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Secure Multiple Amplify-and-Forward Relaying with Co-Channel Interference

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Abstract—We investigate the impact of co-channel interference on the security performance of multiple amplify-and-forward (AF) relaying networks, where $N$ intermediate AF relays assist the data transmission from the source to the destination. The relays are corrupted by multiple co-channel interferers, and the information transmitted from the relays to destination can be overheard by the eavesdropper. In order to deal with the interference and wiretap, the best out of $N$ relays is selected for security enhancement. To this end, we derive a novel lower bound on the secrecy outage probability (SOP), which is then utilized to present two best relay selection criteria, based on the instantaneous and statistical channel information of the interfering links. For these criteria and the conventional max-min criterion, we quantify the impact of co-channel interference and relay selection by deriving the lower bound on the SOP. Furthermore, we derive the asymptotic SOP for each criterion, to explicitly reveal the impact of transmit power allocation among interferers on the secrecy performance, which offers valuable insights into practical design. We demonstrate that all selection criteria achieve full secrecy diversity order $N$, while the proposed in this paper two criteria outperform the conventional max-min scheme.

Index Terms—Secure communications, co-channel interference, relay selection, secrecy diversity order.

I. INTRODUCTION

Due to its broadcast nature, wireless transmission may be overhead by eavesdroppers in the network, which brings out the risk of information leakage. To prevent this leakage, secure techniques, such as encryption and physical-layer security (PLS) [1], have been widely investigated in the literature. In the pioneering work by Wyner [2], the classical wiretap model was proposed to analyze the secure communication. Then the study on PLS has been extended over fading channels, such as Rayleigh and Nakagami-$m$ [3]–[6]. In these works, important metrics of secrecy performance, such as secrecy outage probability (SOP) and secrecy capacity, have been studied. To enhance the transmission security for multi-antenna systems, antenna selection technique can be used to exploit the dynamic nature among the multi-antenna fading channels [7].

Relaying technique has attracted increasingly attention in the literature, since it extends the radio coverage and improves the system capacity, without raising the transmit power [8]–[11]. Hence, it is of vital importance to study the PLS in relay networks [12]–[15]. There are two fundamental relaying protocols: amplify-and-forward (AF) and decode-and-forward (DF). For DF-aided relay networks, the system secure communication has been extensively studied, by deriving analytical expressions for the SOP in [16]–[18]. In order to enhance the security for multi-DF relay networks, these works [16]–[18] used relay selection techniques to exploit the dynamic nature among multi-relay fading channels. Compared with DF relaying, it is, however, much more complicated to obtain analytical SOP expressions for AF relay networks, since the received signal-to-noise ratios (SNRs) at the destination and eavesdroppers are represented in complex forms. In order to deal with this issue, the authors in [19] analyzed the intercept probability, which depends on the second-hop relay channels only. However, this probability is just a special case of the SOP, where the target secrecy data rate is set to zero. Furthermore, the authors in [20] investigated the PLS of multiuser multi-AF relay networks, and presented closed-form expressions for the limiting behavior of SOP, assuming a large transmit power.

One of the utmost concerns arising in wireless networks is the existence of co-channel interference, due to the excessive frequency reuse [21]–[25]. In [26], the authors studied a relay network in the presence of co-channel interference and analyzed the effect of interference power distribution1 on the network performance. For multi-AF relay networks with co-channel interference, the relay selection aided by the interfering channel parameters can be used to improve the network transmission performance [27]. Recently, the impact of co-channel interference on the secure communications has received much attention. In [28], the authors studied the PLS of multi-DF relay networks in the presence of co-channel interference, by deriving the analytical and asymptotic SOP expressions. To the best of our knowledge, no prior work

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1As shown in [26], the interference power distribution refers to the transmit power allocation among interferers, for a given total transmit power.
has considered the secure communications of multi-AF relay networks, taking into account the impact of co-channel interference and relay selection.

In this paper, we study the secure communications of multi-AF relay networks in the presence of an eavesdropper, assuming that the \( N \) relays are disturbed by multiple co-channel interferers. To tackle with the co-channel interference and wiretap, relay selection is performed, such that the best relay is chosen to enhance the network security. We study the network secrecy performance by deriving the analytical and asymptotic SOP expressions. The key contributions of this paper are summarized as follows,

- To facilitate the secure performance evaluation, we derive a novel lower bound on the SOP, which is valid for an arbitrary transmit power.
- Besides the traditional max-min criterion, we utilize the newly derived lower bound on the SOP to present two relay selection criteria, based on the instantaneous and statistical channel information of the interfering links, respectively.
- For each criterion, we derive an analytical lower bound on the SOP, in order to investigate the system secrecy performance.
- We present novel asymptotic results for the SOP with high main-to-eavesdropper ratio (MER), which can be efficiently used to determine the factors governing the secrecy performance.
- Based on these asymptotic expressions, we provide key insights into the network secrecy diversity order and the impact of interference power distribution on the network security.

The rest of the paper is organized as follows. Section II introduces the system model of the secure multi-AF relay networks in the presence of co-channel interference. In Section III, we first derive a novel lower bound expression for the SOP, and then we present the relay selection criteria. Section IV provides the analytical lower bound of SOP as well as the asymptotic expression, assuming high value of MER. Simulations and numerical results are presented in Section V to show the impact of co-channel interference and relay selection on the network security. Finally, conclusions are drawn in Section VI.

Notations: The notation \( \mathcal{CN}(0, \sigma^2) \) denotes a circularly symmetric complex Gaussian random variable (RV) with zero mean and variance \( \sigma^2 \). We use \( f_X(\cdot) \) and \( F_X(\cdot) \) to represent the probability density function (PDF) and cumulative density function (CDF) of the RV \( X \), respectively. The function, \( E_1(x) = \int_x^{\infty} \frac{e^{-t}}{t} dt \), is the exponential integral function [29], while \( \text{Pr}[\cdot] \) returns the probability, and \( E[\cdot] \) denotes statistical average.

II. SYSTEM MODEL

Fig. 1 depicts the system model of a two-phase multiple AF relay network with co-channel interference, where the source \( S \) communicates with the destination \( D \) with the help of \( N \) intermediate AF relays, \( \{R_n|1 \leq n \leq N\} \). Apart from the additive white Gaussian noise (AWGN), the relays are corrupted by \( M \) co-channel interferers, \( \{I_m|1 \leq m \leq M\} \). An eavesdropper, \( E \), can overhear the message forwarded from relays, which indicates a great threat to the communication from \( S \) to \( D \). Note that the network secrecy performance becomes worse if multiple eavesdroppers exist in the network, no matter whether the eavesdroppers decode the messages in a colluding or non-colluding manner [20]. However, the relay selection criteria and the secrecy performance analytical framework proposed in this work can be easily extended to the case of multiple eavesdroppers. We assume that \( D \) and \( E \) are disturbed by the AWGN only. A severe shadowing environment is considered, so that there is no direct link from \( S \) to \( D \) or from \( S \) to \( E \). Due to the size limitation, all nodes in the network are equipped with a single antenna. To deal with the wiretap channel and co-channel interference, the best relay, \( R_n \), needs to be selected among \( N \) relays for enhancing the network security. Before presenting the relay selection criterion, we first formulate the two-phase data transmission with co-channel interference at relays.

Suppose that \( R_n \) is selected for data transmission. In the first phase, \( S \) sends signal \( x_S \) to \( R_n \) in co-channel interference environments. The received signal at \( R_n \) is given by

\[
y_{R_n} = \sqrt{P} h_{S,R_n} x_S + \sum_{m=1}^{M} \sqrt{P} h_{I_m,R_n} x_{I_m} + n_R, \tag{1}\n\]

where \( P \) is the transmit power at \( S \), \( h_{S,R_n} \sim \mathcal{CN}(0, \alpha) \) is the channel coefficient of the \( S-R_n \) link, \( P \) and \( x_{I_m} \) are the transmit power and signal of the interferer \( I_m \), \( h_{I_m,R_n} \sim \mathcal{CN}(0, \epsilon) \) is the channel coefficient of the interfering \( I_m-R_n \) link, and \( n_R \sim \mathcal{CN}(0, N_o) \) is the AWGN at \( R_n \). As per the rules of AF relaying, \( R_n \) amplifies \( y_{R_n} \) using the factor

\[
\kappa_n = \frac{P}{\sqrt{\|h_{S,R_n}\|^2 + \sum_{m=1}^{M} |h_{I_m,R_n}|^2 + N_o}}, \tag{2}\n\]

![Fig. 1. A network consisting of multiple AF relays with co-channel interference and an eavesdropper.](image-url)
The received signals at D and E from $R_n$ in the second phase can be respectively written as

\[ y_D = h_{R_n,D} \kappa_n y_D + n_D, \]
\[ y_E = h_{R_n,E} \kappa_n y_E + n_E, \]

where $h_{R_n,D} \sim CN(0, \beta_1)$ and $h_{R_n,E} \sim CN(0, \beta_2)$ denote the channel coefficients of the $R_n-D$ and $R_n-E$ links, respectively, and $n_D \sim CN(0, N_0)$ and $n_E \sim CN(0, N_0)$ are the AWGN at D and E, respectively. Note that D and E only receive signals, but not transmit. Hence, there is no channel link between D and E. Using (1)–(4), the end-to-end signal-to-interference-plus-noise ratios (SINRs) at D and E can be written as

\[ \gamma_n^D = \frac{\hat{P}_{u_n}}{1 + \sum_{m=1}^{M} \hat{P}_{l_m} w_{mn}} \tilde{P}_{v_{1n}}, \]
\[ \gamma_n^E = \frac{\hat{P}_{u_n}}{1 + \sum_{m=1}^{M} \hat{P}_{l_m} w_{mn}} \tilde{P}_{v_{2n}}, \]

where $\hat{P} = P/N_0$ and $\hat{P}_{l_m} = P_{l_m}/N_0$ denote the average SNR at the source and interferer $I_m$, respectively. For the simplification of notation, let us denote $u_n = |h_{S,R_n}|^2$, $v_{1n} = |h_{R_n,D}|^2$, $v_{2n} = |h_{R_n,E}|^2$, and $w_{mn} = |h_{I_m,R_n}|^2$ as the associated channel gains.

The SOP with $R_n$ is defined as the probability that the difference of the data rate between the main and eavesdropper links falls below a given threshold $R_s$, which is formulated as

\[ P_{n,\text{out}} = \Pr \left[ \frac{1}{2} \log_2 (1 + \gamma_n^D) - \frac{1}{2} \log_2 (1 + \gamma_n^E) < R_s \right], \]
\[ = \Pr \left[ 1 + \frac{\gamma_n^D}{1 + \gamma_n^E} < \gamma_s \right], \]

where the term $\frac{1}{2}$ in (7) is due to the two-phase data transmission, and $\gamma_s = 2^{2R_s}$ denotes the secrecy SNR threshold.

III. RELAY SELECTION

A. A Novel Lower Bound on the SOP

As observed from (5) and (6), the received SINRs, $\gamma_n^D$ and $\gamma_n^E$, share two common RVs, namely, $u_n$ and $w_{mn}$. As such, it is not trivial to derive an exact analytical expression for the SOP, since $\gamma_n^D$ and $\gamma_n^E$ are correlated RVs. To deal with this issue, we note that the authors in [20] presented simplified expressions for $\gamma_n^D$ and $\gamma_n^E$, by assuming large transmit power $P$. However, this is not applicable in practical scenarios, where the terminals are limited powered, e.g., mobile devices or sensor nodes. Next, we derive a novel lower bound on the SOP. We first write $P_{n,\text{out}}$ as

\[ P_{n,\text{out}} = \Pr \left[ 1 + \frac{\hat{P}_{u_n} \tilde{P}_{v_{1n}}}{1 + \hat{P}_{u_n} \tilde{P}_{v_{1n}} + \tilde{P}_{v_{2n}}} < \gamma_s \right], \]

where $z_n = \sum_{m=1}^{M} \tilde{P}_{l_m} w_{mn}$. Based on the following equalities

\[ 1 + \frac{\hat{P}_{u_n} \tilde{P}_{v_{1n}}}{1 + \hat{P}_{u_n} \tilde{P}_{v_{1n}} + \tilde{P}_{v_{2n}}} = \frac{(1 + \hat{P}_{u_n} \tilde{P}_{v_{1n}})(1 + \tilde{P}_{v_{2n}})}{1 + \hat{P}_{u_n} \tilde{P}_{v_{1n}} + \tilde{P}_{v_{2n}}}, \]
\[ 1 + \frac{\hat{P}_{u_n} \tilde{P}_{v_{2n}}}{1 + \hat{P}_{u_n} \tilde{P}_{v_{2n}} + \tilde{P}_{v_{2n}}} = \frac{(1 + \hat{P}_{u_n} \tilde{P}_{v_{2n}})(1 + \tilde{P}_{v_{2n}})}{1 + \hat{P}_{u_n} \tilde{P}_{v_{2n}} + \tilde{P}_{v_{2n}}}, \]

we rewrite $P_{n,\text{out}}$ in a more compact form as

\[ P_{n,\text{out}} = \Pr \left[ (1 + \hat{P}_{v_{1n}})(1 + \hat{P}_{u_n} \tilde{P}_{v_{1n}}) < \gamma_s \right], \]
\[ = \Pr \left[ 1 + \frac{\hat{P}_{u_n} \tilde{P}_{v_{2n}}}{1 + \hat{P}_{u_n} \tilde{P}_{v_{2n}} + \tilde{P}_{v_{2n}}} < \gamma_s \right], \]
\[ = \Pr \left[ \frac{\hat{P}_{u_n} \tilde{P}_{v_{2n}}}{1 + \hat{P}_{u_n} \tilde{P}_{v_{2n}} + \tilde{P}_{v_{2n}}} < \frac{\gamma_s - 1}{\gamma_s} \right]. \]

By applying the inequality$^2$ [30]

\[ \frac{1}{x_1 + x_2} = \frac{x_1 x_2}{x_1 + x_2} \leq \min(x_1, x_2) \]

into (14), a new lower bound expression of $P_{n,\text{out}}$ is obtained as

\[ P_{n,\text{out}}^{LB} = \Pr \left[ \min \left( \frac{\hat{P}_{u_n} \tilde{P}_{v_{1n}}}{\gamma_s}, \frac{1 + \hat{P}_{v_{2n}}}{\gamma_s} \right) < 1 + \hat{P}_{v_{2n}} \right], \]

\[ = \Pr \left[ \min \left( \frac{\hat{P}_{u_n} \tilde{P}_{v_{2n}}}{\gamma_s}, \frac{1 + \hat{P}_{v_{2n}}}{\gamma_s} \right) < \hat{P}_{v_{2n}} + v_{2n} \right], \]

where $\hat{P}_{v_{2n}} = \frac{1}{P}$. It is worthwhile to note that the lower bound derived above can be used for the entire regime of transmit power, thus being more applicable than the method given by [20] for secrecy performance evaluation.

B. Selection Criterion

Relying on the newly derived lower bound on $P_{n,\text{out}}$, in (16), we next present the relay selection criterion to choose the best relay $R_n$, in order to deal with the co-channel interference and wiretap. In practical communication scenarios with passive eavesdroppers, it is hard to acquire the instantaneous channel coefficients of eavesdropper links, and only the channel coefficients of main and interfering links can be utilized to

$^2$Note that the accuracy of the bound in (15) depends on the values of $x_1$ and $x_2$. Specifically, it is quite accurate when $x_1$ is far from $x_2$, while the accuracy becomes worse when $x_1$ is close to $x_2$. 
perform relay selection. From (16), the best relay, $R_{n^*}$, is selected according to

$$n^* = \arg \max_{1 \leq n \leq N} \min \left( \frac{u_n}{(\gamma_s - 1)(1 + z_n)}, \frac{\tilde{P}_r + v_{1n}}{\gamma_s} \right).$$  \hspace{1cm} (17)

According to this criterion, the system needs to know the instantaneous channel coefficients of the interfering links, which can be obtained in some communication systems through dedicated feedback channels from the interferers. However, in some other communication systems without such feedback, the system is only able to know the statistical channel information of interfering links. In this case, the best relay $R_{n^*}$ is selected according to

$$n^* = \arg \max_{1 \leq n \leq N} \min \left( \frac{u_n}{(\gamma_s - 1)(1 + E(z_n))}, \frac{\tilde{P}_r + v_{1n}}{\gamma_s} \right).$$  \hspace{1cm} (18)

Apart from the proposed selection criteria, the conventional max-min criterion can also be used to select the best relay. This criterion is mathematically expressed as

$$n^* = \arg \max_{1 \leq n \leq N} \min(u_n, v_{1n}),$$  \hspace{1cm} (19)

which maximizes the minimum channel gain of the dual-hop main link.

After relay selection, the lower bound on the SOP with selected $R_{n^*}$ is given by

$$p_{\text{out}}^{\text{LB}} = \Pr \left[ \min \left( \frac{u_{n^*}}{(\gamma_s - 1)(1 + z_{n^*})}, \frac{\tilde{P}_r + v_{1n^*}}{\gamma_s} \right) < \tilde{P}_r + v_{2n^*} \right].$$  \hspace{1cm} (20)

For the reader’s convenience, we next refer to the selection criterion in (17), (18) and (19) as criterion I, II, and III, respectively. For these three criteria, we will derive the analytical expression for the SOP and the asymptotic SOP in the high regime of MER.

IV. SECRECY OUTAGE PROBABILITY

A. LOWER BOUND FOR CRITERION I

Based on the selection criterion in (17), we write the lower bound on the SOP as

$$p_{\text{out}}^{\text{LB}} = \Pr \left[ \max_{1 \leq n \leq N} \min \left( \frac{u_n}{(\gamma_s - 1)(1 + z_n)}, \frac{\tilde{P}_r + v_{1n}}{\gamma_s} \right) < \tilde{P}_r + v_{2n^*} \right].$$  \hspace{1cm} (21)

By defining $\theta_n$ as,

$$\theta_n = \min \left( \frac{u_n}{(\gamma_s - 1)(1 + z_n)}, \frac{\tilde{P}_r + v_{1n}}{\gamma_s} \right),$$  \hspace{1cm} (22)

we rewrite $p_{\text{out}}^{\text{LB}}$ as

$$p_{\text{out}}^{\text{LB}} = \Pr \left( \max_{1 \leq n \leq N} \theta_n < \tilde{P}_r + v_{2n^*} \right).$$  \hspace{1cm} (23)

Note that both $u_n$ and $v_{1n}$ follow exponential distribution with mean $\alpha$ and $\beta_1$, respectively. The PDF of $z_n$ is given by [31]

$$f_{z_n}(z) = \sum_{(i,j)} \chi_{i,j} \left( \frac{\epsilon P_{1<\theta}}{j-1} \right)^{j-1} e^{-\frac{z(\epsilon P_{1<\theta})}{j-1}},$$  \hspace{1cm} (24)

where

$$\sum_{(i,j)} = \sum_{i=1}^{\rho(A)} \sum_{j=1}^{\tau(A)};$$  \hspace{1cm} (25)

and $A = \text{diag}(\epsilon P_{1}, \epsilon P_{2}, \cdots, \epsilon P_{M})$. We denote $\rho(A)$ as the number of distinct diagonal elements, $\epsilon P_{1<\theta} > \epsilon P_{1<\theta} > \cdots > \epsilon P_{1<\theta}$ as the distinct diagonal elements in decreasing order, $\tau(A)$ as the multiplicity of $\epsilon P_{1<\theta}$, and $\chi_{i,j}$ as the $(i,j)$-th characteristic coefficient of $A$. From the above, we obtain the CDF of $\theta_n = \max_{1 \leq n \leq N} \theta_n$ in the following theorem.

**Theorem 1:** The CDF of $\theta_n$ is

$$F_{\theta_n}(x) = 1 - \sum_{n=1}^{\rho(A)} \sum_{k=1}^{\tau(A)} \left( \frac{N}{n} \right)^{(1-k)n} d_{i,k} x^n,$$

$$\times \exp \left[ - \left( \frac{\gamma_s - 1}{\beta_1} + \frac{1}{\alpha} \right) n \theta \right] \left( \frac{\theta + \alpha}{(\gamma_s - 1)\epsilon P_{1<\theta}} \right)^{-k},$$  \hspace{1cm} (26)

where

$$d_{i,k} = \frac{1}{n \tau(A)} \frac{d^{\tau(A)-k}}{d x^{\tau(A)-k}} g(x) \left|_{x=-\gamma_s w_{i,j}} \right. \frac{x^n}{(\gamma_s - 1)\epsilon P_{1<\theta}};$$  \hspace{1cm} (27)

with

$$g(x) = \sum_{(i,j)} \chi_{i,j} \left[ 1 + \frac{(\gamma_s - 1)\epsilon P_{1<\theta}}{\alpha} \right]^{-j}.$$

**Proof:** See Appendix A.

From Theorem 1 and (23), we can write the lower bound on the SOP for criterion I in eqs. (29)-(30), as shown at the top of the next page, where [24, eq.(3.352.4)] and [24, eq.(3.352.3)] are used to achieve the last equality and $\Xi(a, b, k)$ is given by

$$\Xi(a, b, k) = \begin{cases} e^{ab} E_1(ab), & k = 1 \\ \frac{1}{(k-1)!} \sum_{n=1}^{k-1} (-a)^{k-n} b^n. \\ + \frac{(-a)^{k-1}}{(k-1)!} e^{ab} E_1(ab), & k \geq 2 \end{cases}$$  \hspace{1cm} (31)

B. LOWER BOUND FOR CRITERIA II AND III

We firstly express criterion II of (18) and III of (19) in a unified way as

$$n^* = \arg \max_{1 \leq n \leq N} \min(u_n, v_{1n} + c_1),$$  \hspace{1cm} (32)

where $c_1 = \tilde{P}_r$ and $c_2 = (\gamma_s - 1)(1 + \epsilon P_{1<\theta})$ correspond to criterion II, while $c_1 = 0$ and $c_2 = 1$ correspond to criterion III. Note that in the existing works such as [20] and [32],...
\[\mathcal{P}_{\text{out}}^{\text{LB}} = 1 - \sum_{n=1}^{N} \sum_{(i,j) \in \mathcal{A}} \sum_{k=1}^{n_{r}(A)} \binom{N}{n} (-1)^{n-1} \frac{\beta_{2}}{\beta_{1}} \exp \left[ - \left( \frac{n(\gamma_{s} - 1)}{P} \left( \frac{1}{\alpha} + \frac{1}{\beta_{1}} \right) \right) \right] \times \int_{0}^{\infty} e^{-\left[ \frac{1}{2} + n \left( \frac{n_{r}}{2} + \frac{n_{r}-1}{n} \right) \right]} \left[ \frac{1}{\gamma_{s}} \left( \sum_{i,j} \chi_{i,j} \left( \frac{\alpha}{\xi} \right)^{j} \right) \right] \right] = 1 - \sum_{n=1}^{N} \sum_{(i,j) \in \mathcal{A}} \sum_{k=1}^{n_{r}(A)} \binom{N}{n} (-1)^{n-1} \frac{\beta_{2}}{\beta_{1}} \exp \left[ - \left( \frac{n(\gamma_{s} - 1)}{P} \left( \frac{1}{\alpha} + \frac{1}{\beta_{1}} \right) \right) \right] \cdot \gamma_{s} \left( \sum_{i,j} \chi_{i,j} \left( \frac{\alpha}{\xi} \right)^{j} \right) \right]
\]

From Theorem 2, we write the lower bound on the SOP for criteria II and III as

\[\mathcal{P}_{\text{out}}^{\text{LB}} = \Pr \left\{ \min \left( \frac{u_{n^{*}}}{(\gamma_{s} - 1)(1 + z_{n^{*}})}, \frac{\tilde{P}_{r} + v_{1} + v_{2}^{n^{*}}}{\gamma_{s}} \right) \right\} \]

By using the PDF of \(z_{n^{*}}\) in (24) and \(f_{z_{n^{*}}}(v_{2}^{n^{*}}) = \frac{1}{2^{m}} e^{-\frac{v_{2}^{n^{*}}}{2^{m}}},\) and solving the integral, we obtain the analytical lower bound on the SOP for criteria II and III in (43), as shown at the top of this page, where \(\theta_{1} = (\gamma_{s} - 1 + 1/z_{n^{*}}) \tilde{P}_{r} + v_{2}^{n^{*}}\).

C. Asymptotic SOP for Criterion I

In order to get insights into the system behavior for criterion I, we present an asymptotic expression for the SOP, when high MER is assumed. By applying the approximation of \(e^{-x} \approx 1 - x \) and \((1 + x)^{-n} \approx 1 - n x\) for small value of \(|x|\), we obtain the asymptotic CDF of \(\theta_{n}\) as

\[F_{\theta_{n}}(\theta) \approx \frac{\gamma_{s} + (\gamma_{s} - 1)(1 + \varepsilon \tilde{P}_{r} \chi_{1})}{\alpha} \theta, \]

Proof: See Appendix B.
where we also assume a large transmit power \( P\), and \( \tilde{P}_1 \) denotes the total transmit power of interferers. From the asymptotic \( F_{\theta_0}(\theta) \), we write the asymptotic SOP for criterion I as
\[
\mathcal{P}_{\text{out}} \simeq (2\lambda + (\gamma_s - 1)(1 + \varepsilon \tilde{P}_1 A)) N \int_0^\infty v_2^{N} f_{v_2}(v_2) dv_2
\]
(45)
\[
= \frac{N!}{\lambda^N} \left( \frac{\lambda}{\alpha} \right)^N (\gamma_s - 1)(1 + \varepsilon \tilde{P}_1 A)^N, \quad (46)
\]
where \( \lambda = \frac{\beta_1}{\beta_2} \) is the MER, defined as the average channel gain ratio of the main to the eavesdropper link. From (46), we conclude that the secrecy diversity order is equal to the gain ratio of the main to the eavesdropper link. From (46),

we now provide the asymptotic SOP for criteria II and III as follows: for a given total interference power, the optimal secrecy performance is achieved with equal-power interferers, while only one effective interferer3 leads to the worst secrecy performance.

\[
\sum_{i=1}^{N} \frac{(\gamma_s - 1)(1 + \varepsilon \tilde{P}_1 A)^N}{\alpha} \left( \frac{1}{\beta_1} + \frac{c_2\alpha}{\beta_1 + c_2\alpha} \right) N \int_0^\infty v_2^{N} f_{v_2}(v_2) dv_2
\]

D. Asymptotic SOP for Criteria II and III

We now provide the asymptotic SOP for criteria II and III with high MER. By applying the approximation of \( e^{-x} \simeq \sum_{n=0}^{N-1} \frac{(-1)^n}{n!} x^n \) [29] for small value of \( |x| \), we obtain the asymptotic distributions of \( u_{n^*} \) and \( v_{n^*} \) as
\[
F_{u_{n^*}}(x) \simeq \frac{x^N}{\zeta^N} \left( \frac{\beta_1}{\beta_1 + c_2\alpha} \right)^N, \quad (47)
\]
\[
F_{v_{n^*}}(x) \simeq \frac{x^N}{c_2\zeta^N} \left( \frac{\beta_1}{\beta_1 + c_2\alpha} \right)^N, \quad (48)
\]
where we also assume a large transmit power \( P \). Then the asymptotic SOP for criteria II and III can be written by
\[
\mathcal{P}_{\text{out}} \simeq \Pr \left[ \min \left( \frac{u_{n^*}}{(\gamma_s - 1)(1 + z_{n^*})}, \frac{v_{n^*}}{\gamma_s} \right) < v_{n^*} \right], \quad (49)
\]
\[
= 1 - \Pr \left[ u_{n^*} \geq (\gamma_s - 1)(1 + z_{n^*})v_{n^*}, v_{n^*} \geq \gamma_s v_{n^*} \right], \quad (50)
\]
\[
= (\gamma_s - 1)^N \zeta^N \left( \frac{\beta_1}{\beta_1 + c_2\alpha} \right)^N \int_0^\infty \int_0^\infty (1 + z_{n^*})^n v_{n^*}^{N} \times f_{v_{n^*}} v_{n^*}^N f_{z_{n^*}} z_{n^*}^N dz_{n^*} dv_{n^*} + \frac{(\gamma_s - 1)^N}{\zeta^N} \left( \frac{\beta_1}{\beta_1 + c_2\alpha} \right)^N \int_0^\infty v_{n^*}^N f_{v_{n^*}} f_{z_{n^*}} (v_{n^*})^N dz_{n^*} dv_{n^*}. \quad (51)
\]

By applying the PDFs of \( z_{n^*} \) and \( v_{n^*} \), and then solving the integral, we obtain the asymptotic SOP for criteria II and III as
\[
\mathcal{P}_{\text{out}} \simeq \frac{N!}{\lambda^N} \left( \frac{\beta_1 + c_2\alpha}{\alpha} \right)^{N-1} \left( \frac{\beta_1(\gamma_s - 1)^N}{\alpha} T_z + \frac{\gamma_s^N}{c_2^{N-1}} \right), \quad (52)
\]
where \( T_z = E \left[ (1 + z_{n^*})^N \right] = \sum_{n=0}^{\infty} \sum_{i,j} (N) X(i)(N+j)(D_i-1)^{-1} E(P_{I\leq i}^N). \quad (53)
\]

From the asymptotic expression, it is evident that criteria II and III achieve the full secrecy diversity of order \( N \). Hence, the system secrecy performance is significantly enhanced by increasing the number of relays. Moreover, it is found from [33]–[35] that \( T_z \) is a Schur-convex function with respect to the interference power vector \( [P_{I_1}, P_{I_2}, \ldots, P_{I_M}] \). Hence, the interference power distribution affects the SOP of criteria II and III as follows: for a given total interference power, the optimal secrecy performance is achieved with equal-power interferers, while only one effective interferer3 leads to the worst secrecy performance.

V. NUMERICAL AND SIMULATION RESULTS

In this section, we present some simulation and numerical results to demonstrate the impact of co-channel interference and relay selection on the secrecy performance. All links in the network experience Rayleigh flat fading. Without loss of generality, the distance between the source S and destination D is normalized to unity, and the relays are in between. Let \( D \) denote the distance between the relays and D, so that \( \alpha = (1 - D)^{-4} \) and \( \beta_1 = D^{-4} \), where the path loss model with the exponent of 4 is used. Note that the path loss model can be used for the average channel gains of eavesdropping links. Let \( D_E \) denote the distance between the relays and E. Then \( z \) is set to \( D_E^{-4} \), and the associated MER is \( (D/D_E)^{-4} \). Since MER is related to \( D_E \), and is a key factor that regulates the secrecy performance, we prefer to use MER as a key parameter in the simulations, which can actually reflect the value of \( D_E \) since \( D_E = D \cdot \text{MER}^{-1/4} \). The average channel gain of interfering links is set to one, and the target secrecy data rate \( R_s \) is set to 0.5 bps/Hz, so that the associated secrecy SNR threshold \( \gamma_s \) is 2.

Figs. 2-4 illustrate the effect of transmit power \( P \) on the SOP with \( \lambda = 30\text{dB} \), where \( D = 0.5 \), \( N_0 = 1 \), \( M = 3 \), and \( N \) varies from 1 to 4. Specifically, Figs. 2, 3 and 4 correspond to criteria I, II and III, respectively. The total transmit power of interferers \( P_{I_A} \) is set to 10 dB, and un-equal interference power distribution is used with \( P_{I_1} = 7 \), \( P_{I_2} = 2 \) and \( P_{I_3} = 1 \). In this work, we consider the transmit power of the source

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3 As shown in [26], one effective interferer indicates that one interferer uses the total interference power to transmit signal, while the other interferes do not transmit signals.
and interferers normalized by the noise power, and hence the relative unit of $P_{IA}$ is dB. As it is observed from these figures, for each criterion and each number of relays, the lower bound on SOP is close to the simulation results in the entire region of $P$. This validates the effectiveness of the derived lower bound expression. Moreover, the SOP for each criterion is profoundly improved by increasing the number of relays, as more relays can help strengthen the secure transmission. The SOP can be also improved by increasing $P$. However, this improvement is almost saturated for large $P$, since the fixed main-to-eavesdropper ratio becomes the bottleneck of the network security.

Figs. 5-7 demonstrate the impact of relay selection and MER on the SOP with $P = 40$ dB, where $M = 2$ and the unequal interference power distribution is used with $P_{I_1} = 7$, $P_{I_2} = 2$ and $P_{I_3} = 1$. Specifically, Figs. 5, 6 and 7 correspond to criteria I, II and III, respectively. As can be seen, for each criterion, the lower bound on SOP matches well with the simulation result in the entire region of MER. This also validates the effectiveness of the derived lower bound expression. Moreover, the asymptotic result approaches the exact result with high MER, which corroborates the derived asymptotic expression for each criterion. Furthermore, the curve slope of SOP is in parallel with the number of relays, indicating that the network secrecy diversity order is equal to
N for each criterion.

Figs. 8-10 show the impact of interference power distribution on the network SOPs of the three selection criteria, where $N = 4$, $M = 3$ and the total interference power $P_{IA}$ is fixed to 10 dB. Specifically, Figs. 8, 9 and 10 correspond to criteria I, II and III, respectively. For comparison, we consider three interference scenarios: the equal-power interferers with $P_{I_1} = P_{I_2} = P_{I_3} = 10$, the distinct-power interferers with $[P_{I_1}, P_{I_2}, P_{I_3}] = [7, 2, 1]$, and the only one effective interferer with $[P_{I_1}, P_{I_2}, P_{I_3}] = [10, 0, 0]$. As can be clearly observed from Figs. 8-10 that the SOP of criterion I remains almost unchanged with the three interference scenarios, indicating that the network security is not affected by the interference power distribution. In contrast, the secrecy outage probabilities of criteria II and III are both affected by the interference scenarios. In particular, the optimal secrecy performances of criterion II and III can be achieved for the equal-power interferers, while the secrecy performances become worst for the only one effective interferer. Such observation validates the insights into the asymptotic SOP expressions of criteria II and III. We note that the interference power distribution imposes a noticeable impact on the secrecy performance of criteria II and III only in the high MER regime. This motivates us to use the asymptotic SOP to evaluate the impact of interference power distribution on the secrecy performances.

Fig. 11 compares the secrecy performances of the three selection criteria versus MER, where $N = 4$, $M = 3$ and the total interference power $P_{IA}$ is set to 10 dB. The un-equal interference power distribution with $P_{I_1} = 7$, $P_{I_2} = 2$ and $P_{I_3} = 1$ is used. For comparison, we also present the simulated SOP result of the relay selection scheme in [28]. As observed from Fig. 11, we find that criterion I outperforms criterion II by achieving lower secrecy outage probability, since the former employs the instantaneous information of interfering links in the relay selection. We then find that criterion II outperforms criterion III, since the former incorporates different impact from the two hops into the network security. Furthermore, the selection scheme in [28] achieves higher secrecy outage probability than the three selection investigated in this work. This is because that the selection scheme proposed in [28] is a partial relay selection scheme that relies on the second-hop main channel only, for the sake of low complexity.

Fig. 12 illustrates the secrecy outage probabilities of the
three selection criteria with respect to the number of interferers $M$, where $N = 3$, $P = 40$ dB and $\lambda = 30$ dB. The number of interferers varies from 1 to 5, and each interferer has the equal transmit power of 3 dB. From this figure, we find that for different number of interferers, criterion I outperforms criterion II, and criterion II outperforms criterion III, which is in accordance with the results in Fig. 11. Moreover, the network secrecy performance becomes worse when $M$ increases, since more interferers deteriorate the forwarding ability of relays.

VI. CONCLUSIONS

In this paper, we studied the communication security of multi-AF relay networks with co-channel interference. A novel lower bound expression was developed for the network secrecy outage probability, and then three selection criteria were presented to select the best relay among multiple ones, in order to deal with the co-channel interference and wiretap. For each criterion, we derived an analytical lower bound on SOP and also provided an asymptotic expression in the high MER region. From this expression, we found that each criterion achieves the full secrecy diversity order, and the interference power distribution affects the SOP of criterion II and III. Simulations and numerical results were presented to validate the proposed studies and verify the obtained insights on the system.

APPENDIX A

PROOF OF THEOREM 1

The CDF of $\theta_n = \min \left( \frac{u_n}{(\gamma_s - 1)(1 + z_n)} \right)$ is given by

\[
F_{\theta_n}(\theta) = \Pr \left[ \min \left( \frac{u_n}{(\gamma_s - 1)(1 + z_n)} \right) \leq \theta \right] = 1 - \Pr \left[ \frac{u_n}{(\gamma_s - 1)(1 + z_n)} > \theta \right].
\]

(A.1)

Since $v_{1n}$ is independent of $u_n$ and $z_n$, we can further write $F_{\theta_n}(\theta)$ as

\[
F_{\theta_n}(\theta) = 1 - \Pr \left[ u_n > (\gamma_s - 1)(1 + z_n)\theta \right] \times \Pr \left[ v_{1n} > (\gamma_s - \hat{P}_r) \right] = 1 - \int_0^\infty \int_0^\infty f_{u_n}(u_n) f_{z_n}(z_n) du_n dz_n \int_{\gamma_s - \hat{P}_r}^{\infty} f_{v_{1n}}(v) dv.
\]

(A.3)

(46) Criterion III: $P = 40$ dB

By applying the PDFs of $u_n$, $z_n$ and $v_{1n}$ into the above equation and then solving the integral, we can obtain the CDF of $\theta_n$ as

\[
F_{\theta_n}(\theta) = 1 - e^{-\frac{1}{\gamma_s} \left( \frac{\gamma_s - 1}{\gamma_s} + \frac{\gamma_s - 1}{\gamma_s} \right)} \sum_{i,j} \chi_{i,j} \left[ 1 + \frac{\theta(\gamma_s - 1)(\gamma_s - \hat{P}_i < \gamma_s >)}{\alpha} \right]^{-j}.
\]

(A.5)

By applying (26) and (26.102) into the above equation, we can arrive at the CDF of $F_{\theta_n}(\theta)$, as shown in (26) of Theorem 1.

APPENDIX B

PROOF OF THEOREM 2

From the selection criterion in (32), we now compute the CDF of $u_{n*}$ as

\[
F_{u_{n*}}(x) = \sum_{n=1}^{N} \Pr \left[ u_n \leq x, \min(u_n, v_{1n} + \frac{c_1}{c_2}) \geq \max_{1 \leq m \leq N, n \neq m} \phi_m \right],
\]

(B.1)

where $\phi_m = \min(u_m, v_{1m} + \frac{c_1}{c_2})$. Due to the symmetry among $N$ relays, we can rewrite $F_{u_{n*}}(x)$ as

\[
F_{u_{n*}}(x) = N \Pr \left[ u_1 \leq x, \min(u_1, v_{11} + \frac{c_1}{c_2}) \geq \phi_{m*} \right],
\]

(B.2)

where $\phi_{m*} = \max_{2 \leq m \leq N} \phi_m$. The CDF of $\phi_m$ is derived as

\[
F_{\phi_m}(\phi) = \Pr \left[ \min(u_m, v_{1m} + \frac{c_1}{c_2}) \leq \phi \right] = 1 - \Pr(u_n > \phi) \cdot \Pr(v_{1m} > c_2\phi - c_1).
\]

(B.3)

We now consider the two cases of $0 < \phi < \frac{c_2}{c_1}$ and $\frac{c_2}{c_1} \leq \phi$, respectively. When $0 < \phi < \frac{c_2}{c_1}$, $c_2\phi - c_1 < 0$ and hence $v_{1m} > c_2\phi - c_1$ always holds. In this case, $F_{\phi_m}(\phi)$ becomes

\[
F_{\phi_m}(\phi) = 1 - e^{-\frac{\phi}{\gamma_s}}.
\]

(B.4)
On the other hand, when \( \phi \geq \frac{c_1}{c_2} \), \( c_2\phi - c_1 \geq 0 \) holds, and \( F_{\phi_m}(\phi) \) becomes

\[
F_{\phi_m}(\phi) = 1 - e^{-\frac{\phi}{\alpha}} e^{-\frac{c_2\phi - c_1}{\beta}}. \tag{B.6}
\]

From the above CDF of \( \phi_m \), we can write the CDF of \( \phi_{m^*} \) as

\[
F_{\phi_{m^*}}(\phi) = \begin{cases} 
(1 - e^{-\frac{\phi}{\alpha}})^{N-1} \sum_{n=0}^{N-1} \binom{N}{n} e^{-\frac{c_2\phi - c_1}{\beta}}, & 0 < \phi < \frac{c_1}{c_2} \\
\hfill \left(1 - e^{-\frac{\phi}{\alpha}} e^{-\frac{c_2\phi - c_1}{\beta}}\right)^{N-1} \sum_{n=0}^{N-1} \binom{N}{n} \hfill , & \phi \geq \frac{c_1}{c_2}
\end{cases}
\]

where \( \zeta \) is defined in (35). From (B.2), we can further write \( F_{u_{m^*}}(x) \) as

\[
F_{u_{m^*}}(x) = N \int_0^{x} f_{\phi_{m^*}}(\phi) \int_0^x f_{u_1}(u_1) du_1 d\phi + N \int_{\frac{c_1}{c_2}}^{\infty} f_{\phi_{m^*}}(\phi) \left[ \int_0^x f_{u_1}(u_1) du_1 \cdot \int_{c_2\phi - c_1}^{\infty} f_{v_1}(v_1) dv_1 \right] d\phi. \tag{B.7}
\]

By applying the distributions of \( \phi_{m^*} \), \( u_1 \) and \( v_1 \) into the above equation, and then solving the integral, we can arrive at the CDF of \( u_{m^*} \), as shown in (33) of Theorem 2. Similarly, we can obtain the CDF of \( v_{1,m^*} \), as shown in Theorem 2. In this way, we have completed the proof of Theorem 2.

REFERENCES


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