Spectrophotometric and Digital Colour Colourimetric (DCC) analysis of Colour-based Indicators


Published in:
SENSORS AND ACTUATORS B-CHEMICAL

Document Version:
Peer reviewed version

Queen's University Belfast - Research Portal:
Link to publication record in Queen's University Belfast Research Portal

Publisher rights
Copyright 2018 Elsevier.
This manuscript is distributed under a Creative Commons Attribution-NonCommercial-NoDerivs License (https://creativecommons.org/licenses/by-nc-nd/4.0/), which permits distribution and reproduction for non-commercial purposes, provided the author and source are cited.

General rights
Copyright for the publications made accessible via the Queen's University Belfast Research Portal is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy
The Research Portal is Queen’s institutional repository that provides access to Queen’s research output. Every effort has been made to ensure that content in the Research Portal does not infringe any person’s rights, or applicable UK laws. If you discover content in the Research Portal that you believe breaches copyright or violates any law, please contact openaccess@qub.ac.uk.
Spectrophotometric and Digital Colour Colourimetric (DCC) analysis of Colour-based Indicators

Dilidaer Yusufu and Andrew Mills*

School of Chemistry and Chemical Engineering, Queens University Belfast, BT9 5AG

e-mail: andrew.mills@qub.ac.uk

Key words: digital photography; spectrophotometry; RGB; colour analysis; colour indicators
Abstract

Seven simulated absorption spectra that span the visible spectrum, are used to probe the degree of linear correlation that exists between real absorbance, $A_o$, at $\lambda_{max}$, and three well-established colour-based parameters, based on the standard Red, Green and Blue scale, sRGB, namely: (i) apparent absorbance, $A(sRGB)$, (ii) apparent fraction of absorbed light, 1-T(sRGB), where T is the apparent transmittance and (iii) colour difference, $\Delta E$. In all cases the colour-based parameter, $A(sRGB)$, linearly correlates best with $A_o$. This predicted correlation is tested using three different, actual colour-based indicators, using UV/Vis absorption spectroscopy to monitor the change in actual absorbance of each of the indicators and digital photography to monitor simultaneously the change in the values of sRGB, and so $A(sRGB)$. The three different indicators used were: a CO$_2$ indicator, a photocatalytic activity indicator and an oxygen indicator. In all three cases the apparent absorbance parameter, $A(sR)$, derived from sRGB analysis of the digital images, is proportional to the real absorbance, as measured using UV/Vis spectrophotometry, and able to yield the same key analytical information. The increasing use of sRGB analysis of digital photographic images, i.e. digital colour colourimetry, DCC, is discussed briefly.
Introduction

There is a great deal of interest in optical sensors and probes, which are able to respond reversibly, or irreversibly, to specific analytes [1]. In many cases the optical effect is a colour change measured using UV/Vis absorption spectroscopy, where a change in the measured absorbance at a specific wavelength, $A_{\lambda}$, is usually related simply to a change in concentration of the analyte under test. However, even when used in a very basic form, UV/Vis spectroscopy is not an inexpensive technique, nor is it particularly portable, both of which add to the overall cost of analysis when using optical sensors.

Interestingly, there is a recent and growing interest in the use of digital photography, coupled with digital image analysis, to probe colour changing reactions that are so often studied using UV/Vis spectroscopy. For example, Knutson et al. have used digital photography to study the kinetics of reaction between crystal violet and hydroxide ions [2]. Wang et al. have used a mobile phone's digital camera to probe the colour change associated with a microchip enzyme-linked immunosorbent assay, ELISA, when exposed to different levels of the ovarian HE4 biomarker in urine [3]. Capitan-Vallvey et al. have used colour digital photography for one-shot, multi-ion (potassium, magnesium and hardness) detection [4] and Ozcan et al. have used mobile phone microscopy for high resolution pathology imaging [5]. And finally and most recently, photography has been used monitor an epidermal UV colorimetric dosimeter and is now the basis of L'Oreal's 'My Patch' UV dosimeter, which involves monitoring UV dose with a mobile phone digital camera coupled to an App [6]. Interestingly, in several of the different examples cited above the method used to relate the digital photographic data to the analyte concentration was different. The above approach to quantitative analysis via digital image analysis, has been termed 'digital camera colourimetry', which we shall refer to henceforth as DCC, given its clear link with conventional colourimetry and its use of simple (non-spectrophotometric) devices, such as the filter photometer [7, 8].

Colour has been precisely defined internationally and standards have been developed to ensure accurate colour representation [9, 10]. Thus, the International Colour Consortium, ICC, have defined a device-independent, standard Red ($R$), Green ($G$) and Blue ($B$) colour space, sRGB, where any colour in that colour space is defined by the values of $R$, $G$ and $B$, each of which ranges from zero to 255 (i.e. 8 bit format), or 0 to 1 (sometimes referred to
as: \textit{fractional format}) \cite{11}. Whatever the format, often these values are referred to as 'intensities' and this terminology will be adopted here, since, as we shall see, they are used in DCC to generate apparent absorbance and transmittance values, i.e. $A(sRGB)$ and $T(sRGB)$, respectively, \textit{vide infra}. Many image analysis mobile phone Apps (ColorMeter \cite{12}, Color Card \cite{13}, and Color Mate \cite{14}) and open source digital image processing programs, such as: ImageJ \cite{15}, Adobe Photoshop \cite{16} or Image Colour Picker \cite{17}, are able to analyse readily any part of a digital image and return the \textit{non-linear sRGB} values associated with the colour.

As noted earlier, in many of the examples of DCC cited above the individual methodologies used to relate the \textit{sRGB} colour data to the analyte concentration were different. For example, Knutson \textit{et al.} \cite{2}, in their study of the kinetics of reaction between crystal violet and hydroxide ion, showed that the DCC absorbance parameter for the green component, i.e. $A(sG)$, was related directly to the concentration of the dye, crystal violet, CV, where:

\begin{equation}
A(sG) = \log(sG_o/sG_{CV})
\end{equation}

and $sG_o$ and $sG_{CV}$ are the digital image 'intensity' values for the sG component derived from the photograph of the reaction solution in the absence and presence of the CV, respectively; note: $sG_o$ is usually taken to be equal to 255 (or 1). In contrast, in their use of DCC to quantify the level of HE4 in urine, Wang \textit{et al.} \cite{3} showed that the DCC transmittance for the red component of the digital image, i.e. $T(sR)$, was related directly to the concentration of HE4, via the expression:

\begin{equation}
1 - T(sR) = K[HE4]
\end{equation}

where, $T(sR) = sR_{HE4}/sR_o$ and $sR_o$ and $sR_{HE4}$ are the intensity values for the sR components of the digital image of the ELISA indicator in the absence and presence of the HE4, respectively. The parameter, $1 - T(sR)$, will be referred to here as the apparent fraction of light absorbed by the system. Since the standard red component is not absorbed in absence of HE4, once again it is assumed that the value of $sR_o = 255$ (or 1 if in \textit{fractional format}).

Finally, Araki \textit{et al.} \cite{6}, in their use of DCC to determine the UV dose received by the indicator, employed the $sRGB$ data, derived from photographic images of the indicator, to calculate the values of $L$, $a$ and $b$, in the \textit{Lab} colour scale, and then determine the change in colour between a UV exposed and non-exposed indicator, i.e. $\Delta E$, where:
\[ \Delta E = \left[ (L_o - L_x)^2 + (a_o - a_x)^2 + (b_o - b_x)^2 \right]^{1/2} \]

(3)

Where the subscripts 'o' and x' refer to the values of L, a and b values derived from the images of the non-exposed and UV-exposed indicator, respectively, where the value \(L_o\), \(a_o\) and \(b_o\) were assumed to be 1, 0 and 0, respectively.

This paper seeks to identify which of the above three digital image-based parameters, i.e. \(A(sRGB)\), \(1-T(sRGB)\) and \(\Delta E\), is best at providing a linear correlation with real absorbance values, as measured using UV/Vis spectrophotometry, at a series of wavelengths that span the visible solar spectrum. Once identified, this DCC analysis best method is combined with digital image recording and sRGB calculations, using a mobile phone and App, respectively, to probe the responses of three different known optical sensor systems to see if it is able to generate the same analytical information as that gleaned from a UV/Vis spectrophotometric analysis of the same system.

**Experimental**

**Materials**

Unless stated otherwise, all chemicals were purchased from Sigma Aldrich and used as received. The Activ™ self-cleaning glass was a gift from Pilkington Glass. All aqueous solutions we made up with double-distilled, deionised water. All gases were purchased from BOC.

The phenol red (PR) CO2-sensitive plastic polymer film was prepared as described previously [18], using PR instead of 8-hydroxyppyrene-1,3,6-trisulfonic acid trisodium salt (HPTS) as the pH-sensitive dye. Thus, 0.2 g of PR were fully dissolved in a mixture of 3.1 ml of 40% tetrabutylammonium hydroxide, TBAH, aqueous solution and 100 ml of ethanol, after which 2 g of hydrophilic silica were added, and the dispersion stirred for 2.5 h. The final purple powdered form of the PR-TBAH-SiO2 pigment was then obtained via spray-drying the dispersion using a Buchi B-290 spray dryer. The PR-TBAH-SiO2 pigment was then mixed with low density polyethylene (LDPE), 5 wt%, and extruded out as a 50 \(\mu\)m thick, 10 cm wide, film using a Rondol Microlab 10 mm twin screw extruder (barrel L/D 25/1). The final purple coloured plastic film changed to a yellow colour upon exposure to 100% CO2, returning to its original purple colour in the absence of CO2, i.e. the colour-changing process was reversible.
The preparation of the resazurin, Rz, ink used in this work is described elsewhere [19], but briefly, 1.33 mg of Rz and 133 mg of glycerol were added to 1 mL of a 1.5 wt% aqueous solution of hydroxyethyl cellulose (HEC), (MW = 250k). The ink was stirred for at least 5 h, to ensure thorough mixing and dissolution of the dye, before use. The Activ™ self-cleaning glass samples were coated with the Rz ink, by securing the glass sample to an impression bed (i.e. a clipboard) and drawing down a ca. 2.5 cm line of the ink placed 3 mm from the top edge of the glass sample. A wire wound rod (a 'K-bar' No. 3 [20]) was used to create the draw down film, the final dry thickness of which was ca. 2.1 µm. The Rz-coated Activ™ sample was then irradiated with UV light (2 mW cm⁻² using a 352 nm broad band UVA black light (BL) lamp, 2 x 15W) and the photocatalysed reduction of the Rz monitored periodically both spectrophotometrically and photographically until no further colour change was observed in the Rz ink, or after a period of 12 min, whichever was the shorter period of time.

The preparation of the oxygen sensitive thionin acetate, Th, ink used in this work was otherwise identical to that of a MB ink described elsewhere [21], and which briefly comprised: 20 mg of thionin acetate, 100 mg of P25 titania and 1 g of glycerol dissolved mixed in with 10 cm³ of a 5 wt.% of hydroxyethyl cellulose (HEC, average Mw: 123k) solution in double distilled deionised water. This ink was sonicated for at least 30 minutes to ensure thorough dissolution of the soluble components and subsequently spin-coated onto a borosilicate cover slip (2.4 mm in diameter and 0.145 mm thick) at a rotation speed of 2000 rpm, to produce a dried Th ink film of thickness ~2.1 µm. The ink film was then ‘activated’ to its colourless, oxygen sensitive form by exposing it to UVA irradiation (typical irradiance, 2 mW cm⁻², using a 352 nm broad band UVA BL lamp, 2 x 15W)) for, typically, 20 s. The oxygen driven recovery of the leuco-thionin to the blue coloured thionin was monitored as a function of time, t, by UV-vis spectrophotometry and digital photography.

Methods

All UV/Vis spectra were recorded using a Cary 60 UV/Vis spectrophotometer. All digital images were recorded using the digital camera (12-megapixel) on a 7+ iPhone. All digital images were analysed using either the ColorMeter App [12], or the free ImageJ (v 1.51d) software [15], both yielded the same non-linear values, sR', sG' and sB', which were subsequently processed as described in the text.
**Simulated absorption spectra and determination of sRGB and Lab values**

A very simple simulation of the UV/Vis absorption spectrum of an absorbing species, D, which has a wavelength of maximum absorption, $\lambda_{\text{max}}$, can be generated using the following expression:

$$A_\lambda = A_0 \exp\left[-\left(\frac{\lambda - \lambda_{\text{max}}}{0.6 \times \text{FWHM}}\right)^2\right]$$

(4)

where $A_\lambda$ and $A_0$ are the absorbances due to D at $\lambda$ and $\lambda_{\text{max}}$, respectively, and FWHM is full width at half maximum of the absorption band, set at 50 nm. Note that according to Beer’s law, $A_0$ is proportional to the concentration of D, [D], and can be varied as required. Thus, figure 1 illustrates the simulated absorption spectra for a series of simulated dyes, D, with $\lambda_{\text{max}}$ values set at those associated with the rainbow colours of the solar spectrum, i.e. red, orange, yellow, green, cyan, blue violet, with, in all cases, $A_0$ set at 1.

---

**Figure 1:** Absorption spectra of seven simulated dyes each absorbing at their $\lambda_{\text{max}}$ values the primary rainbow colours, red, orange, yellow, green, cyan, blue and indigo. Each spectrum was calculated using eqn(4) with $A_0 = 1$.

Knowledge of the absorption spectrum of any light-absorbing species allows its linear sRGB values to be calculated and its coloured defined, via the three tristimulus values, $X$, $Y$ and $Z$, which can be calculated using the following formulae [10]:

...
\[ X = \frac{\sum_{\lambda} T(\lambda)S(\lambda)x(\lambda)}{\sum_{\lambda} S(\lambda)y(\lambda)} \]  

(5)

\[ Y = \frac{\sum_{\lambda} T(\lambda)S(\lambda)y(\lambda)}{\sum_{\lambda} S(\lambda)y(\lambda)} \]  

(6)

\[ Z = \frac{\sum_{\lambda} T(\lambda)S(\lambda)z(\lambda)}{\sum_{\lambda} S(\lambda)y(\lambda)} \]  

(7)

where \( T(\lambda) \) is the transmittance (i.e. \( 10^{-A(\lambda)} \)) of the simulated dye, \( S(\lambda) \) is the spectral power of a standard illuminant (here assumed to be daylight and usually referred to as D_65), and \( x(\lambda) \), \( y(\lambda) \) and \( z(\lambda) \) are the two degree standard colour matching functions (CMFs), which are a consequence of the three different cone responses of the eye. Tables of \( S(\lambda) \) for D_65 and \( x(\lambda) \), \( y(\lambda) \) and \( z(\lambda) \) are readily available from the literature [22] and a typical set used here are illustrated in figure 2, and also contained in the 'S1.xls' spread sheet in the supplementary information.
Figure 2: Plots of the known colour matching functions, i.e. $x(\lambda)$, $y(\lambda)$ and $z(\lambda)$ for a 2° standard observer and the $S(\lambda)$ relative spectral power of a standard (D$_{65}$, i.e. daylight) illuminant as a function of wavelength, $\lambda$ [20].

Since the value of $A_\lambda$ at any wavelength, $\lambda$, for any of the simulated dyes illustrated in figure 1, can be calculated using eqn (4), given a knowledge of $\lambda_{\text{max}}$, it follows that each simulated dye absorption spectrum depicted in figure 1, can be defined by a set of tristimulus values, $X$, $Y$ and $Z$. These, in turn, can be converted to $sR$, $sG$ and $sB$ values using the following matrix transformation equation [10]:

$$\begin{bmatrix} sR \\ sG \\ sB \end{bmatrix} = \begin{bmatrix} 3.2410 & -1.5374 & -0.4986 \\ -0.9692 & 1.8760 & 0.0416 \\ 0.0556 & -0.2040 & 1.0570 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

(8)

The above process generates linear $sR$, $sG$ and $sB$ fractional values in the range 0-1, however, it more usual to convert them to the 24 bit sRGB code, $[sR \ sG \ sB]$, where $[0 \ 0 \ 0]$ is black and $[255 \ 255 \ 255]$ is white. Usually this means multiplying each fractional value by 255 and rounding to nearest whole number, with the caveat that if any fractional value is $< 0$, then a value of zero is returned and if any is $> 1$, a value of 255 is returned [10].
Alternatively, the tristimulus values, \(X\), \(Y\) and \(Z\), can be converted to \(Lab\) values using the following equations [6]:

\[
L^* = 116f(Y/Y_n) - 16
\]

\[
a^* = 500[f(X/X_n) - f(Y/Y_n)]
\]

\[
b^* = 200[f(Y/Y_n) - f(Z/Z_n)]
\]

Where

\[
f(t) = \begin{cases} t^{1/3} & \text{if } t > \left(\frac{6}{29}\right)^3 \\ \frac{1}{3} \left(\frac{29}{6}\right)^2 t + \frac{4}{29} & \text{otherwise} \end{cases}
\]

Where, for any simulated dye, \(X_n\), \(Y_n\) and \(Z_n\) are the values of \(X\), \(Y\) and \(Z\), calculated using eqns (5-7), respectively, but with \(T(\lambda)\) set \textbf{always} to be 1. Thus, in this work, it is found that: \(X_n = 95.047\), \(Y_n = 100.000\), \(Z_n = 108.883\) using the D65 Illuminant.

Table 1 lists the: (i) \(X\), \(Y\) and \(Z\), (ii) \(sR\), \(sG\) and \(sB\) and (iii) \(Lab\) and \(\Delta E\) values calculated for each of the absorption spectra illustrated in figure 1, using equations (5 – 7), (8) and (9) and (3), respectively. In table 1, the colour border used round this data, i.e. (i) – (iii) is how each simulated dye with a maximum absorbance, \(A_0\) = 1 would appear, i.e. as the complimentary colour to that which it is absorbing.

An example spreadsheet, highlighting the calculations involved in the determination of the (i) – (iii) values reported in Table 1 for the yellow-absorbing, i.e. \(\lambda_{max} = 575\) nm, simulated dye is given in the 'S2.xls' spreadsheet in the supplementary information. Note: in all \(\Delta E\) value calculations, all colour changes are with reference to white light, for which the values of: \(L_0\), \(a_0\) and \(b_0\) are: 100, 0 and 0, respectively.
Table 1: Spectral and calculated s(RGB), Lab and ΔE characteristics of seven simulated dyes spanning the solar spectrum

<table>
<thead>
<tr>
<th>Colour</th>
<th>Violet</th>
<th>Blue</th>
<th>Cyan</th>
<th>Green</th>
<th>Yellow</th>
<th>Orange</th>
<th>Red</th>
</tr>
</thead>
<tbody>
<tr>
<td>λ\text{max} (nm)</td>
<td>410</td>
<td>470</td>
<td>495</td>
<td>530</td>
<td>575</td>
<td>590</td>
<td>650</td>
</tr>
<tr>
<td>[X,Y,Z]</td>
<td>[0.88,0.99,0.74]</td>
<td>[0.83,0.90,0.37]</td>
<td>[0.87,0.77,0.69]</td>
<td>[0.80,0.54,1]</td>
<td>[0.53,0.52,1.1]</td>
<td>[0.49,0.60,1.1]</td>
<td>[0.76,0.92,1.1]</td>
</tr>
<tr>
<td>sRGB</td>
<td>[244,255,160]</td>
<td>[255,229,65]</td>
<td>[255,158,159]</td>
<td>[255,71,255]</td>
<td>[94,130,255]</td>
<td>[31,177,255]</td>
<td>[128,255,255]</td>
</tr>
<tr>
<td>Lab</td>
<td>[97,-12,24]</td>
<td>[95,-5,54]</td>
<td>[97,29,12]</td>
<td>[93,65,-33]</td>
<td>[79,9,-39]</td>
<td>[77,-21,-31]</td>
<td>[92,-22,-6]</td>
</tr>
<tr>
<td>ΔE*</td>
<td>27</td>
<td>54</td>
<td>31</td>
<td>73</td>
<td>45</td>
<td>44</td>
<td>24</td>
</tr>
<tr>
<td>PCC**</td>
<td>blue</td>
<td>blue</td>
<td>green</td>
<td>green</td>
<td>red</td>
<td>red</td>
<td>red</td>
</tr>
</tbody>
</table>

*: Reference white point is RGB (255, 255, 255) or Lab (100, 0, 0), where ΔE = 0.
**: Primary colour component.
**Correlation studies**

The previous section outlines how it is possible to use the associated UV/Vis absorption spectrum to calculate the $s_R$, $s_G$ and $s_B$ and $Lab$ and $\Delta E$ values for any of the simulated dyes solutions illustrated in figure 1. Now, for all the simulated dyes illustrated in figure 1, the maximum absorption at $\lambda_{max}$, i.e. $A_0$, was set at 1. However, the same process can also be used to calculate the $s_R$, $s_G$ and $s_B$ and $Lab$ and $\Delta E$ values for any of the simulated dyes for any value of $A_0$, i.e. at any dye concentration. Thus, in this work $A_0$ was varied from 0-1, in steps of 0.05, for each of the simulated dyes to simulate a range of different dye concentrations, and in each case values for $s_R$, $s_G$ and $s_B$ and $Lab$ and $\Delta E$, were calculated using the same procedure as described in the previous section. Spectra for the simulated dyes for which $A_0 > 1$ were not studied for, as we shall see, this is too high for DCC to produce any likely correlation with any measured UV/Vis absorbance. In the case of the $s_R$, $s_G$ and $s_B$ data generated for each simulated dye, usually one of the colours, i.e. $R$, $G$ or $B$, varies to a greater extent compared to the other two over the $A_0$ range 0-1. For example, for the yellow-absorbing dye illustrated in figure 1, with $\lambda_{max} = 575$ nm, a brief inspection of the variation of the calculated values of $s_R$, $s_G$ and $s_B$ as a function of $A_0$, illustrated in figure 3, reveals that the red component is most affected by the change of $A_0$ from 0-1. In all this work, for any light absorbing system we shall refer to this component, i.e. the colour component which changes most markedly with change in $A_0$ as the 'primary colour component' or 'PCC' for short. Note: as a rough guide, the PCC is the complementary colour to that of the analytical system under test. Thus, the PCC is red, green or blue for a coloured system that appears approximately cyan, magenta or yellow, respectively [23].
Figure 3: Plots of $s_R$ (red line), $s_G$ (green line), and $s_B$ (blue line), values determined for the yellow-absorbing simulated dye as a function of absorbance at $\lambda_{\text{max}}$, i.e. $A_o$, from which it is clear that the red component varies most significantly as the value of $A_o$ is increased from 0 to 1, in steps of 0.05, whilst, in contrast, the blue component remains unchanged at all values of $A_o$.

As a consequence, since red is the PCC for the yellow absorbing dye (see figure 3), only the red component data were used to calculate values for $A(s_R)$ and $1-T(s_R)$ for the yellow-absorbing simulated dye, using the appropriate versions of equations (1) and (2), respectively, as a function of $A_o$. In addition, the $s_R$, $s_G$ and $s_B$ data in figure 3, for the yellow-absorbing simulated dye, was used to calculate values for $Lab$, and so $\Delta E$, also as a function of $A_o$ which was varied over the range 0-1. Plots of these three different data sets, i.e. $A(s_R)$, $1-T(s_R)$and $\Delta E$ vs $A_o$, for the yellow simulated dye are illustrated in figure 4 from which it appears that the absorbance-like parameter based on the $s_R$ values, i.e. $A(s_R)$, provides the best linear correlation, of the three plots, with $A_o$, and this observation is supported by the near unity value for the square of the correlation coefficient for the line of best fit (i.e. $r^2 = 0.9941$). It is also clear that all three parameters show increasing deviation from linearity as the value of is $A_o$ increased and that even $A(s_R)$ shows clear signs of deviating significantly at $A_o$ values $>1$. This was found to be true for all the simulated dyes tested and so the correlation study was limited to a variation of $A_o$ from 0 to 1, as noted earlier.
Figure 4: Plots of $A(s_R)$ (black dots), $1-T(s_R)$ (red dots) and $\Delta E$ (blue dots) as a function of $A_o$ for the yellow-absorbing simulated dye (see figure 1) calculated using the $s_R$, $s_G$ and $s_B$ values illustrated in figure 3. The line of best fit (broken line) for the plot of $A(s_R)$ vs. $A_o$ yields a correlation coefficient, $r^2$, 0.9941.

The same procedure was applied to all the simulated dyes illustrated in figure 1 and in each case the PCC was identified (see Table 1) and the data associated with the PCC used to generate plots of: $A(s_R)$, $1-T(s_R)$ and $\Delta E$ as a function of $A_o$ over the $A_o$ range of 0-1. The square of the correlation coefficient was determined for each of these correlation plots and the results of this work are plotted as a function of $\lambda_{max}$ in figure 5 for the different simulated dyes. A brief inspection of this plot of correlation coefficient data reveals that, as for the yellow-absorbing dye in figure 4, the absorbance-like parameter, $A(s_R$, $s_G$ or $s_B)$, correlates linearly much more closely with $A_o$, than the other two functions, $1-T(s_R$, $s_G$ or $s_B)$ and $\Delta E$. 
Figure 5: Plots of squares of correlation coefficients, $r^2$ as a function of $\lambda_{\text{max}}$ for the seven simulated dyes listed in table 1. The individual $r^2$ values themselves were derived from plots of the sRGB PCC data for each of the seven dyes in the form of: $A(sR, sG \text{ or } sB)$ (black line), $1-T(sR, sG \text{ or } sB)$ (red line) or $\Delta E$ (blue line) vs. $A_o$.

These results imply that values for the absorbance-like parameter, i.e. $A(sR, G \text{ or } B)$, determined from digital photographic data, i.e. $sR, sG$ or $sB$ values, can be used, instead of absorbance values determined using UV/Vis spectrophotometry, as a measure of concentration of the light absorbing species. This is a useful observation given that the cost of DCC is low and the technique very portable, unlike UV/Vis spectroscopy and, also – once in place - the process is simple to effect. In order to test the above hypothesis, derived from studies of simulated dyes, three, well-established colour-based sensors were studied using both the conventional, and costly, UV/Vis spectrophotometric technique and the very inexpensive, increasingly popular, simple method of DCC, using a digital mobile phone camera and a RGB measuring App.
Application of DCC to established optical sensor systems

(1) CO₂-sensitive indicators

A large number of CO₂-sensitive, colour-based indicators have been developed and commercialised for various applications, including correct tracheal intubation [24] and environmental monitoring in air and water [25-28]. In most cases the colour changing process is due to the following equilibrium reaction:

\[ \text{D}^- + \text{H}_2\text{O} + \text{CO}_2 \rightleftharpoons \text{DH} + \text{HCO}_3^- \]  \hspace{1cm} (13)

where D⁻ and DH are the deprotonated and protonated forms, respectively, of a pH sensitive dye, such as phenol red, PR. It follows that in the presence of an excess of bicarbonate, the concentrations of D⁻ and DH are related to the ambient level of CO₂, i.e. via an expression of the form:

\[ \frac{[\text{DH}]}{[D^-]} = K \cdot \%\text{CO}_2 \]  \hspace{1cm} (14)

Where, [DH] and [D⁻] are the concentrations of the protonated and deprotonated forms of the pH dye, respectively, and K is the proportionality constant which provides a measure of the sensitivity of the sensor towards CO₂. If, as is usually the case, the absorbance of the indicator is measured at a wavelength where only D⁻ absorbs, which is usually λ_max for D⁻, i.e. A(D⁻), then, according to eqn (14) and Beer’s law, A(D⁻) will decrease as %CO₂ is increased. It also follows that a plot of 1/A(D⁻) vs %CO₂ will yield a straight line with a gradient, K [29, 30]. However, a much simpler, although more approximate method for assessing the value of K is to measure the %CO₂ necessary to create equal concentration of [DH] and [D⁻], i.e. %CO₂(S = ½), since it is equal to the reciprocal of K. Note: at %CO₂(S = ½), A(D⁻) = A(D⁻)_o/2, where A(D⁻)_o is the initial absorbance of the indicator [31].

In this work the optical responses of a typical PR-based CO₂-sensitive plastic film sensor, towards different levels of CO₂, were measured using both a UV/Vis spectrophotometer and a mobile phone digital camera and the results of this work are illustrated in figure 6 [32].
Figure 6: UV/Vis absorption spectra and digital photographic images recorded for a PR-based CO₂ sensitive plastic film as a function of increasing levels of %CO₂ in the gas phase.

The UV/Vis absorbance data in figure 6 is for the PR film at the $\lambda_{\text{max}}$ for its deprotonated form (582 nm) was then plotted as a function of %CO₂ as illustrated in figure 7, from which a value for %CO₂($S = \frac{1}{2}$), and so $K$, were gleaned for the PR CO₂ indicator film. Similarly, the ColorMeter App on the mobile phone was used to analyse each of the digital photographs taken of the film as a function of %CO₂ and illustrated in figure 6. The sRGB values extracted using the App are gamma corrected, non-linear parameters, i.e. $sR'$, $sG'$ and $sB'$ values. In this, and all the other indicators described in this section, the PCC was red and the conversion from the App measured $sR'$ non-linear values associated with the digital photographs illustrated in figure 6, to their linear, $sR$, counterparts used the following function:

$$\text{If } sR' \leq 0.0405, \text{ then } sR = 12.92. R', \text{ otherwise } sR = \left(\frac{(sR' + 0.055)}{1.055}\right)^{2.4}$$

(15)

where $sR'$ and $sR$ are in their fractional (i.e. 0-1) forms, rather than their more usual 8 bit (0-255) forms. Once $sR'$ and $sR$ were converted to their linear values, using eqn (15), then the value of $A(sR)$ associated with each of the indicator photographs illustrated in figure 6 was determined and a plot constructed of $A(sR)$ vs %CO₂, which is illustrated in figure 7. As an
example, $s_{RGB}$ analysis (using the App) of the image of the CO$_2$ indicator at 2% CO$_2$ reveals a value of $sR'$ of 0.59 (or 150 in 8 bit form), which translates to a value of 0.30 (or 77 in 8 bit form) for $sR$, calculated using eqn (15), and a value of 0.52 for $A(sR)$, based on eqn (1), assuming $sR_0 = 255$.

A quick comparison of the two plots in *figure 7*, namely absorbance, $A_{582}$, (at $\lambda_{\text{max}}$ PR; i.e. 582 nm, measured spectrophotometrically and taken from the spectral changes in figure 6) vs %CO$_2$ and $A(sR)$ (calculated as in eqn (1) using $sR$ values derived from the digital images in figure 6) vs %CO$_2$ reveals that they are near identical in shape, implying –as predicted in the first section – that in practice spectrophotometric absorbance, $A_{582}$, and the apparent absorbance parameter, $A(sR)$, based on digital image analysis, are linearly correlated in this system. As you would expect, given the linear correlation between $A_{582}$ and the DCC parameter, $A(sR)$, both plots of $A_{582}$ and $A(sR)$ vs %CO$_2$ yielded the same value of 2.7 % for %CO$_2(S = \frac{1}{2})$, as illustrated in figure 6. Thus, the solid line in figure 7 is based on eqn (14), assuming a value of $K = 0.37 \%^{-1}$, which predicts the value of %CO$_2(S = \frac{1}{2}) = 2.7\%$.

![Figure 7](image.png)

**Figure 7**: Plots of: (i) absorbance (at $\lambda_{\text{max}}$ PR; measured spectrophotometrically and taken from the spectral changes in figure 6) vs %CO$_2$ (black data points) and $A(sR)$ (calculated as in eqn (1) using $sR$ values derived from the digital images in figure 6) vs %CO$_2$ (red data points). The broken line identifies the values of $A_{592}$ and $A(sR)$, when the indicator is exposed to 100% CO$_2$, so that all the PR is in its protonated form. The solid line was generated using eqn (14), with $K = 0.37 \%^{-1}$, which yields a value of %CO$_2(S = \frac{1}{2})$ of 2.7%,
(2) Photocatalyst activity sensitive indicators

In recent years a number of new, so called 'self-cleaning' architectural materials have been developed in the form of glass (e.g. Activ® from Pilkington Glass) [33], paint (e.g. Climisan® from STO) [34], concrete (e.g. TX Active® from Italcementi) [35] and tiles (e.g. Hydrotect® from TOTO) [36]. In all cases the active ingredient is photoactive TiO₂, which absorbs UV light and is able to effect the complete mineralisation of most organic contaminants which have deposited onto its surface, i.e.

\[
\text{TiO}_2 + \text{Pollutant} + \text{O}_2 \overset{\text{UV}}{\longrightarrow} \text{minerals (such as: H}_2\text{O, CO}_2 \text{ and acids)}
\]

The above process is an example of semiconductor photocatalysis [37]. There are a growing number of commercial and research photocatalytic materials and so there is a real need for methods to assess the photocatalytic activity. As a consequence a number of international standard testing methods have been developed for this purpose, however most are slow (usually take hours) and are laboratory based, and so not conducive to testing samples in situ [38]. Recently a new colourimetric method of assessing photocatalytic activity has been reported [39, 40] based the photocatalysed reduction of a blue dye, resazurin, Rz, to a pink coloured product, resorufin, Rf, via the following photocatalytic reaction:

\[
\text{TiO}_2 + \text{glycerol} + \text{Rz} \overset{\text{UV}}{\longrightarrow} \text{glyceraldehyde} + \text{Rf}
\]

The rate of photo-induced change in colour of the Rz ink film is proportional to the activity of the underlying photocatalytic material under test. The test is easy to use, fast, i.e. usually < 10 min, and can be used in the in situ assessment of photocatalytic materials [41, 42]. In addition, it is now the basis of a recent ISO (DIS 21066) [43], in which the time taken for the
Rz to lose 90% of its colour, $ttb(90)$, is measured, and taken as an inversely proportional measure of the activity of the photocatalyst.

Here the Rz ink was used to probe the activity of a piece of Activ® self-cleaning glass using both a UV/Vis spectrophotometer and a mobile phone digital camera to monitor the change in colour of the Rz ink film (blue to pink) as a function of UV irradiation time and the results of this work are illustrated in figure 8.

![Image](image.png)

**Figure 8:** UV/Vis absorption spectra and digital photographic images recorded for a Rz ink on a piece of Activ® glass as a function of UV irradiation time.

The parameter $ttb(90)$ can be determined for the Activ® glass by plotting the change in absorbance due to the Rz at its $\lambda_{max} = 609$ nm, i.e. $A_{609}$, as a function of irradiation time, as illustrated in figure 9, where $\Delta A_{t=0}$ is the overall change in $A_{609}$ as the indicator turns from blue to pink due to reaction (17), and $ttb(90)$ is the UV irradiation time taken for $\Delta A = 0.9$. $\Delta A_{t=0}$. Using the same data manipulation process as described in the previous section, the photographic images in figure 8 of the Rz ink film were used to generated the plot of $A(sR)$ vs UV irradiation time, also illustrated in Figure 9. As before, a quick comparison of the two
plots in figure 9, namely absorbance, $A_{609}$ (at $\lambda_{\text{max}}$ Rz, i.e. 609 nm; measured spectrophotometrically and taken from the spectral changes in figure 8) and $A(sR)$ (calculated as in eqn (1) using $sR$ values derived from the digital images in figure 8) vs UV irradiation time reveals that the spectrophotometric absorbance and $A(sR)$ data are linearly correlated, as the data points lie on a common line. As a consequence the two data sets generate the same value for $ttb(90)$, namely, ca. 8.6 min.

Figure 9: Plots of: (i) absorbance (at $\lambda_{\text{max}}$ Rz; measured spectrophotometrically and taken from the spectral changes in figure 8) vs %CO$_2$ (black data points) and $A(sR)$ (calculated as in eqn (1) using $sR$ values derived from the digital images in figure 8) vs UV irradiation time (red data points). Both data sets identify the same value for $ttb(90)$, namely 8.6 min.

(3) UV-activated, O$_2$-sensitive indicators

Probably the most commonly analysed chemical species is O$_2$, which is not surprising given its key role in many biochemical and chemical processes. In terms of indicators the detection of oxygen is dominated both commercially and in the academic literature by luminescence quenching [44]. Examples of commercial O$_2$ indicators based on this technology include: Oxydot® from oxysese [45], Spot SP® series from PreSense [46], OpTech® O$_2$ from Mocon [47], RedEye® oxygen sensor patches from OceanOptics [48]. In contrast, there are few colour-based O$_2$ indicators [49], although this group has recently developed a UV-activated colour-based oxygen indicator that utilises an ink containing a semiconductor photocatalyst (usually TiO$_2$), a highly coloured redox dye, usually a thiazine
dye such as methylene blue, MB or thionine, Th, and a sacrificial electron donor, usually glycerol. Upon an initial illumination with UV the ink is 'activated' – i.e. rendered O₂-sensitive, via the following photocatalytic process:

\[
\text{TiO}_2 \quad \text{glycerol + MB} \rightarrow \text{glyceraldehyde + LMB} \quad \text{UV} \quad (18)
\]

since the reduced form of MB, i.e. \textit{leuco}-methylene blue, LMB, reacts readily with O₂, via:

\[
\text{LMB} + \text{O}_2 \rightarrow \text{MB} + \text{H}_2\text{O} \quad (19)
\]

Thus, upon exposure to a short, intense burst of UV illumination the initially blue coloured ink is bleached to LMB and stays bleached until and unless O₂ is present, whereupon it regains its original blue colour at a rate, or half-life, \(t(50)\), that depends upon the ambient level of O₂ \[50\]. This indicator technology has been used commercially to identify O₂ ingress in packaged food \[51\].

In this study, a typical TiO₂/thionine/glycerol ink was used to coat a glass cover slip and, after exposure to a burst of UV light (2 mW cm⁻² for 20 s from 2x15 W 352 nm BL lamps) the recovery of its original colour in air (21% O₂) was monitored both spectrophotometrically and photographically as a function of 'dark' time (i.e. time after the initial exposure to UV radiation) and the results of this work are illustrated in figure 10.
Figure 10: Recovery in air of a photocatalytically-reduced TiO$_2$/thionine/glycerol ink film monitored both spectrophotometrically and using a digital mobile phone camera. The change in absorbance spectrum of the ink film recorded every 2 mins is illustrated here.

The parameter $t(50)$ in air can be determined for the UV-activated TiO$_2$/thionine/glycerol ink film by plotting the change in absorbance due to the Th in the ink at its $\lambda_{\text{max}} = 609$ nm, i.e. $A_{609}$, as a function of 'dark' time, as illustrated in figure 11, where $\Delta A_{t=0}$ is the overall change in $A_{609}$ as the indicator turns from colourless to blue due to reaction (19), and $t(50)$ is the time taken for $\Delta A = 0.5 \times \Delta A_{t=0}$. Using the same data manipulation process as described in the previous section, the photographic images in figure 10 of the TiO$_2$/thionine/glycerol ink film were used to generated the plot of $A(sR)$ vs 'dark' time, also illustrated in Figure 11. As before, a quick comparison of the two plots in figure 11, namely absorbance, $\text{Abs}_{609}$ (at $\lambda_{\text{max}}$ for Th, i.e. 609 nm; measured spectrophotometrically and taken from the spectral changes in figure 10 and $A(sR)$ (calculated as in eqn (1) using $sR$ values derived from the digital images in figure 10) vs UV irradiation time reveals that the spectrophotometric absorbance and $A(sR)$ data are linearly correlated, as the data points lie on a common line.
As a consequence the two data sets generate the same value for $t(50)$, namely, 4.6 min. Other work shows that $t(50)$ is inversely proportion to %O$_2$ [47].

**Figure 11:** Plots of: (i) absorbance (at $\lambda_{max}$ Th; measured spectrophotometrically and taken from the spectral changes in figure 9) vs %CO$_2$ (black data points) and A(sR) (calculated as in eqn (1) using sR values derived from the digital images in figure 9) vs 'dark' time (red data points). Both data sets identify the same value for $t(50)$, namely 4.6 min.
Conclusions

The absorption spectrum of a simple simulated dye, with an absorbance, $A_0$, at $\lambda_{\text{max}}$ is described by eqn (4). This equation allows the creation of seven absorption spectra, with $A_0 = 1$, that span the visible spectrum. These spectra can be converted into $sRGB$ values, see Table 1, which in turn can be used to calculate values for the apparent absorbance, $A(sRGB)$, apparent fraction of absorbed light, $1-T(sRGB)$, where $T$ is the apparent transmittance and (iii) colour difference, $\Delta E$. The latter are popular parameters in digital colour colourimetry, DCC. For each dye, one of the $sRGB$ colour parameters, the principle colour component, PCC, varies more than the other two as $A_0$ is varied from 0 to 1 (see Table 1) and it is this colour that is used to probe the degree of correlation between actual absorbance ($A_0$) and the three DCC parameters: $A(sRGB)$, $1-T(sRGB)$ and $\Delta E$. For all seven simulated dyes, over the absorbance range 0-1, the apparent absorbance, $A(sRGB)$, correlates better with $A_0$ than the other two DCC parameters. Three real indicators, namely: a CO$_2$ indicator, a photocatalytic activity indicator and an oxygen indicator, were used to test this prediction and in each case the PCC was red. In all three cases the apparent absorbance parameter, $A(sR)$, derived from $sRGB$ analysis of the digital images, was found to be proportional to the real absorbance, as measured using UV/Vis spectrophotometry, and yielded the same key analytical information, i.e. pCO$_2$(S=1/2) = 2.7%, $ttb(90) = 8.6$ min and $t(50) = 4.6$ min. In all this work, digital image information capture required only a mobile phone camera and a colour measuring App, and so is much cheaper and easier to use than most UV/Vis spectrophotometers. Although never as good as UV/Vis spectrophotometry, the widespread use of digital cameras and Apps makes it increasingly likely that the use of DCC in quantitative and, especially semi-quantitative, analysis of colour based indicators will become more common place. This work suggests that in most cases the digital data should be plotted in the form of apparent absorbance $A(sRGB)$, rather than fractional light absorbed, $1-T(sRGB)$, or colour difference, $\Delta E$. The fact that a digital camera can photograph many indicators simultaneously, suggests that it is also ideally suited for multi-analyte analysis, using an array of colourimetric indicators, unlike UV/Vis spectrophotometry.
References


