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A Compact Reconfigurable NRI-TL Metamaterial Phase-Shifter for Antenna Applications

Muhammad Ali Babar Abbasi, Marco A. Antoniades, and Symeon Nikolaou

Abstract—This paper presents a compact reconfigurable phase-shifter based on negative-refractive-index transmission-line (NRI-TL) metamaterial unit cells. Two inter-switchable NRI-TL metamaterial unit cells are collocated within the same board area, and can be reconfigured based on the biasing polarity of embedded PIN diodes to provide two discrete phase states. The PIN diodes are located on the shunt branches of the metamaterial line in order to reduce losses in the direct signal path. Design limitations in terms of return loss and insertion loss are discussed in relation to the two phase states. A proof-of-concept module with a size of 17.8 × 21.6 mm2 is designed at 1 GHz, with measured insertion phases of −14.5° and +58.5° in the two phase states leading to a differential phase shift of 73°, while exhibiting insertion losses of 1.43 dB and 0.89 dB, respectively. The combined bandwidth for which the reflection coefficient is below −10 dB is 0.46 GHz (46%), from 0.83 GHz to 1.29 GHz.

Index Terms—Negative-refractive-index transmission-line (NRI-TL), reconfigurable, metamaterial, phase shifter.

I. INTRODUCTION

Artificial material engineering has enabled the design and development of compact, cost-effective and high-performance solutions at microwave, terahertz and optical frequencies. The electromagnetic behavior of metamaterial structures is modified intentionally by adjusting either their electrical or geometrical properties to formulate non-linear materials, semiconductor structures, liquid crystals, microfluids and so on [1]. Within the same framework, the increasing demand for tunable microwave systems for advanced steerable antenna applications has further advanced research towards reconfigurability within metamaterials. At microwave frequencies, recent developments in negative-refractive-index transmission line (NRI-TL) metamaterials [2-3] have enabled the design and realization of electrically small reconfigurable metamaterial lines. The reconfigurability is achieved by loading a host transmission line with adjustable lumped capacitors and inductors. The practical use of such NRI-TL metamaterials still poses a number of technological and theoretical challenges in terms of operational bandwidth, losses, realization complexity, tuning speed and tolerance sensitivity. Over and above the aforementioned challenges, the inclusion of the tuning mechanism (biasing lines and control mechanism) must not affect the desired electromagnetic behavior of the reconfigurable system. Traditionally, ferrites have been used to achieve continuous phase shifting in antenna array systems [4-5], but more recently other novel materials such as graphene have also been used [6].

Some prominent techniques to achieve reconfigurability in metamaterial phase shifters include microfluidic channels [7], mechanically variable MIM capacitors [8], CMOS-based active inductors [9-10], BST thick-film substrates [11], GaAs [12-13] and Schottky varactor diodes [14], ferroelectric varactors [15], and MEMS capacitors [16].

In this work, a reconfigurable NRI-TL metamaterial phase shifter is presented that uses PIN diodes to change the insertion phase through the device. Two phase states have been achieved by reciprocating the polarity of the biasing voltage. Using the same physical microstrip transmission line to host more than one NRI-TL metamaterial unit cell, leads to a degradation in the performance of the phase shifter when switching from one state to another. These issues are thoroughly discussed, leading to the major contribution of this work, which is the application of a multivariable optimization algorithm that allows the device to exhibit low insertion loss and good impedance matching for both phase states. A detailed analysis related to design limitations and the matching topology used to match both phase states in a common design is presented in the following sections.

II. PROPOSED RECONFIGURABLE NRI-TL METAMATERIAL

NRI-TL metamaterials are synthesized by periodically loading a conventional microwave transmission line with lumped-element series capacitors and shunt inductors. Fig. 1(a) shows the equivalent circuit of a symmetric II-shaped NRI-TL metamaterial unit cell [17]. Here, a host transmission line with characteristic impedance \( Z_0 \), series inductance per unit length \( L \), shunt capacitance per unit length \( C \), and length \( d \) has been loaded with a lumped-element series capacitor \( C_0 \) and two shunt inductors \( 2L_0 \). The conventional host transmission line realizes a negative phase response, \( \phi_{H-TL} \), while the series capacitive and shunt inductive loading forms a backward-wave (BW) line with a positive phase response, \( \phi_{BW} \), as shown in Fig. 1(b). Under effective medium conditions, the phase shift per NRI-TL metamaterial unit cell is given by [3]:

\[
\phi_{H-TL} = \phi_{H-TL}^c + \phi_{H-TL}^w \tag{1a}
\]

\[
\phi_{BW} = -\pi \sqrt{L_c d} + \frac{1}{\omega \sqrt{L_c C_0}} \tag{1b}
\]

This is valid under the impedance matching condition below, which stipulates that both the lines must have the same characteristic impedance.

\[
Z_0 = \sqrt{\frac{L}{C}} = \sqrt{\frac{L_0}{C_0}} \tag{2}
\]
In this work, a microstrip transmission line with an impedance of $Z_0 = 50 \, \Omega$ and a fixed length of $d = 35 \, \text{mm}$ is used to host two collocated and reconfigurable NRI-TL metamaterial phase-shifting lines that realize two discrete phase states, State $A$ and State $B$, given by $\phi_{\text{MTM}_A}$ and $\phi_{\text{MTM}_B}$, respectively. The architecture of the two individual NRI-TL metamaterial lines is shown in Fig. 1(c) and (d). Both lines have the same series components, and differ only in the locations and values of the shunt loading inductors, $L_{dA}$ and $L_{dB}$. By switching between the two inductor values, a fixed phase change can be effected, according to (1b). A change in the value of $L_0$ without changing $C_0$, however, will lead to a mismatch along the line, since the impedance matching condition of (2) will no longer apply. This is mitigated by the fact that the two metamaterial unit cells used in Fig. 1 (c) and (d) also differ in size, given by $d_A$ and $d_B$ respectively, providing an additional degree of freedom that is used to provide good impedance matching in both states. Note that the total length of both the metamaterial lines (including the feed lines) always remains fixed at $d = d_A + d_c + d_B = 35 \, \text{mm}$.

### III. RECONFIGURABLE PHASE SHIFTER DESIGN

Initially, the structure of Fig. 1(a) was used to design a two-state NRI-TL metamaterial line with a fixed length. Using (1) and the design procedure outlined in [17], p. 17 with $\phi_{\text{H-TL}} = -70^\circ$ at a design frequency of $f_0 = 1 \, \text{GHz}$, the loading element values required to achieve a phase of $\phi_{\text{MTM}_A} = -15^\circ$ in State $A$ are $C_0 = 3.2 \, \text{pF}$, and $L_0 = 8.0 \, \text{nH}$, while to achieve a phase of $\phi_{\text{MTM}_B} = +60^\circ$ in State $B$ the values are $C_0 = 1.4 \, \text{pF}$, and $L_0 = 3.5 \, \text{nH}$. The values for the phases $\phi_{\text{MTM}_A}$ and $\phi_{\text{MTM}_B}$ were chosen representatively in order to realize a proof-of-concept design with two phase states that are not harmonically related. The transmission and reflection characteristics of the two-state metamaterial line are presented in Fig. 2. It can be observed from Figs 2(a) and 2(b) that in both states the metamaterial line exhibits excellent transmission and reflection characteristics around 1 GHz, while the two desired phase states are achieved.

Combining two NRI-TL metamaterial lines representing two distinct phase states poses two major challenges. Firstly, when the same transmission line is used to host two NRI-TL unit cells with reconfigurability only in the shunt branch, a single series loading capacitor $C_0$ must be used for both phase states, which results in impedance matching degradation. To further elaborate on this, consider the NRI-TL metamaterial unit cell from above that incurs a phase of $\phi_{\text{MTM},A} = -15^\circ$ at 1 GHz in State $A$, that is now required to change its phase to $\phi_{\text{MTM},B} = +60^\circ$ at 1 GHz in State $B$ without changing the value of $C_0$. To increase the phase incurred to achieve a higher phase in State $B$ using the same unit cell size and series capacitive loading, the shunt loading inductance $L_0$ must be decreased according to (1b), since $\phi_{\text{H-TL}}$ and $C_0$ will remain constant. The gradual decrease in the value of $L_0$ that leads to a higher incurred phase can be seen clearly in Fig. 3, together with the commensurate degradation of the impedance matching at 1 GHz. This is due to the mismatch between the characteristic impedance of the transmission line ($50 \, \Omega$) and the backward-wave line ($21.7 \, \Omega$), which makes the impedance matching condition of (2) invalid. The second major challenge in the implementation of the two-state phase shifter is that a reconfigurable mechanism is required that does not disturb the matching and phase response of the metamaterial line while switching between the two phase states.

The proposed reconfigurable NRI-TL metamaterial phase-shifter shown in Fig. 4 resolves both these problems. The phase-shifting line consists of a microstrip transmission line with a series loading capacitor $C_0$, and two pairs of reconfigurable shorted stubs, namely $\text{Stub } A$ ($l_{A1} + l_{A2} + l_{A4}$) and $\text{Stub } B$ ($l_{B1} + l_{B2} + l_{B3}$), which host the shunt loading inductors $2L_{dB}$ and $2L_{dB}$, and which are placed in shunt at fixed distances along the transmission line. The two main functions of these stubs are to facilitate the reconfigurability mechanism enabling them to switch between the two discrete shunt inductor loading values, and to aid in impedance matching.

The metamaterial phase-shifter of Fig. 4 was first designed in the Keysight – Advanced Design System (ADS) simulator as shown in Fig. 5 to incur an insertion phase in State $A$ of $\phi_{\text{MTM}_A} = -15^\circ$ at 1 GHz using the two central stubs ($\text{Stub } A$), while the
two outer stubs (Stub B) were turned off. Subsequently, the two outer stubs (Stub B) were turned on, and the two inner ones (Stub A) were turned off while keeping C0 constant, in order to achieve an insertion phase in State B of $\phi_{MTM_B} = +60^\circ$ at 1 GHz, thus achieving a differential phase shift of 75°. In doing so, a similar impedance matching degradation to the one shown in Fig. 3(a) was observed. Thus, Quasi-Newton multivariable optimization was used to match the impedance of both State A and State B using the following algorithm.

**IV. OPTIMIZATION ALGORITHM**

**Step 1:** For phase State A, design a metamaterial unit cell on a transmission line with an impedance $Z_0$, length $d$, phase shift $\phi_{MTM_A}$ at frequency $f_0$, and formulate initial $C_0$ and $L_{0A}$ values.

**Step 2:** Design stub A with lengths L_A1, L_A2, and L_A3 and gaps to host $L_{0A}$ and PIN diode with forward polarity.

**Step 3:** For phase State B, calculate $\phi_{MTM_B}$ while $C_0$ is kept the same as defined in Step 1.

**Step 4:** Design stub B with lengths L_B1, L_B2, and L_B3 and gaps to host $L_{0B}$ and PIN diode with reverse polarity.

**Step 5:** Evaluate optimized values of the optimization variables using Quasi-Newton multivariable optimization with the following simultaneous goals:

1. $|S_{11}|$ in State A $< -10$ dB at $f_0$
2. $|S_{11}|$ in State B $< -10$ dB at $f_0$
3. $\phi_{MTM_A} = \phi_{MTM_B} = \pm E_0$
4. $\phi_{MTM_A} = \phi_{MTM_B} = \pm E_0$
5. $2 \times (TL_{L1} + TL_{L2} + TL_{L3}) = d$

(Where $E_0$ are the tolerance factors in degrees with initial value = 0.5°)

If the optimization criteria are satisfied go to the next sequential step. Else go to Step 14.

**Step 6:** Define optimization variables L_B1, L_B2, L_B3, L_A1, L_A2, and L_A3. Go to Step 5. If already optimized, go to next sequential step.

**Step 7:** Define optimization variables TL_L1, TL_L2, TL_L3. Repeat Step 5 and 6. If already optimized, go to next sequential step.

**Step 8:** Define optimization variables $L_{0A}$ and $L_{0B}$. Repeat Step 5, 6 and 7.

**Step 9:** Replace the optimized values of $L_{0A}$ and $L_{0B}$ with closest discrete inductance value from the Coilcraft chip inductor library. Repeat Step 5, 6 and 7.

**Step 10:** Define optimization variables $C_0$. Repeat Step 5, 6 and 7.

**Step 11:** Replace the optimized value of $C_0$ with closest discrete capacitance value from the Murata chip capacitor library. Repeat Step 5, 6 and 7.

**Step 12:** Define optimization variables $RS_{L1}$, $RS_{L2}$, $RS_{W}$, $RS_{\theta}$. Repeat Step 5, 6 and 7.

**Step 13:** Decrease $E_A$ and $E_B$ values by 0.5°. Repeat Steps 6-12.

**Step 14:** Increase $E_A$ and $E_B$ values by 0.5°. Repeat Steps 6-12.

**Step 15:** End.

The algorithm was used with the following inputs: $Z_0 = 50 \, \Omega$, $d = 35 \, \text{mm}$, $\phi_{MTM_A} = -15^\circ$ (State A), $\phi_{MTM_B} = +60^\circ$ (State B) and $f_0 = 1$ GHz. Upon successful completion of the optimization algorithm, the final values of the lumped components were $C_0 = 3.10 \, \text{pF}$, $L_{0A} = 0.55 \, \text{nH}$, $L_{0B} = 1.40 \, \text{nH}$, while the optimized geometrical dimensions of the phase shifter are listed in Table I. The resulting phase difference between states A and B was $73^\circ$. The proposed algorithm works for a given $\phi_{MTM_A}$ and $\phi_{MTM_B}$ and the error tolerance factors $E_A$ and $E_B$ can be set based on the application in which the proposed model is to be used. For the scenario discussed in section III, the final values of $E_A$ and $E_B$ were 1.5°.

**V. FABRICATION**

To achieve reconfigurability, a Skyworks SMP1345 PIN diode was used, which achieves ON and OFF states based on the biasing polarity. It is important to note that the polarity of the diode on Stub A (D−) is opposite to the polarity of the diode on Stub B (D+). Negative biasing through the radial stubs ($U_{rs}$, $W_{rs}$, $V_{rs}$, and $\theta_{rs}$) along the top of the microstrip line in Fig. 4 turns on the two diodes D−, and turns off the two diodes D+, thus defining State A. Similarly, positive biasing through the radial stubs reverses this operation, consequently defining State B. The DC ground for the differential diode biasing voltage is applied on the microstrip ground and is applied to the diodes through the grounding vias at the end of the stubs.

Surface-mount Murata chip capacitors (GJM03 series) and Coilcraft chip inductors (0402CS series), both with high self-resonant frequencies well above the operating frequency, were used in the realization of the phase shifter. It is important to mention that the achievable phase states rely on the available lumped-element component values in the Murata GJM03 series and the Coilcraft 0402CS series component libraries. The gaps $g_1$ and $g_2$ were designed keeping in mind the recommended soldering footprint for each lumped-element component and the diodes.

Finally, Keysight – ADS was used to design and analyze the performance of the proposed reconfigurable NRI-TL phase shifter using realistic S-parameter models for the Murata capacitors, the Coilcraft inductors and the Skyworks diodes, in conjunction with a realistic model of the physical geometry of

**TABLE I**

<table>
<thead>
<tr>
<th>parameter</th>
<th>Length (mm)</th>
<th>parameter</th>
<th>Length (mm)</th>
<th>parameter</th>
<th>Length (mm)</th>
</tr>
</thead>
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<tr>
<td>$l_{11}$</td>
<td>6.95</td>
<td>$l_{01}$</td>
<td>1.00</td>
<td>$w_A$</td>
<td>1.90</td>
</tr>
<tr>
<td>$l_{21}$</td>
<td>6.80</td>
<td>$l_{02}$</td>
<td>2.30</td>
<td>$w_B$</td>
<td>0.50</td>
</tr>
<tr>
<td>$l_{31}$</td>
<td>3.75</td>
<td>$l_{03}$</td>
<td>1.00</td>
<td>$g_1$</td>
<td>0.50</td>
</tr>
<tr>
<td>$l_{12}$</td>
<td>3.80</td>
<td>$l_{r1}$</td>
<td>1.49</td>
<td>$g_2$</td>
<td>1.20</td>
</tr>
<tr>
<td>$l_{22}$</td>
<td>1.40</td>
<td>$w_B$</td>
<td>1.90</td>
<td>$r_{rs}$</td>
<td>1.50</td>
</tr>
<tr>
<td>$l_{32}$</td>
<td>6.00</td>
<td></td>
<td></td>
<td>$\theta_{rs}$</td>
<td>70°</td>
</tr>
</tbody>
</table>
the microstrip lines and gaps on a Rogers RO4003C substrate ($\varepsilon_r = 3.38$, $\tan \delta = 0.0027$, $h = 0.813 \text{ mm}$), as can be seen in the full simulation models of Figs 4 and 5. For a two-state insertion phase of $\phi_{\text{MTM}, A} = -15^\circ$ in State $A$ and of $\phi_{\text{MTM}, B} = +60^\circ$ in State $B$, the final optimized set of loading values was determined to be $C_0 = 3.1 \text{ pF}$, $2L_{0A} = 1.1 \text{ nH}$, and $2L_{0B} = 2.8 \text{ nH}$, corresponding to available discrete values in the Murata GJM03 and the Coilcraft 0402CS component series. It is worth mentioning here that the total shunt inductance for a particular state is a combination of the loading inductance ($L_{0A}$ or $L_{0B}$), the internal inductance of the Skyworks diodes ($L_{\text{PIN}} = 0.7 \text{ nH}$) and the physical dimensions of the corresponding stub (Stub $A$ or Stub $B$). The final layout dimensions of the phase shifter are also listed in Table I.

The fabricated prototype of the proposed reconfigurable NRI-TL phase shifter is presented in Fig 6(a). First, the microstrip conductor and gap patterns shown of Fig. 4 were realized on the Rogers RO4003C substrate using a LPKF ProtoMat H100 milling machine. Holes of 0.4 mm diameter were drilled at the end of all four stubs for the placement of shorting vias. Then, the lumped components ($C_0$, $2L_{0A}$ and $2L_{0B}$) and diodes (D$^-$ and D$^+$) were soldered onto the microstrip transmission lines, as shown in the zoomed-in view of the central metamaterial unit cell in Fig. 6 (b). Finally, SMA connectors were attached for the S-parameter measurements.

To achieve reconfigurability, a Skyworks SMP1345 PIN diode was used, which achieves ON and OFF states based on the biasing polarity. It is important to note that the polarity of the diode on Stub $A$ (D$^+$) is opposite to the polarity of the diode on Stub $B$ (D$^-$). Negative biasing through the radial stubs ($l_{\text{rs}}, W_{\text{rs}}, r_{\text{rs}}$, and $\theta_{\text{rs}}$) along the top of the microstrip line in Fig. 4 turns on the two diodes D$^-$, and turns off the two diodes D$^+$, thus defining State $A$. Similarly, positive biasing through the radial stubs reverses this operation, consequently defining State $B$. The DC ground for the differential diode biasing voltage is applied on the microstrip ground and is applied to the diodes through the grounding vias at the end of the stubs.

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Finally, Keysight – ADS was used to design and analyze the performance of the proposed reconfigurable NRI-TL phase shifter using realistic S-parameter models for the Murata capacitors, the Coilcraft inductors and the Skyworks diodes, in conjunction with a realistic model of the physical geometry of the microstrip lines and gaps on a Rogers RO4003C substrate ($\varepsilon_r = 3.38$, $\tan \delta = 0.0027$, $h = 0.813 \text{ mm}$), as can be seen in the full simulation models of Figs 4 and 5. For a two-state insertion phase of $\phi_{\text{MTM}, A} = -15^\circ$ in State $A$ and of $\phi_{\text{MTM}, B} = +60^\circ$ in State $B$, the final optimized set of loading values was determined to be $C_0 = 3.1 \text{ pF}$, $2L_{0A} = 1.1 \text{ nH}$, and $2L_{0B} = 2.8 \text{ nH}$, corresponding to available discrete values in the Murata GJM03 and the Coilcraft 0402CS component series. It is worth mentioning here that the total shunt inductance for a particular state is a combination of the loading inductance ($L_{0A}$ or $L_{0B}$), the internal inductance of the Skyworks diodes ($L_{\text{PIN}} = 0.7 \text{ nH}$) and the physical dimensions of the corresponding stub (Stub $A$ or Stub $B$). The final layout dimensions of the phase shifter are also listed in Table I.

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VI. RESULTS AND DISCUSSION

The simulated and measured results of the reconfigurable NRI-TL phase shifter are shown in Fig. 7, where it can be
observed that there is very good correlation between the two. The reflection coefficients for both State A and State B shown in Fig. 7(a) are well below −10 dB at 1 GHz, indicating good impedance matching at the design frequency. At 1 GHz, the simulated and measured $|S_{11}|$ are 18.34 dB and −19.33 dB, respectively for State A, while they are −29.05 dB and −23.38 dB, respectively for State B. The advantages achieved by excluding the tuning mechanism from the direct signal path can be witnessed in terms of the low insertion losses, seen in Fig. 7(b). The simulated and measured $|S_{21}|$ are −1.53 dB and −1.43 dB, respectively for State A, and −0.23 dB and −0.89 dB, respectively for State B. In Fig. 7(c), the phase response of an unloaded microstrip line is compared with the simulated and measured phase responses for both State A and State B. From Fig. 7(a), (b) and (c), it can be observed that the reconfigurable NRI-TL metamaterial phase shifter retains its good impedance matching and transmission characteristics even though the insertion phase is significantly changed from State A to State B. At 1 GHz, the transmission line phase shift of $\phi_{TL} = -70^\circ$ is compensated by $\phi_{BW} = 55.5^\circ$ and $128.5^\circ$ for State A and State B, respectively (as discussed in Section III), resulting in $\phi_{STM,A} = -14.5^\circ$ and $\phi_{STM,B} = +58.5^\circ$ at 1 GHz. The measured phase shift deviates by 2.4% and 0.03% from the predicted simulated value for State A and State B, respectively, which is well within the fabrication tolerances. Although the difference between the simulated and measured phase responses is relatively small, cascaded phase shifters and phase sensitive systems like Directional Modulation (DM) antenna arrays demand more accuracy. This error can be associated with the observable fabrication anomalies especially at the transition between the transmission line and the stubs, caused due to the limitations of the in-house fabrication facilities, as highlighted in Fig. 6(b). The measured phase error can be further decreased by a more careful and controlled fabrication of the microstrip traces, for example using wet etching and photolithography. The group delay of the reconfigurable NRI-TL phase shifter is shown in Fig. 7(d), depicting good simulation and measurement agreement for both states. At 1 GHz, the measured group delay is 0.5 ns for State A, and 0.9 ns for State B, and these remain relatively flat in the range of 0.4 ns to 1.3 ns across the operating band shown.

Fig. 7. Simulated and measured responses of the reconfigurable NRI-TL metamaterial phase shifter. (a) $|S_{11}|$, (b) $|S_{21}|$, (c) phase of $S_{21}$, and (d) group delay.

Fig. 8 shows the surface current distribution on the conductors of the NRI-TL metamaterial phase shifter for State A and State B. It can be observed that the maximum surface current resides within the defined NRI-TL metamaterial unit cell for a particular state, while the un-used stubs carry an insignificant amount of surface current, resulting in very good isolation in both states. The measured phase difference between the two states, $\Delta \Phi = \angle S_{21,B} - \angle S_{21,A}$, is shown in Fig. 9, where it can be observed that it is relatively flat with a value of 73° at 1 GHz that varies between 38.4° to 89.1° in the range shown.

Although the operational range of the proposed algorithm in Section IV depends upon the acceptable tolerance factor for any given application, an overview has been presented in Table II where the proposed algorithm was tested for a range of $\phi_{BW}(s)$ for both states while $Z_0$ and $f_0$ were kept the same as they were in the solution presented in Fig. 4 and Table I. The resulting set of $\phi_{STM}(s)$ for both states are shown in Table II, where it is evident that the phase deviation from the intended $\phi_{STM}$ remains below 1% for $\phi_{BW}$ as low as 20° and $\phi_{BW}$ as high as 160°. On the other hand, the algorithm still converged when $\phi_{BW,A}$ and $\phi_{BW,B}$ were 100° and 200° respectively, while the phase deviation was 10.25% from the intended phase difference. Despite the different phase differences the overall size of the phase-shifter’s transmission line does not change. Finally, Table III summarizes the performance of the proposed reconfigurable NRI-TL metamaterial phase shifter and other phase shifters found in the literature, which compares quite favorably. It has the most compact size (0.07 λ × 0.06 λ) when normalized with respect to the central frequency wavelength, the widest bandwidth (18.7%) within which the phase of $S_{21}$ varies less than ±20°, and has the lowest insertion loss amongst the phase shifters implemented with lumped surface-mount components. Albeit its compact and simple structure, one of the major disadvantages of the proposed architecture is the discrete phase shift that it can achieve.

<table>
<thead>
<tr>
<th>Frequency(GHz)</th>
<th>$\phi_{BW,A}$</th>
<th>$\phi_{BW,B}$</th>
<th>Desired $\Delta \Phi$</th>
<th>$\phi_{STM,A}$</th>
<th>$\phi_{STM,B}$</th>
<th>Realized $\Delta \Phi$</th>
<th>Phase deviation</th>
</tr>
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<tr>
<td>20°</td>
<td>40°</td>
<td>20°</td>
<td>-50.69°</td>
<td>-30.08°</td>
<td>20.61°</td>
<td>0.19%</td>
<td></td>
</tr>
<tr>
<td>40°</td>
<td>80°</td>
<td>40°</td>
<td>-29.69°</td>
<td>+10.06°</td>
<td>39.75°</td>
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<td>120°</td>
<td>60°</td>
<td>-10.01°</td>
<td>+52.97°</td>
<td>62.98°</td>
<td>0.83%</td>
<td></td>
</tr>
<tr>
<td>80°</td>
<td>160°</td>
<td>80°</td>
<td>+10.97°</td>
<td>+89.40°</td>
<td>78.43°</td>
<td>0.27%</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 8. Normalized surface current distribution at 1 GHz on the conductors of the NRI-TL metamaterial phase shifter in (a) State A, and (b) State B.

Fig. 9. Measured phase difference between the two states.
Other topologies that have achieved continuous phase tuning capabilities can be found in [8-10]. An extension of this work would be to apply existing continuous phase tuning methods to the architecture proposed herein.

VII. CONCLUSION

A novel architecture of a reconfigurable phase-shifter based on NRI-TL metamaterial unit cells has been presented that is compact in size and exhibits low insertion loss characteristics. By modeling and optimizing two collocated NRI-TL metamaterial II unit cells loaded with the same series capacitance but different shunt inductances, two distinct phase states have been achieved. It has been shown that by decreasing the shunt inductance in an NRI-TL unit cell to achieve a higher phase shift while using the same series capacitance, disturbs the matching of the unit cell severely. Good matching has been achieved in both phase states by adjusting the length and positions of the inductively-loaded shorted stubs. The reconfigurable mechanism has been achieved by placing PIN diodes on four shorted stubs, enabling the device to operate in two phase states based on the biasing polarity. This also avoids the presence of lossy components in the direct signal path. The proposed device was fabricated on a 17.8 × 21.6 mm² Rogers RO4003C substrate and the measured results show good agreement with the simulations. The usable bandwidth of the proposed device for which the |S11| of both states simultaneously remains below −10 dB is 0.46 GHz (46%), from 0.83 GHz to 1.29 GHz. In State A, the phase shifter achieves a phase shift of −14.5°, while in State B +58.5°, resulting in a measured differential phase shift of 73° at 1 GHz. The measured |S21| for State A is −1.43 dB, and for State B −0.89 dB. The realized phase difference is representative, and the same metamaterial phase-shifting architecture can also be used to achieve any arbitrary phase shifting value till ΔΦ = 90°. Thus, the proposed reconfigurable NRI-TL metamaterial phase-shifter is ideal for use in feeding networks of next-generation antenna array systems for pattern and polarization diversity applications. Also, the capability to achieve high phase differences makes it well suited for use in massive MIMO systems since the compact footprint of the proposed phase shifter is easy to be accommodated within the limited space left in a massive MIMO system, which includes a large number of radiating elements. In addition, despite the different phase differences the overall physical dimensions of the phase-shifter’s transmission line remain unchanged and thus rather compact. Most importantly, the phase shifter, because of its small size compared to the wavelength at f₀ does not radiate itself, and therefore it does not perturb the radiation pattern of the array, even when it is implemented on the same layer as the radiating elements.

REFERENCES
