_{i,p(j)}$ intended for cell-edge UE $(i, p(j))$ is decoded by the cell-center UE $(i, j)$ with the achievable rate

$$r_{i,p(j)}(\mathbf{V}) = \ln \left(1 + \frac{|H_{i,j} V_{i,p(j)}|^2}{\mathbf{M}_{i,j}(\mathbf{V})}\right), \quad (60)$$

and is decoded by the cell-edge UE $(i, p(j))$ itself with the achievable rate

$$r_{i,p(j)}^p(\mathbf{V}) = \ln \left(1 + \frac{\Re \{H_{i,j} V_{i,p(j)}\}^2}{\mathbf{M}_{i,j}^p(\mathbf{V})}\right) \quad (61)$$

where

$$\mathbf{M}_{i,j}^p(\mathbf{V}) \triangleq \mathbf{M}_{i,j}(\mathbf{V}) - |H_{i,i,j} V_{i,p(j)}|^2 = \sum_{(s,l) \in S_i} |H_{s,i,j} V_{s,l}|^2 + \sigma^2,$$

and

$$\mathbf{M}_{i,p(j)}^p(\mathbf{V}) \triangleq \mathbf{M}_{i,p(j)}(\mathbf{V}) - |H_{i,i,j} V_{i,p(j)}|^2 = \sum_{(s,l) \in S_i} |H_{s,i,j} V_{s,l}|^2 + \sigma^2.$$

Also, the message $s_{i,j}$ intended for the cell-center UE $(i, j)$ is successively decoded by UE $(i, j)$ itself with the throughput

$$r_{i,j}(\mathbf{V}) = \ln \left(1 + \frac{\Re \{H_{i,i,j} V_{i,j}\}^2}{\mathbf{M}_{i,j}^p(\mathbf{V})}\right) \quad (62)$$

where

$$\mathbf{M}_{i,j}^p(\mathbf{V}) \triangleq \mathbf{M}_{i,j}(\mathbf{V}) - |H_{i,i,j} V_{i,j}|^2 = \sum_{(s,l) \in S_i} |H_{s,i,j} V_{s,l}|^2 + \sigma^2.$$

For $r_{i,p(j)}(\mathbf{V}) \triangleq \min \{r_{i,p(j)}(\mathbf{V})^p(\mathbf{V}), r_{i,p(j)}^p(\mathbf{V})\}$, the problem (12) in this case is

maximize $\mathbf{P}(\mathbf{V}) \triangleq \sum_{i=1}^N \sum_{j=1}^{K_i} (r_{i,j}(\mathbf{V}) + r_{i,p(j)}(\mathbf{V}))$ \quad (63a)

subject to $r_{i,j}(\mathbf{V}) \geq r_{i,j}, \ \forall i \in I, \ \forall j \in K_i$, \quad (63b)

$r_{i,p(j)}(\mathbf{V}) \geq r_{i,j}, \ \forall i \in I, \ \forall j \in K_i$, \quad (63c)

$r_{i,p(j)}^p(\mathbf{V}) \geq r_{i,j}, \ \forall i \in I, \ \forall j \in K_i$, \quad (63d)

$$\sum_{j \in J} \|\mathbf{V}_{i,j}\|^2 \leq P_{i,max}, \ \forall i \in I. \quad (63e)$$

Due to the above transforms (61) and (62) under condition (59), the nonconvex constraints (63b) and (63c) are expressed by the second-order cone (SOC) constraints

$$\Re \{\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}\} \geq \sqrt{e^{r_{i,j}} - 1} \sqrt{\mathbf{M}_{i,j}(\mathbf{V})}, \quad \forall i \in I, \ \forall j \in K_i, \quad (64)$$

$$\Re \{\mathbf{H}_{s,i,p(j)} \mathbf{V}_{i,p(j)}\} \geq \sqrt{e^{r_{i,p(j)}} - 1} \sqrt{\mathbf{M}_{i,p(j)}(\mathbf{V})}, \quad \forall i \in I, \ \forall j \in K_i, \quad (65)$$

but the constraint (63d) remains to be nonconvex.

To approximate functions in (63a) we use the inequality

$$\ln(1 + z) \geq a(\bar{z}) - \bar{b}(\bar{z}) \frac{1}{\bar{z}}, \quad \forall \bar{z} > 0, \ \bar{z} > 0 \quad (66)$$

with

$$0 < a(\bar{z}) \triangleq \ln(1 + \bar{z}) + \frac{\bar{z}}{\bar{z} + 1}, \quad 0 < \bar{b}(\bar{z}) \triangleq \frac{\bar{z}^2}{\bar{z} + 1}, \quad (67)$$

whose proof is provided by Appendix C.

Applying (66) for $\bar{z} = \bar{z}(\bar{\mathbf{M}}) \triangleq |\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}^{(\kappa)}|^2/\mathbf{M}_{i,j}^{(\kappa)}(\mathbf{V})$ and $\bar{z} = |\mathbf{H}_{s,i,j} \mathbf{V}_{i,p(j)}^{(\kappa)}|^2/\mathbf{M}_{i,p(j)}^{(\kappa)}(\mathbf{V})$ yields

$$r_{i,p(j)}(\mathbf{V}) \geq a(\bar{z}_{i,j}) \left(b(\bar{z}_{i,j}) \frac{\mathbf{M}_{i,j}^{(\kappa)}(\mathbf{V})}{|\mathbf{H}_{i,i,j} \mathbf{V}_{i,j}^{(\kappa)}|^2}\right) \geq a(\bar{z}_{i,j}) \left(\frac{\mathbf{M}_{i,j}^{(\kappa)}(\mathbf{V})}{|\mathbf{H}_{i,i,j} \mathbf{V}_{i,j}^{(\kappa)}|^2}\right), \quad (68)$$

over the trust region

$$\bar{z}_{i,j}^{(\kappa)}(\mathbf{V}) \triangleq 2 \Re \{\mathbf{H}_{s,i,j} \mathbf{V}_{i,j}^{(\kappa)} \mathbf{H}_{i,i,j} \mathbf{V}_{i,j}^{(\kappa)*}\} - |\mathbf{H}_{i,i,j} \mathbf{V}_{i,j}^{(\kappa)}|^2 > 0. \quad (69)$$
Algorithm 3 Tailored QP-based path-following algorithm for the STM (63) in MISO-NOMA

Initialization: Initialize a feasible point $V^{(0)}$ for constraints in (63).  

k-th iteration: Solve the convex quadratic program (74) to find the optimal solution $V^{*}$. If $|P(V^{*}) - P(V^{(k)})|/P(V^{(k)}) \leq \epsilon$, terminate. Otherwise, set $k := k + 1, V^{(k)} := V^{*}$ and continue.

Analogously, 

$$r^{p(j),i,p(j)}_{i,j} \geq r^{p(j),i,p(j)}_{i,p(j)}(V) \triangleq a(z^{p(j),i,p(j)}_{i,j}) - b(z^{p(j),i,p(j)}_{i,j}) \frac{\lambda_{p(j),i,p(j)}(V)}{\varphi^{p(j),i,p(j)}_{i,j}(V)}$$  

(70)

with 

$$\varphi^{p(j),i,p(j)}_{i,j}(V) \triangleq \Re\{H_{i,i,p(j)}V^{(i)}_{i,p(j)}\} \left(2\Re(H_{i,i,p(j)}V_{i,p(j)}) - \Re(H_{i,i,p(j)}V^{(i)}_{i,p(j)})\right)$$

over the trust region

$$2\Re(H_{i,i,p(j)}V_{i,p(j)}) - \Re(H_{i,i,p(j)}V^{(i)}_{i,p(j)}) > 0, \quad (71)$$

and

$$r_{i,j}(V) \geq r^{(i)}_{i,p(j)}(V) \triangleq a(z^{(i)}_{i,j}) - b(z^{(i)}_{i,j}) \frac{\lambda_{p(j),i,p(j)}(V)}{\varphi^{(i)}_{i,j}(V)}$$  

(72)

with 

$$\varphi^{(i)}_{i,j}(V) \triangleq \Re\{H_{i,i,j}V^{(i)}_{i,j}\} \left(2\Re(H_{i,i,j}V_{i,j}) - \Re(H_{i,i,j}V^{(i)}_{i,j})\right)$$

over the trust region

$$2\Re(H_{i,i,j}V_{i,j}) - \Re(H_{i,i,j}V^{(i)}_{i,j}) > 0. \quad (73)$$

In Algorithm 3, we propose an QP-based path-following algorithm to solve problem (63). At the k-th iteration it solves the following SOC program to generate the next feasible point $V^{(k+1)}$;

$$\max_{V} \quad P^{(i)}(V) \triangleq \sum_{i=1}^{N} \sum_{j=1}^{K} \left( r^{j}_{i,p(j)}(V) + r^{(i)}_{i,p(j)}(V) \right)$$ 

subject to $r^{j}_{i,p(j)}(V) \geq r_{i,p(j)}, \forall i \in I, \forall j \in K_{2}$, (63e), (64), (65), (69), (71), (73) 

(74a)

where $r^{(i)}_{i,p(j)}(V) \triangleq \min\{r^{j}_{i,p(j)}(V), r^{p(j),i,p(j)}_{i,j}(V)\}$.  

To find a feasible point for constraints in (63) for initializing Algorithm 3, initialized by a feasible point $V^{(0)}$ for the convex constraints (63e), (64), and (65), the following SOC based iterations

$$\max_{V} \min_{(i,j) \in S_{2}} \left\{ r^{j}_{i,p(j)}(V) \right\}$$ 

subject to (63e), (64), (65), (69) 

(75a)

are invoked for reaching a value more or equal to 1 in satisfying constraints in (63).

Complexity analysis: The SOC program (74) involves $m_{SOC} = N(1+6K)$ quadratic or SOC constraints and $n = KN(2N_{L} + 1)$ real decision variables. Its computational complexity is $O(n^{2}m_{SOC}^{2.5} + m_{SOC}^{3.5})$, which is seen higher than that of the convex quadratic problem (28).

VI. NUMERICAL RESULTS

In this section we use numerical examples to evaluate the performance of the proposed algorithms. A system topology shown in Fig. 2 is set up. There are $N = 3$ macro cells and 4 UEs per cell with two cell-center UEs and two cell-edge UEs, which are located near to the boundaries with the two adjacent cells. Unless stated otherwise, $N_{t} = 4$ and $N_{r} = 2$ are set for MIMO-NOMA, for which $L = N_{r}$ is set. Thus, the precoder-matrices $V_{i,j}$ are of dimension $N_{t} \times N_{r}$. The channel matrix between a BS and a UE at a distance $d$ (in kilometres) is generated as $H = \sqrt{10^{-\alpha_{PL}}/10}H$ [26]. Here, $\alpha_{PL}$ is the path loss (PL) in dB and the entries of $H$ are independent and identically distributed complex Gaussian variables with zero mean and unit variance. Without loss of generality, the requirement thresholds for all UEs are set as $r_{i,j} = r_{i,p(j)} = \bar{R}$ and the same power budget $P^{\max}_{i} = P^{\max}$, $\forall i \in I$ is given to all BSs.

For the ease of reference, the other parameters given in Table I including $\bar{R}$ are used. The error tolerance in the proposed Algorithms is set to $\epsilon = 10^{-3}$. The numerical results are obtained using the parser YALMIP [27]. The achieved sum throughput results are divided by $\ln(2)$ to arrive at the unit of bps/channel-use. Each simulation is run 100 times and the result are averaged to arrive at the final figures.

A. Algorithms’ Convergence

Fig. 3 shows the typical convergence behavior of the proposed algorithms for a given set of channel realizations that are randomly generated for the two cases. According to Fig. 3(a), both Algorithm 1 and 2 for MIMO-NOMA reach the almost optimal value of sum throughput in 18 and 13 iterations. As expected, Algorithm 2 converges faster than Algorithm 1. On the other hand, according to Fig. 3(b), Algorithm 3 for NOMA-MISO converges very fast reaching the optimal value in 6 iterations.
B. Numerical Results for MIMO-NOMA

For the ease of reference, the result achieved by (13) is labeled by “Conventional MIMO-CoMP” whereas that achieved by (12) is labeled by “Proposed MIMO-NOMA.” Fig. 4(a) plots the sum throughput versus the power budget \( P_{\text{max}} \) under setting \( \bar{R} = \{0, 1\} \) bps/Hz. For \( \bar{R} = 0 \) bps/Hz, i.e. there is no UEs’ QoS requirement imposed, CoMP slightly outperforms MIMO-NOMA by achieving throughput concentrated at the cell-center UEs of good conditions. Table II details the UEs’s throughput distribution for \( P_{\text{max}} = 30 \) dBm. The high ratio \( \frac{9.39}{0.38} = 24.7 \) between the best UE throughput and the worst UE throughput (BWR) implies that CoMP would perform wobbly in the QoS maximization problem (29) (with \( r_{i,j} = 1 \)), which also expresses the system ability to offer the uniform service to UEs. BWR for MIMO-NOMA is 5.1 = 7.13/1.39 so it is expected to outperform CoMP in maximizing (29). The low throughput 1.46 bps/Hz at UE (3, 4) by DPC is a result of a strong interference from an adjacent cell, which cannot be mitigated by DPC.

For \( \bar{R} = 1 \) bps/Hz, MIMO-NOMA of course offers a higher sum throughput than CoMP, where the BSs are seen spending a nearly full power budget \( P_{\text{max}} \) in gaining the sum throughput. Increasing \( P_{\text{max}} \) also leads to a remarkable gain in sum throughput by NOMA compared with CoMP. The sum throughput by the former also catches up that by DPC. The gain of MIMO-NOMA is a result of canceling interference from intra-cluster interference, as shown in (11). The cell-center UEs in CoMP experience intra-cluster interference that becomes stronger when transmit power increases. The plot of sum throughput versus QoS requirement threshold \( \bar{R} \in [0.6, 2.4] \) bps/Hz is shown by Fig. 4(b) for \( P_{\text{max}} = 30 \) dBm. The sum throughput are nearly flat for \( \bar{R} \leq 1.2 \) bps/Hz and are degraded after that. The BSs in CoMP must allocate much more power to serve cell-edge UEs when QoS threshold increases. As a result, the system sum throughput is dropped quickly. In contrast, the sum throughput of MIMO-NOMA is still slightly sensitive to QoS requirement threshold because

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carrier frequency/ Bandwidth</td>
<td>2 [GHz]/ 20 [MHz]</td>
</tr>
<tr>
<td>Noise power density</td>
<td>-174 [dBm/Hz]</td>
</tr>
<tr>
<td>Path loss from the BS to a UE, ( \sigma_{PL} )</td>
<td>128.1 + 37.6log_{10}(d) [dB]</td>
</tr>
<tr>
<td>Shadowing standard deviation</td>
<td>8 [dB]</td>
</tr>
<tr>
<td>Radius of each cell, ( r_o )</td>
<td>500 [m]</td>
</tr>
<tr>
<td>Coverage of near UEs, ( r_n )</td>
<td>150 [m]</td>
</tr>
<tr>
<td>Distance between BS and nearest UE</td>
<td>&gt; 10 [m]</td>
</tr>
<tr>
<td>Threshold ( \bar{R} )</td>
<td>1 [bps/Hz]</td>
</tr>
</tbody>
</table>

**Fig. 2.** MIMO-NOMA multi-cell system.

**Fig. 3.** Convergence pattern for \( P_{\text{max}} = 30 \) dBm.
BSs can tune the power allocation in meeting cell-edge UEs’ QoS requirements whenever the cell-center UEs’ QoS requirement is easily met.

Fig. 5 shows the impact of the number of UEs per cell and the number of transmit antennas at the BS on the performance of the system. Fig. 5(a) shows that MIMO-NOMA can deliver an acceptable sum throughput for large $K$. Again, MIMO-NOMA outperforms CoMP in all $K$. The sum throughput of the both systems decreases from a certain value of $K$ where there is not much degree-of-freedom (DoF) for leveraging multi-user diversity. Interestingly, MIMO-NOMA achieves its best sum throughput for $K = 3$ (6 UEs) while CoMP is peaked at $K = 2$ (4 UEs). Of course, these numbers are not magic and can be changed in other settings. Fig. 5(b) plots the sum throughput vs the number $N_t$ of antennas at the BSs.

Table III details the throughput at UEs under setting $N_t = 6$ and $P_{\text{max}} = 30$ dBm. Under the same QoS requirement threshold for UEs, the CoMP’s throughput is mostly contributed by the cell-center UEs, i.e. CoMP still tends to punish the cell-edge UEs, who are in poor channel condition. Raising the QoS requirement for the cell-edge UEs to counter this discrimination would lead to the risk of CoMP service feasibility. In contrast, in maximizing the system’s throughput, MIMO-NOMA offers much fairer and balanced services without contrasting the QoS requirement thresholds so it is very suitable for new quality-of-experience (QoE) services for cell-edge UEs.

By Fig. 6, the system’s throughput achieved by the
proposed precoder design is compared to that achieved by signal alignment MIMO-NOMA (SA MIMO-NOMA) [10] and interfering channel alignment CoMP MIMO-NOMA (ICA-CoMP MIMO-NOMA) [11] in the two-cell scenario with $K = 4$ users, $N_t = 5$, while $N_r = 4$ is set to make the signal and channel alignment feasible. In SA MIMO-NOMA, the inter-cluster interference is canceled by detection vectors based SA technique at the UEs and zero-forcing (ZF) based precoder matrix at the BSs. In ICA-CoMP MIMO-NOMA, a receive beamformer is constructed at the cell-edge UEs to align the interfering channels, and then a transmit beamformer based on the null space at the BS is designed to ensure zero inter-cell and inter-cluster interference. For the cell-center UEs, a ZF decoder is designed to cancel the inter-cluster interference only. To ensure a fair comparison, it is additionally assumed that the cell-center UEs do not experience inter-cell interference as they are far away from the neighboring cell in practice [11]. The two different settings of $P_{\text{max}} = (15 \text{ dBm}, 30 \text{ dBm})$, according to 3GPP TR 36.942 v.9.0.1 with a 46-dBm maximum transmit power for the 20 MHz bandwidth are under consideration. Fig. 6 plots the cumulative distribution function (CDF) of the sum throughput. As expected, MIMO-NOMA outperforms both ICA-CoMP MIMO-NOMA and SA MIMO-NOMA. Specifically, by controlling the interference to the cell-edge UEs more efficiently, MIMO-NOMA reaches 1.5 bps/Hz and 5.9 bps/Hz higher than the ICA-CoMP MIMO-NOMA and SA MIMO-NOMA, respectively, in about 60% of the simulated trials with $P_{\text{max}} = 15 \text{ dBm}$ (see Fig. 6(a)). With $P_{\text{max}} = 30 \text{ dBm}$, it is even more essential (see Fig. 6(b)).

C. Numerical Results for MISO-NOMA

The performance of MISO-NOMA achieved by (63) is compared to that achieved by the two-stage beamforming in [12]. The key idea of the two-stage beamforming is that
ZF beamforming is employed at the BS first to cancel the inter-pair interference and then SIC is used for each pair of UEs. The optimal solution for two-stage beamforming can be easily found by using Algorithm 3.

Fig. 7 plots the total sum throughput vs. the number of transmit antennas at the BS under setting $N = 3, K = 2$ and $P^{\text{max}} = 30$ dBm. Note that two-stage beamforming requires $N_t \geq 2(K - 1) + 2 = 4$. Unsurprisingly, MISO-NOMA achieves a better sum throughput than the two-stage beamforming. Two-stage beamforming achieves closer performance to MISO-NOMA as the number $N_t$ of transmit antennas increases, providing more degrees of freedom to leverage multi-user diversity. Fig. 8 plots the CDF of the sum throughput at $N_t = 6$. The performance gap is narrower at a higher power budget.

Fig. 9. Average sum throughput (b) for the MIMO-NOMA, and (c) for the MISO-NOMA with different cluster sizes ($N_t = 12$ and $P^{\text{max}} = 30$ dBm).
D. Comparison for Different Cluster Sizes

As the last numerical example, we investigate the system performance in a single-cell scenario of more than two UEs grouped to create a virtual cluster for NOMA. There are 6 UEs in total, which are randomly placed in three different areas, as shown by Fig. 9(a). Two cell-center UEs are located inside the disc of radius $r_c = 100$ m, two cell-middle UEs are located in the ring of inner radius 100 m and outer radius 250 m, and two cell-edge UEs are located inside the ring of inner radius 250 m and outer radius 500 m. Different cluster sizes are considered: two UEs per cluster, three UEs per cluster, and six UEs per cluster. For two-UE-per-cluster, a cell-center UE is randomly paired with a cell-middle UE, while the other is randomly paired with a cell-edge UE. The unpaired cell-middle UE and cell-edge are then paired to create the third cluster. There are two scenarios in grouping for three-UE-per-cluster.

- scenario-1 (more distinct channel conditions): each cluster consists of a cell-center UE, a cell-middle UE and a cell-edge UE;
- scenario-2 (less distinct channel conditions): each cluster consists of a cell-center UE.

The order of decoding messages for UEs in the same cluster of size three is as follows: the message for a cell-edge UE is decoded by all UEs, the message for a cell-middle UE is decoded by itself and the third UE by canceling the previously decoded message for the cell-edge UE from the intra-cluster, and the message for the third UE is decoded by itself only by canceling all previously decoded messages from the intra-cluster interference. Analogously, the messages for UEs (1, 1), (1, 2), (1, 3), (1, 4), (1, 5) and (1, 6) are successively decoded and canceled from the intra-cell interference in the case of six-UE-per-cluster, i.e. all UEs of the same cell have NOMA. The proposed algorithms are easily adapted for solution of the corresponding sum throughput maximization problems.

Fig. 9(b) and Fig. 9(c) plot the sum throughput achieved by different clustering versus throughput threshold for MIMO-NOMA and MISO-NOMA under setting $N_t = 12$ and $P_{\text{max}} = 30$ dBm. In general, the sum throughput achieved by the three-UE-per-cluster and six-UE-per-cluster based schemes are dropped less than that achieved by two-UE-per-cluster based one when the threshold $R$ raises. Specifically, in Fig. 9(b), the sum throughput of the three-UE scenario 2 and six-UE are worse than the two-UE for $R < 2.4$ bps/Hz and vice versa. The BS will allocate a much higher transmit power to the UE of the worst channel condition in the three-UE and six-UE schemes than in the two-UE scheme to meet the QoS constraints. In other words, the cell-edge UEs’ throughput is significantly improved in larger cluster sizes.

Notably, the sum throughput by three-UE scenario 1 catches up that by DPC for larger $R$ in both Fig. 9(b) and Fig. 9(c). In addition, six-UE scheme cannot provide a good sum throughput since large UEs per cluster may have error propagation in SIC leading to drastically reduce NOMA performance. Another interesting observation is that the sum throughput of the three-UE scenario 1 outperforms that of the other schemes. Recalling that NOMA is more efficient by exploiting their channel condition differences, i.e. 3-UE scenario 1 with more distinct channel conditions. Consequently, a larger cluster size is recommended for more distinct channel conditions while a smaller cluster size is recommended for less distinct channel conditions.

VII. CONCLUSIONS

We have addressed the problem of sum throughput maximization in NOMA based systems by proposing new path-following optimization algorithms. Numerical examples with realistic parameters have confirmed their fast convergence to an optimal solution. They reveal that NOMA not only helps increase the cell-edge UEs’ throughput substantially but also achieves much higher total sum throughput. The appropriate size of UE cluster with more distinctive channel gains has also been shown to achieve remarkable gains in NOMA systems.

APPENDIX A

PROOF FOR INEQUALITY (31)

By [28, Appendix B]

\[
(\alpha V_1 + \beta V_2)^H (\alpha X_1 + \beta X_2) (\alpha V_1 + \beta V_2) \leq \\
\alpha V_1^H X_1^{-1} V_1 + \beta V_2^H X_2^{-1} V_2
\]

(76)

for all $\alpha \geq 0$, $\beta \geq 0$, $\alpha + \beta = 1$ and $V_1$, $V_2$, $X_1 > 0$, $X_2 > 0$. This means for all $x$, function

\[
f(V, X) = x^H V^H X^{-1} V x
\]

(77)

is convex. Then, for all $V$, $V$, $X > 0$, $X > 0$ it is true that [23]

\[
f(V, X) \geq f(\bar{V}, \bar{X}) + \langle \nabla f(\bar{V}, \bar{X}), (V, X) - (\bar{V}, \bar{X}) \rangle
\]

\[
= x^H \left[ \bar{V}^H \bar{X}^{-1} V + V^H \bar{X}^{-1} \bar{V} - \bar{V}^H \bar{X}^{-1} XX^{-1} \bar{V} \right] x,
\]

(78)

i.e.,

\[
x^H V^H X^{-1} V x \geq x^H \left[ \bar{V}^H \bar{X}^{-1} V + V^H \bar{X}^{-1} \bar{V} - \bar{V}^H \bar{X}^{-1} XX^{-1} \bar{V} \right] x, \forall x
\]

(79)

proving (31).
APPENDIX B
PROOF FOR INEQUALITY (32)
Since function $\ln |X|$ is concave on $X > 0$, it is true that [23]
$$-\ln |A| \geq -\ln |B| - \langle B^{-1}, A - B \rangle,$$
\[ \forall A \succ 0, B \succ 0 \] (80)
or equivalently
$$\ln |A|^{-1} \geq \ln |B|^{-1} - \langle B^{-1}, A - B \rangle,$$
\[ \forall A \succ 0, B \succ 0 \] (81)
Then (32) follows by substituting $X = A^{-1}$ and $\bar{X} = B^{-1}$ into (81).

APPENDIX C
PROOF FOR INEQUALITY (66)
By [29, Th. 6] function $\ln(1 + x^{-1})$ is convex on $x > 0$ so for all $x > 0$ and $\bar{x} > 0$, it is true that [23]
$$\ln(1+x^{-1}) \geq \ln(1+\bar{x}^{-1}) + [(1+\bar{x}^{-1})^{-1} - x^{-1}] (x-\bar{x}).$$
(82)
Inequality (66) then follows by substituting $z = x^{-1}$ and $\bar{z} = \bar{x}^{-1}$ into (82).

REFERENCES
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